

# The Analysis of Tidal Stream Power

**JACK HARDISTY**

*The University of Hull, Kingston-upon-Hull, UK*

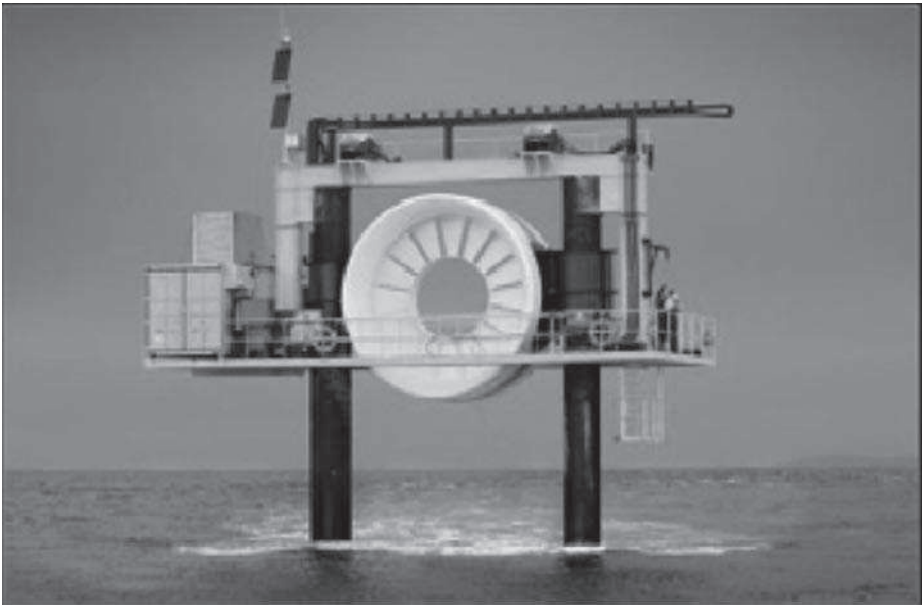
 **WILEY-BLACKWELL**

A John Wiley & Sons, Ltd., Publication



# The Analysis of Tidal Stream Power





# The Analysis of Tidal Stream Power

**JACK HARDISTY**

*The University of Hull, Kingston-upon-Hull, UK*

 **WILEY-BLACKWELL**

A John Wiley & Sons, Ltd., Publication

This edition first published 2009  
© 2009 by John Wiley & Sons Ltd.

Wiley-Blackwell is an imprint of John Wiley & Sons, formed by the merger of Wiley's global Scientific, Technical and Medical business with Blackwell Publishing.

*Registered office*

John Wiley & Sons Ltd, The Atrium, Southern Gate, Chichester, West Sussex,  
PO19 8SQ, UK

*Other Editorial Offices:*

9600 Garsington Road, Oxford, OX4 2DQ, UK  
111 River Street, Hoboken, NJ 07030-5774, USA

For details of our global editorial offices, for customer services and for information about how to apply for permission to reuse the copyright material in this book please see our website at [www.wiley.com/wiley-blackwell](http://www.wiley.com/wiley-blackwell)

The right of the author to be identified as the author of this work has been asserted in accordance with the Copyright, Designs and Patents Act 1988.

All rights reserved. No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by any means, electronic, mechanical, photocopying, recording or otherwise, except as permitted by the UK Copyright, Designs and Patents Act 1988, without the prior permission of the publisher.

Wiley also publishes its books in a variety of electronic formats. Some content that appears in print may not be available in electronic books.

Designations used by companies to distinguish their products are often claimed as trademarks. All brand names and product names used in this book are trade names, service marks, trademarks or registered trademarks of their respective owners. The publisher is not associated with any product or vendor mentioned in this book. This publication is designed to provide accurate and authoritative information in regard to the subject matter covered. It is sold on the understanding that the publisher is not engaged in rendering professional services. If professional advice or other expert assistance is required, the services of a competent professional should be sought.

*Library of Congress Cataloging-in-Publication Data*

Hardisty, J. (Jack), 1955–

The analysis of tidal stream power / Jack Hardisty  
p. cm.

Includes bibliographical references and index.

ISBN 978-0-470-72451-4

1. Tidal power-plants. 2. Tidal power. 3. Tide-waters. I. Title  
TK1081.H342 2009  
621.31'2134—dc22

2008044506

A catalogue record for this book is available from the British Library.

