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Hedge Fund Modelling and Analysis Using MATLAB®

Paul Darbyshire David Hampton

WILEY

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$\label{eq:continuous_problem} \mbox{To Mum \& Dad}$ Thank you for all your love and support, as always. P.D.

To Marie-Christine, Juliette and Antoine, with my unconditional love.

D.H.

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Preface

This book is a practical introduction to modelling and analysing hedge funds based on the MATLAB® technical computing environment. MATLAB® is a high-level language and interactive environment for numerical computation, visualisation and programming. Using MATLAB®, you can analyse data, develop algorithms and create models and applications. The language, tools and built-in maths functions enable you to explore multiple approaches and reach a solution faster than with spreadsheets or traditional programming languages, such as C/C++ or Java. MATLAB® is the foundation for all products, including Simulink® and can be extended with add-on products for a whole range of applications, including statistics, computational finance and optimisation.

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MATHWORKS CONTACT INFORMATION

For MATLAB® and Simulink product information, please contact:

The MathWorks, Inc.

3 Apple Hill Drive

Natick, MA, 01760-2098 USA

Tel: 508-647-7000

Fax: 508-647-7001

E-mail: info@mathworks.com

Web: mathworks.com

1. MATLAB® SOURCE CODE

This book assumes a working knowledge of MATLAB® and an ability to implement built-in functions and have a familiarity with developing basic MATLAB® applications.

All MATLAB® source code used throughout the book has been tried and tested with the following MATLAB® version and Operating System:

MATLAB® Version: 8.1.0.604 (R2013a)

Operating System: Microsoft Windows 8 Version 6.2

Java Version: Java 1.6.0_17-b04 with Sun Microsystems Inc.

All MATLAB $^{\circledR}$ source code is displayed in the following format.

In addition, the following MATLAB® add-on products were included in the installation:

Financial Toolbox Version 5.2

Optimisation Toolbox Version 6.4

Statistics Toolbox Version 8.3

```
%File: barchart.m
%import XL data
[~,dates,returns] = getXLData(,hfma matlab data.xlsx,,,CTA
Index.):
n = size(returns,1); %# data points
figure; %create figure
sDate = datenum(dates(1)); %set start date for x-axis
eDate = datenum(dates(end)); %set end date for x-axis
xData = linspace(sDate,eDate,n);
bar(xData, returns); %plot bar chart
xlabel(,Date,); %add x label
ylabel(,RoR (%),); %add y label
box off;
ytick = get(gca,,YTick,); %format axes
set(gca,,YTickLabel,, sprintf(,%.2f|,,ytick))
datetick(,x,,,yyyy,,,keeplimits,);
```

Sample MATLAB® source code

If %< > is used at the top of any MATLAB® source code it indicates that part of the code has been omitted for simplicity.

```
%File: optimisation.m
%< .... >
%target return, linear constraints and bounds
rstar = 9.0; %target return
Aeq = [R,;ones(1,N)];
beq = [rstar;1];
lb = zeros(N,1);
ub = ones(N,1)*0.5;
```

Sample MATLAB® source code with code omitted

2. MATLAB® USER-DEFINED FUNCTIONS

As well as making use of numerous MATLAB® built-in functions, there are many user-defined MATLAB® functions (prefixed with the letter "f") that extend functionality where necessary. All MATLAB® user-defined functions are presented in the following format:

```
%File: fStd.m
%STANDARD DEVIATION
function m2 = fStd(x,flag,f)
%------
%x: returns
%flag: 0 = sample, 1 = population
%f: reporting frequency
%m2: standard deviation (sample or population)
%-----
m2 = std(x,flag).*sqrt(f);
end
```

Sample $MATLAB^{\cite{R}}$ user-defined function

Please note that we do not give any warranty for completeness, nor do we guarantee that the code is error free. Any damage or loss incurred in the application of the MATLAB® source code, functions and concepts discussed in the book are entirely the reader's responsibility.

If you notice any errors in the MATLAB® source code or you wish to submit a new method as a user-defined MATLAB® function, algorithm, model, or some improvement to a method illustrated in the book, you are more than welcome.

3. HYPOTHETICAL HEDGE FUND DATA

Throughout the book there is constant reference to many hedge fund return series and factors. The 10 hedge funds and 15 factors used are all *hypothetical* and have been simulated by the authors as a unique data set for demonstration purposes only. The techniques and models used in the book can therefore be tested on the hypothetical data before being applied to real-life situations by the reader. The hypothetical data are nonetheless close to what would be expected in reality. The 10 funds are a mixture of several major hedge fund strategies, i.e. Commodity Trading Adviser (CTA), Long-Short Equity (LS), Global Macro (GM) and Market Neutral (MN) strategies as described in the table below:

10 hypothetical hedge funds

Hedge Fund	Abbreviation	
Commodity Trading Advisor	CTA1, CTA2, CTA3	
Long-Short Equity	LS1, LS2, LS3	
Global Macro	GM1, GM2	
Market Neutral	MN1, MN2	

The 15 factors are a mixture of both passive and active indices as described in the table below:

15 hypothetical hedge fund factors

#	Beta Factors	Abbreviation
1	Passive Global Stock Index	PSDX
2	S&P 500 Equity Index	S&P 500 Index
3	Passive Global Bond Index	PBond DX
4	Passive Long Global Commodity Index	PCom DX
5	Passive Long US\$ Index	PUSD DX
6	Risk-Free Rate	Rf
	Industry Reference Alternative Beta Factors	
7	Commodity Trading Advisor Index	CTA Index
8	Long-Short Equity Index	LS Index
	Fama French Carhart Factors	
9	Value minus Growth	Val - Gr
10	Small Cap minus Large Cap	SC - LC
11	Momentum	Mom
	Active Alternative Beta Factors	
12	Active Global Stock Futures Index	ASDX
13	Active Global Bond Futures Index	ABDX
14	Active Global Commodity Futures Index	ACDX
15	Active Global Foreign Exchange Futures Index	AFDX

4. BOOK WEBSITE

The official website for the book is located at:

www.darbyshirehampton.com

The website provides free downloads to all of the hypothetical data and MATLAB® source code as well as many other useful resources.

The authors can be contacted on any matter relating to the book, or in a professional capacity, at the following email addresses:

Paul Darbyshire: pd@darbyshirehampton.com

David Hampton: dh@darbyshirehampton.com

CHAPTER 1 The Hedge Fund Industry

The global credit crisis originated from a growing bubble in the US real estate market which eventually burst in 2008. This led to an overwhelming default of mortgages linked to subprime debt to which financial institutions reacted by tightening credit facilities, selling off bad debts at huge losses and pursuing fast foreclosures on delinquent mortgages. A liquidity crisis followed in the credit markets and banks became increasingly reluctant to lend to one another causing risk premiums on debt to soar and credit to become ever scarcer and more costly. The global financial markets went into meltdown as a continuing spiral of worsening liquidity ensued. When the credit markets froze, hedge fund managers were unable to get their hands on enough capital to meet investor redemption requirements. Not until the early part of 2009 did the industry start to experience a marked resurgence in activity realising strong capital inflows and growing investor confidence. Nevertheless, this positive growth has since been slowed as a result of the on-going European sovereign debt crisis affecting the global economy.

The aftermath of the financial crisis has clearly highlighted many of the shortcomings of the hedge fund industry and heightened the debate over the need for increased regulation and monitoring. Nevertheless, it has since been widely accepted that hedge funds played only a small part in the global financial collapse and suffered at the hands of a highly regulated banking system.

Chapter 1 introduces the concept of a hedge fund and a description of how they are structured and managed as

well as a discussion of the current state of the global hedge fund industry in the light of past and more recent financial crises. Several key investment techniques that are used in managing hedge fund strategies are also discussed. Chapter 1 aims to build a basic working knowledge of hedge funds, and along with an overview of hedge fund data sources in Chapter 2, arm the reader with the information required in order to approach and understand the more quantitative and theoretical aspects of modelling and analysis developed in later chapters.

1.1 WHAT ARE HEDGE FUNDS?

Whilst working for *Fortune* magazine in 1949, Alfred Winslow Jones began researching an article on various fashions in stock market forecasting and soon realised that it was possible to neutralise *market risk*¹ by buying undervalued securities and *short selling*² overvalued ones. Such an investment scheme was the first to employ a *hedge* to eliminate the potential for losses by cancelling out adverse market moves, and the technique of leverage³ to greatly improve profits. Jones generated an exceptional amount of wealth through his *hedge fund* over the 1950s and 1960s and continually outperformed traditional money managers. Jones refused to register the hedge fund with the Securities Act of 1933, the Investment Advisers Act of 1940, or the Investment Company Act of 1940, the main argument being that the fund was a private entity and none of the laws associated with the three Acts applied to this type of investment. It was essential that such funds were treated separately to other regulated markets since the use of specialised investment techniques, such as short selling and leverage, was not permitted under these Acts, neither was the ability to charge performance fees to investors.

So that the funds maintained their *private* status, Jones would never publicly advertise or market the funds but only sought investors through word of mouth, keeping everything as secretive as possible. It was not until 1966, through the publication of a news article about Jones' exceptional profit-making ability, that Wall Street and *High Net Worth*⁴ (HNW) individuals finally caught on and within a couple of years there were over 200 active hedge funds in the market. However, many of these hedge funds began straying from the original *market neutral* strategy used by Jones and employed other seemingly more volatile strategies. The losses investors associated with highly volatile investments discouraged them from investing in hedge funds. Moreover, the onset of the turbulent financial markets experienced in the 1970s practically wiped out the hedge fund industry altogether. Despite improving market conditions in the 1980s, only a handful of hedge funds remained active over this period. Indeed, the lack of hedge funds around in the market during this time changed the regulators' views on enforcing stricter regulation on the industry altogether. Not until the 1990s did the hedge fund industry begin to rise to prominence again and attract renewed investor confidence.