ISBN 978-0-470-72451-4

Set in 10/12pt Sabon by Integra Software Services Pvt. Ltd, Pondicherry, India  
Printed in Great Britain by Antony Rowe Ltd, Chippenham, Wiltshire.

First [Impression] 2009

# Contents

Preface	ix
Website contents	xi
Origin of online images	xiii
Copyright acknowledgements	xv
Symbols	xvii
<b>Part I Theory</b>	
<b>1 History of tidal and turbine science</b>	<b>3</b>
1.1 Introduction	3
<b>Part 1 Tidal science</b>	<b>4</b>
1.2 Antiquity: Aristotle and Ptolemy	4
1.3 Middle Ages: Copernicus to Galileo	7
1.4 Isaac Newton and the equilibrium theory	12
1.5 Measurement after Moray	15
1.6 Eighteenth and nineteenth centuries: Laplace to Kelvin	17
1.7 Tide-predicting machines	20
1.8 Tidal currents	22
<b>Part 2 Turbine science</b>	<b>24</b>
1.9 Antiquity: the Romans and Chinese	24
1.10 Middle Ages: the Syrians and Agricola	25
1.11 Eighteenth and nineteenth centuries: Smeaton to Kaplan	26
1.12 Modern turbines	29
1.13 Summary	30
1.14 Bibliography	30
<b>2 Tidal hydraulics</b>	<b>33</b>
2.1 Introduction	33
2.2 Elementary fluid flow	34
2.3 Hydraulic power	35
2.4 Turbulence and the Reynolds number	36
2.5 Critical flow and the Froude number	39
2.6 Bernoulli's equation	40
2.7 von Kármán's equation	42

2.8	Properties of the Airy wave	45
2.9	Tides in estuaries	46
2.10	Harmonic prediction of tidal currents	47
2.11	Turbulent characteristics of tidal currents	48
2.12	Redundancy and intermittency	50
2.13	Summary	52
2.14	Bibliography	54
<b>3</b>	<b>Principles of tidal power devices</b>	<b>55</b>
3.1	Introduction	55
3.2	Tidal wheels, mills, and barrages	57
3.3	Efficiency, capacity factor, and solidity ratio	58
3.4	Hydraulic processes, Part I: Tidal stream power	59
3.5	Hydraulic processes, Part II: Ducts and diffusers	61
3.6	Turbine processes, Part I: Drag and lift forces	64
3.7	Turbine processes, Part II: Shaft power	68
3.8	Electrical processes, Part I: Overview and generators	74
3.9	Electrical processes, Part II: Cabling and grid connection	76
3.10	Categories of turbines	78
3.11	Horizontal-axis devices	80
3.12	Vertical-axis devices (crossflow turbines)	81
3.13	Summary	85
3.14	Bibliography	87
<b>4</b>	<b>Tidal power technologies</b>	<b>89</b>
4.1	Introduction	89
4.2	Blue Energy	91
4.3	Clean Current	92
4.4	Engineering Business	93
4.5	Gorlov helical turbine	94
4.6	Hammerfest Strøm	95
4.7	Lunar Energy	96
4.8	Marine Current Turbines	98
4.9	Neptune Renewable Energy	99
4.10	OpenHydro	102
4.11	Ponte di Archimede (Kobold)	103
4.12	Pulse Generation	104
4.13	SeaPower	105
4.14	SMD Hydrovision	107
4.15	Underwater electric kite	108
4.16	Verdant Power	109
4.17	Other proposals	111
4.18	Early-stage proposals	117
4.19	Bibliography	118
<b>5</b>	<b>Modelling tidal stream power</b>	<b>121</b>
5.1	Introduction	121
5.2	Global tidal streams	122
5.3	Tidal datum and tidal heights	124
5.4	British Admiralty tidal diamonds	127
5.5	Harmonic decomposition	129



5.6	STEM display screen	137
5.7	Running STEM	142
5.8	Case study at Flat Holm in the Bristol Channel	142
5.9	Case study at Hull St Andrews in the Humber Estuary	144
5.10	Summary	146
5.11	Bibliography	149
<b>Part II Practice</b>		
<b>6</b>	<b>Economics and finance</b>	<b>153</b>
6.1	Introduction	153
6.2	The Renewable Energy Business	155
6.3	Costs	157
6.4	Revenue	161
6.5	Economic result	166
6.6	Conclusions	168
6.7	Bibliography	170
<b>7</b>	<b>North-west Europe</b>	<b>171</b>
7.1	Introduction	171
7.2	Geography of north-west Europe	173
7.3	Oceanography of north-west Europe	176
7.4	Mediterranean	181
7.5	Spain and Portugal	182
7.6	France	183
7.7	Belgium, the Netherlands, and Germany	186
7.8	Denmark and Norway	186
7.9	United Kingdom	187
7.10	The estuaries	195
7.11	Bibliography	197
7.12	Appendix: STEM outputs for north-west Europe	199
<b>8</b>	<b>North America</b>	<b>203</b>
8.1	Introduction	203
8.2	Geography of North America	206
8.3	Oceanography of North America	210
8.4	East coast of Canada	214
8.5	East coast of the United States	217
8.6	West coast of Canada	218
8.7	West coast of the United States	219
8.8	Bibliography	225
8.9	Appendix	228
<b>9</b>	<b>Australia and New Zealand</b>	<b>233</b>
9.1	Introduction	233
9.2	Timor Sea	236
9.3	Arafura Sea	238
9.4	Coral Sea	240
9.5	Bass Strait	242
9.6	New Zealand	243

9.7	Bibliography	246
9.8	Appendix: STEM outputs for Australia and New Zealand	248
<b>10</b>	<b>Rest of the world</b>	<b>249</b>
10.1	Introduction	249
10.2	Barents Sea	251
10.3	Western South Atlantic	254
10.4	Western Indian Ocean	258
10.5	East Arabian Sea	259
10.6	Indonesia and the Java Sea	262
10.7	East China and Yellow Seas	264
10.8	Bibliography	266
10.9	Appendix	268
	<b>Glossary</b>	<b>269</b>
	<b>Index</b>	<b>311</b>

# Preface

I have been engaged in marine environmental research throughout my career, but came latterly to the subject of Renewable Energy. My first contact involved an analysis of the potential for tidal power around the United Kingdom. This appeared straightforward, and 18 sites were identified (most of which are detailed now in Chapter 7) from British Admiralty tidal diamonds, and their hydraulic powers were calculated. The draft report, however, missed the Pentland Firth because there are no tidal diamonds in this very high-current regime. Therefore, when the *DTI Tidal Resource Atlas* was published a few weeks later, it was apparent that the methodology was correct (basic physics) but the results were not. There was much more to this renewable energy business than initially met the eye, and I became addicted. A whole new world of fascinating research problems opened up as we worked for some of the major players such as Lunar Energy, ITPower, Pulse Generation, and Neptune. I strove to maintain academic rigour and peer review in a fast-moving field with a harshly commercial environment. The result is this book, which attempts to set down, for the first time, the fundamental physics behind tidal stream power alongside a global analysis of its distribution and potential.

I have been very fortunate to work with some of the best British practitioners. Thanks are due to Simon Meade at Lunar Energy, Jamie O’Nians and Huw Traylor from IT Power, Pete Stratford (then) from BMT Renewables, Marc Paish from Pulse Generation, Glenn Aitken, Andrew Laver, and Nigel Petrie at Neptune Renewable Energy, and Nathalie Stephenson from Atkins Global. I have also engaged with many industrial and business people including Graham Bilaney, formerly at Dunstons, Stuart Reasbeck at IMT Marine, Ian Mitchell at Ormston, MMS Shiprepairers, David Brown Gearboxes, and the electrical engineers at Sprint and Brook Compton. Much has been learnt from these specialists.

Thanks are also due to many academic colleagues, and to the students who quickly and willingly took up undergraduate and graduate dissertations in Renewable Energy. There is a growing group in Hull University who have taken Research Masters and Doctoral programmes on some of the problems detailed in these pages, including Emma Toulson and the MRes students Tom Smith, Chris Smith, and Paul Jensen. It is an old aphorism, but no less valid that: teaching remains the best way of learning. The colleagues with whom I have discussed much, and among whom we have developed our University’s Renewable Energy centre of excellence, include Stuart McLelland, Brendan Murphy, David Calvert, and Professors Lynne Frostick, Tom Coulthard, and Mike Elliott. John Garner drew many of the diagrams herein.

In addition, and for completely different reasons, much of this book was written on the Haemodialysis Unit at Hull Royal Infirmary, and my thanks are due to my

consultant, David Eadington, and to the ward staff, particularly Sue Smith and Rita Soames. Writing was initially interrupted and later enhanced by very useful stays in the excellent Renal Transplant Unit at St James' Hospital; thanks are due to the staff there and in, particular, to Mr Ahmed and the team on Ward 59.