Nowadays, hedge funds are still considered private investment schemes (or vehicles) with a collective pool of capital only open to a small range of institutional investors and/or wealthy individuals and having minimal regulation. They can be as diverse as the manager in control of the capital wants to be in terms of the investment strategies and the range of financial instruments which they employ, including stocks, bonds, currencies, futures, options and physical commodities. It is difficult to define what constitutes a hedge fund, to the extent that it is now often thought in professional circles that a hedge fund is simply one that incorporates any absolute return⁵ strategy that

invests in the financial markets and applies traditional as well as non-traditional investment techniques. Many consider hedge funds to be within the class of *alternative* investments along with private equity and real estate finance that seek a range of investment strategies employing a variety of sophisticated investment techniques beyond the longer established traditional ones, such as *mutual funds*. ⁶

The majority of hedge funds are structured as limited partnerships with the manager acting in the capacity of general partner and investors as limited partners. The general partners are responsible for the operation of the fund, relevant debts and any other financial obligations. Limited partners have nothing to do with the day-to-day running of the business and are only liable with respect to the amount of their investment. There is generally a minimum investment required by accredited investors of the order of \$250,000-\$500,000, although many of the more established funds can require minimums of up to \$10 million. Managers will also usually have their own personal wealth invested in the fund, a circumstance intended to further increase their incentive to consistently generate above average returns for both the clients and themselves. In addition to the minimum investment required, hedge funds will also charge a fee structure related to both the management and performance of the fund. Such fees are not only used for administrative and on-going operating costs but also to reward employees and managers for providing positive returns to investors. A typical fee basis is the so-called 2 and 20 structure which consists of a 2% annual fee (levied monthly or quarterly) based on the amount of Assets under Management (AuM) and a 20% performance-based fee, i.e. an incentive-oriented fee. The performance-based fee, also known as carried interest, is a percentage of the annual profits and only awarded to the

manager when they have provided positive returns to their clients. Some hedge funds also apply so-called *high water marks* to a particular amount of capital invested such that the manager can only receive performance fees, on that amount of money, when the value of the capital is more than the previous largest value. If the investment falls in value, the manager must bring the amount back to the previous largest amount before they can receive performance fees again. A *hurdle rate* can also be included in the fee structure representing the minimum return on an investment a manager must achieve before performance fees are taken. The hurdle rate is usually tied to a market benchmark, such as LIBOR[§] or the one-year T-Bill rate plus a spread.

1.2 THE STRUCTURE OF A HEDGE FUND

In order for managers to be effective in the running of their business a number of internal and external parties covering a variety of operational roles are employed in the structure of a hedge fund as shown in Figure 1.1. As the industry matures and investors are requiring greater transparency and confidence in the hedge funds in which they invest, the focus on the effectiveness of these parties is growing, as are their relevant expertise and professionalism. Hedge funds are also realising that their infrastructure must keep pace with the rapidly changing industry. Whereas in the past, some funds paid little attention to their support and administrative activities, they are now aware that the effective operation of their fund ensures the fund does not encounter unnecessary and unexpected risks.

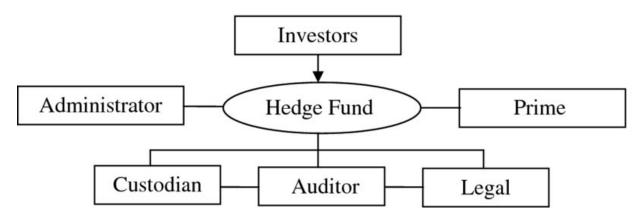


Figure 1.1 A schematic of the typical structure of a hedge fund

1.2.1 Fund Administrators

Hedge fund administrators provide many of the operational aspects of the successful running of a fund, such as compliance with legal and regulatory rulings, financial reporting, liaising with clients, provision of performance reports, risk controls and accounting procedures. Some of the larger established hedge funds use specialist in-house administrators whilst smaller funds may avoid this additional expense by outsourcing their administrative duties. Due to the increased requirement for tighter regulation and improved transparency in the industry, many investors will only invest with managers that can prove a strong relationship with a reputable third-party administrator and that the proper processes and procedures are in place (see <u>Table 1.1</u>).

Table 1.1 Top five global administrators as of 2012

Administrator
State Street Alternative Investment Solutions
Citco Fund Services
BNY Mellon Alternative Investment Services
SS&C GlobeOp
Citi Hedge Fund Services

Hedge funds with offshore operations often use external administrators in offshore locations, to provide expert tax, legal and regulatory advice for those jurisdictions. Indeed, it is a requirement in some offshore locations (e.g. the Cayman Islands) that hedge fund accounts must be regularly audited. In these cases, administrators with knowledge of the appropriate requirements in those jurisdictions would fulfil this requirement.

1.2.2 Prime Brokers

The prime broker is an external party who provides extensive services and resources to a hedge fund, including brokerage services, securities lending, debt financing, clearing and settlement and risk management. Some prime brokers will even offer incubator services, office space and seed investment for start-up hedge funds. The fees earned by prime brokers can be quite considerable and include trade commissions, loan interest and various administration charges. Due to the nature of the relationship between the prime broker and a hedge fund, in particular being the counterparty to trades and positions, only the largest financial institutions are able to act in this capacity, for example Goldman Sachs, J P Morgan and Deutsche Bank. For this reason the prime brokerage market is relatively small and each prime broker tends to