Finally, there is my indulgent family; I gratefully acknowledge the help and support of Paul, Tor, Lexie, Lizzie, Annette, and, in particular, my son James for always being there. Last, but by no means least, this book is for Sarah.

*Jack Hardisty  
East Yorkshire  
July 2008*

# Website contents

[www.wileyeurope.com/college/hardisty](http://www.wileyeurope.com/college/hardisty)

## 1 The simplified tidal economic model (STEM)

STEM Europe

STEM North America

STEM Australia and New Zealand

STEM Rest of the World

STEM Template

## 2 Figures and ancillary models

Figure 1.11 Newton's equilibrium tide.

Figure 2.08 von Karman's equation.

Figure 2.09 van Veen's equation.

Figure 2.11 Airy wave.

Figure 3.01 Tidal stream power.

Figure 3.06 Generalized duct power.

Figure 3.12 Turbine shaft power.

Figure 3.14 Horizontal-axis shaft power.

Figure 3.16 Vertical-axis shaft power.

Figure 5.06 Tidal regressions.

Table 2.04 Tidal species and periods.

Table 4.01 Tidal stream power devices.

Table 8.07 SE Canada flow computation.

Table 8.09 San Francisco tides.

## 3 Bibliographies and references

## 4 Original links to selected figures



# Origin of online images

This Table is available in digital format on the book's website  
[www.wileyurope.com/college/hardisty](http://www.wileyurope.com/college/hardisty)

- 1.1 <http://en.wikipedia.org/wiki/Aristotle>
- 1.2 <http://www-groups.dcs.st-and.ac.uk/~history/PictDisplay/Ptolmey.html>
- 1.3 <http://www-groups.dcs.st-and.ac.uk/~history/PictDisplay/Copernicus.html>
- 1.4 <http://www-groups.dcs.st-and.ac.uk/~history/PictDisplay/Brahe.html>
- 1.5 <http://zuserver2.star.ucl.ac.uk/~apod/apod/ap960831.html>
- 1.7 <http://zuserver2.star.ucl.ac.uk/~apod/apod/ap960830.html>
- 1.8 <http://math.usask.ca/conicsdemo/DEMO/extensions/images/descartes.jpeg>
- 1.9 <http://www.crystalinks.com/newton.html>
- 1.13 <http://content.scholastic.com/browse/article.jsp?id=5173>
- 1.15 <http://www.marxists.org/glossary/people/l/a.htm>
- 1.16 <http://snews.bnl.gov/popsi/spectroscopy.html>
- 1.17 <http://www.ingenious.org.uk/See/Naturalworld/Oceanography/?pageNo=3&s=S1&viewby=images&>
- 1.18 <http://www.gavinrymill.com/flaybrick/doodson/>
- 1.19 <http://www.gavinrymill.com/flaybrick/doodson/>
- 1.21 <http://www.nature.com/nature/journal/v410/n6832/images/4101030aa.0.jpg>
- 1.22 <http://www.uh.edu/engines/epi2194.htm>
- 1.23 <http://www.lycee-fourneyron.fr/etablissement/benoit.html>
- 1.24 [http://www.todayinsci.com/9/9\\_18.htm](http://www.todayinsci.com/9/9_18.htm)
- 1.25 [http://www.invent.org/hall\\_of\\_fame/293.html](http://www.invent.org/hall_of_fame/293.html)
- 1.26 <http://www.kekenegia.hu/viz/kaplanfoto.jpg>
- 2.1 <http://tidesandcurrents.noaa.gov/index.shtml>
- 2.3 <http://en.wikipedia.org/wiki/Image:Oreynolds.jpg>
- 2.5 [http://www.todayinsci.com/11/11\\_28.htm](http://www.todayinsci.com/11/11_28.htm)
- 2.7 <http://en.wikipedia.org/wiki/Image:Danielbernoulli.jpg>
- 2.8 [http://en.wikipedia.org/wiki/Theodore\\_von\\_K%C3%A1rm%C3%A1n](http://en.wikipedia.org/wiki/Theodore_von_K%C3%A1rm%C3%A1n)
- 2.11 <http://www-groups.dcs.st-and.ac.uk/~history/Mathematicians/Airy.html>
- 3.3 [http://en.wikipedia.org/wiki/Tide\\_mill](http://en.wikipedia.org/wiki/Tide_mill)
- 3.4 Left: <http://www.lunarenergy.co.uk>  
Right: <http://www.cleancurrent.com>
- 3.9 <http://history.nasa.gov/SP-367/f38.htm>
- 3.10 <http://www.dopsys.com/loads.htm>
- 3.11 <http://www.search.com/reference/Airfoil>
- 3.13 <http://www.dti.gov.uk/files/file29969.pdf>

- 3.23 <http://www.ossberger.de/index.php?sprache=en& pageid=1-3>
- 3.24 Left: <http://www.openhydro.com/home.html>  
Right: <http://www.marineturbines.com/home.htm>)
- 3.25 Right <http://www.waterpowermagazine.com/story.asp?storyCode=2019602>
- 3.26 [http://www.dpa.unina.it/adag/eng/renewable\\_energy.html](http://www.dpa.unina.it/adag/eng/renewable_energy.html)
- 3.27 [http://www.dpa.unina.it/adag/eng/renewable\\_energy.html](http://www.dpa.unina.it/adag/eng/renewable_energy.html)
- 3.28 [www.neptunerenewableenergy.com](http://www.neptunerenewableenergy.com)
  - 4.1 <http://bluenergy.com/technology.html>
  - 4.2 <http://www.cleancurrent.com/technology/design.htm>
  - 4.3 [http://www.engb.com/services\\_09a.php](http://www.engb.com/services_09a.php)
  - 4.4 <http://www.gcktechnology.com>
  - 4.5 <http://www.e-tidevannsennergi.com/>
  - 4.6 <http://www.lunarenergy.co.uk/productOverview.htm>
  - 4.7 <http://www.marineturbines.com/home.htm>
  - 4.9 <http://www.neptunerenewableenergy.com>
- 4.10 <http://www.neptunerenewableenergy.com>
- 4.11 <http://www.neptunerenewableenergy.com>
- 4.12 <http://www.neptunerenewableenergy.com>
- 4.13 <http://www.openhydro.com/news/OpenHydroPR-140107.pdf>
- 4.14 [http://www.pontediarchimede.it/shared\\_uploads/Download/13\\_DOCUMENTO.pdf](http://www.pontediarchimede.it/shared_uploads/Download/13_DOCUMENTO.pdf)
- 4.15 [http://www.pontediarchimede.it/shared\\_uploads/Download/13\\_DOCUMENTO.pdf](http://www.pontediarchimede.it/shared_uploads/Download/13_DOCUMENTO.pdf)
- 4.16 <http://www.pulsegeneration.co.uk/subpage.asp?id=3>
- 4.17 <http://pa/cm200001/cmsselect/cmsctech/291/291ap25.htm>
- 4.18 <http://www.smdhydrovision.com/products/?id=27>
- 4.19 [http://uekus.com/Clean\\_Energy.html](http://uekus.com/Clean_Energy.html)
- 4.20 <http://www.verdantpower.com/tech/lowimpact.html>
- 4.21 Left: <http://www.biopowersystems.com/biostream.html>
- 4.21 Right: <http://bourneenergy.com/TidalStar.html>
- 4.22 Left: <http://www.mech.ed.ac.uk/research/wavepower/tidal%20shs%20Patras%2098%20paper/tidal%20intro.htm>
- 4.22 Right: [http://cci-entreprises.icomme.fr/public/stand.php?id\\_stand=418](http://cci-entreprises.icomme.fr/public/stand.php?id_stand=418)
- 4.23 Left: <http://www.rgu.ac.uk/cree/general/page.cfm?pge=10769>
- 4.23 Right: [http://www.europeanenergyfair.com/download\\_06/13-Scotrenewable.pdf](http://www.europeanenergyfair.com/download_06/13-Scotrenewable.pdf)
- 4.24 Left: [http://www.statkraft.com/pro/energy\\_products/index.asp](http://www.statkraft.com/pro/energy_products/index.asp)
- 4.24 Right: <http://www.swanturbines.co.uk/>
- 4.25 Left: <http://www.tidalsails.com/businessidea.html>
- 4.25 Right: <http://bourneenergy.com/TidalStar.html>
- 4.26 Left: [www.dpa.unina.it/coiro/Marine-renewable-synthesis.pdf](http://www.dpa.unina.it/coiro/Marine-renewable-synthesis.pdf)
- 4.26 Right: [http://pesn.com/2006/06/13/9500281\\_Southampton\\_Tidal\\_Generator/](http://pesn.com/2006/06/13/9500281_Southampton_Tidal_Generator/)
  - 5.1 <http://www.oso.chalmers.se/~loading/loadingprimer.html>
  - 5.2 <http://www.openhydro.com/envResource.html>
  - 5.3 <http://easytide.ukho.gov.uk/EasyTide/EasyTide/index.aspx>
  - 5.7 [http://oceanservice.noaa.gov/education/kits/tides/media/supp\\_tide07B.html](http://oceanservice.noaa.gov/education/kits/tides/media/supp_tide07B.html)
- 6.2 <http://www.openhydro.com/news/OpenHydroPR-140107.pdf>
- 7.3 <http://www.nersc.no/~helge/Science/hoved.htm>



# Copyright acknowledgements

Cover image copyright and with permission from OpenHydro.

All images are the author's own except where listed.

**Images reproduced with the kind permission of the following:**

1.3 The Nicolas Copernicus University; 1.9 Crystalinks; 1.12 Cambridge University Press; 1.18 and 1.19 The Friends of Flaybrick; 2.1 NOAA National Ocean Service, Centre for Operational Oceanographic Products and Services; 3.4 (Left) Lunar Energy Ltd; 3.4 (Right) Clean Current Ltd; 3.6 and 3.7 Neptune Renewable Energy Ltd; 3.10 Doppler Systems Ltd; 3.11 Ossberger GmbH and Co; 3.13 Marine Current Turbines TM Ltd; 3.15 (Left) Neptune Renewable Energy Ltd; 3.15 (Right) Prof. D.P. Coiro, ADG Research Group, Department of Aerospace Engineering, University of Naples, Federico II, Italy; 3.23 Ossberger GmbH and Co; 3.13 Marine Current Turbines TM Ltd; 3.24 (Left) OpenHydro Ltd; 3.24 (Right) Marine Current Turbines TM Ltd; 3.26 and 3.27 Prof. D.P. Coiro, ADG Research Group, Department of Aerospace Engineering, University of Naples, Federico II, Italy; 3.28 and 3.29 Neptune Renewable Energy Ltd; 4.1 Martin J Burger of Blue Energy Canda Inc.; 3.9 NASA; 4.2 Glen Darou of Clean Current Ltd; 4.3 Steve Aghar of Engineering Business Ltd; 4.4 Gorlov Helical Turbines; 4.6 Lunar Energy Ltd; 4.7 Marine Current Turbines TM Ltd; 4.8 Neptune Renewable Energy Ltd; 4.10 and 4.11 Neptune Renewable Energy Ltd.; 4.12 and 4.13 OpenHydro Ltd.; 4.14 and 4.15 Prof. D.P. Coiro, ADG Research Group, Department of Aerospace Engineering, University of Naples, Federico II, Italy; 4.18 Soil Mechanics Dynamics Ltd.; 4.21 (Left) BioPower Systems; 4.21 (Right) Bourne Energy; 4.23 (Left) Dr Alan Owen of the Centre for Research in Energy and the Environment, The Robert Gordon University, Aberdeen; 5.2 and 6.2 OpenHydro Ltd; 6.3 Richard Dewey; 7.5 Jamie Moore, all rights ABPMer.



# Symbols

$a$	acceleration, as in, for example, Newton's laws ( $\text{m s}^{-1}$ ) (Section 1.4)
$a_A$	speed of constituent $A$ in the Kelvin equation (Section 1.8) or in the harmonic current equation (Section 1.9)
$a_K$	length of the semi-minor axis in Kepler's first law (m) (Section 1.3)
$A$	cross-sectional area of the hydrofoil blade ( $\text{m}^2$ )
$A_o$	capture area of the device ( $\text{m}^2$ ) (Section 3.4)
$A_R$	flow area at the rotor ( $\text{m}^2$ ) (Section 3.5); duct cross-sectional area at the rotor or turbine ( $\text{m}^2$ )
$b_K$	length of the semi-major axis in Kepler's first law (m) (Section 1.3)
$B$	number of blades in the turbine or rotor
$c$	Airy wave phase celerity ( $\text{m s}^{-1}$ ) (Section 2.9)
$C_D$	drag coefficient (Section 3.6)
$C_{D100}$	boundary layer drag coefficient (Section 2.7)
$C_L$	lift coefficient (Section 3.7)
$C_P$	power capacity factor of the device (Section 3.3)
$d$	distance used in Newton's analysis (m) (Section 1.4)
$e$	overall device efficiency (Section 3.3)
$e_E$	electrical efficiency (Section 3.3)
$e_H$	hydraulic efficiency of the ducting (Section 3.3)
$e_R$	rotor or turbine efficiency (Section 3.3)
$f$	rotor reducing amplitude to year of prediction in the Kelvin equation (Section 1.8)
$F$	force, as in, for example, Newton's laws (N) (Section 1.4)
$Fr$	Froude number (Section 2.4)
$Fz$	Formzahl number (Section 5.5.2)
$G$	gravitational acceleration; universal gravitational constant, as in, for example, Newton's laws (kg) (Section 1.4)
$h$	height of tide in the Kelvin equation (m) (Section 1.8) or Airy wave (Section 2.9)
$h(q)$	height of the tide at $q$ in Newton's analysis (m) (Section 1.4)
$h_{\max}$	maximum height of the tide in Newton's analysis (m) (Section 1.4)
$H$	mean amplitude of any constituent $A$ in the Kelvin equation (Section 1.8)
$H_o$	mean water level above datum in the Kelvin equation (Section 1.8)
$I_T$	turbulence intensity (Section 2.11)
$k$	wave number in the Airy expressions $= 2p/l$ (Section 2.8)

$K$	epoch of constituent $A$ in the Kelvin equation (Section 1.8)
$K_E(t)$	kinetic energy per unit area in a tidal current ( $\text{J m}^{-2}$ ) (Section 2.3)
$K_z$	coefficient of eddy viscosity in, for example, the Reynolds experiment (Section 2.4)
$K_1$	lunisolar diurnal constituent (Section 1.7)
$K_2$	lunisolar semi-diurnal constituent (Section 1.7)
$L_2$	smaller lunar elliptic semi-diurnal constituent (Section 1.7)
$m$	mass, as in, for example, Newton's laws (Section 1.4)
$M$	mass, as in, for example, Newton's laws (kg) (Section 1.4), or hydraulic power (Section 2.3)
$M_E$	mass of the Earth in, for example, Newton's analysis (kg) (Section 1.4)
$M_f$	lunar fortnightly constituent (Section 1.7)
$M_m$	lunar monthly constituent (Section 1.7)
$M_M$	mass of the moon in, for example, Newton's analysis (kg) (Section 1.4)
$M_{U2}$	principal lunar semi-diurnal current constituent (Section 5.5.3)
$M_2$	principal lunar semi-diurnal constituent (Section 1.7)
$N$	rate of revolution of the rotor ( $\text{rev min}^{-1}$ ) (Section 3.6)
$N_2$	larger lunar elliptic semi-diurnal constituent (Section 1.7)
$O_1$	lunar diurnal constituent (Section 1.7)
$p$	pressure in, for example, the Bernoulli equation ( $\text{N m}^{-2}$ ) (Section 2.6)
$P$	coefficient in Kepler's second law (Section 1.3)
$P_D(t)$	hydraulic power density ( $\text{W m}^{-2}$ ) (Section 2.3)
$P_E$	electrical output power of the device ( $\text{W}$ ) (Section 3.3)
$P_H$	hydraulic power across the capture area of the device ( $\text{W}$ ) (Section 3.3)
$P_I$	installed power of the device ( $\text{W}$ ) (Section 3.3)
$P_R$	hydraulic power at the rotor or turbine ( $\text{W}$ ) (Section 3.3)
$P_S$	turbine shaft power ( $\text{W}$ ) (Section 3.3)
$P_1$	solar diurnal constituent (Section 1.7)
$Q_1$	larger lunar elliptic diurnal constituent (Section 1.7)
$r$	distance used in Newton's analysis (m) (Section 1.4)
$R$	separation of masses, as in, for example, Newton's laws (m) (Section 1.4)
$R_F$	radius of the point of action of the force on the blade (m)
$R_R$	radius of the rotor (m) (Section 3.6)
$R_1$	semi-major axis of planet 1 in Kepler's third law (m) (Section 1.3)
$R_2$	semi-major axis of planet 2 in Kepler's third law (m) (Section 1.3)
$Re$	Reynolds number (Section 2.4)
$S$	distance used in Newton's analysis (m) (Section 1.4)
$S_{sa}$	solar semi-annual constituent (Section 1.7)
$S_{U2}$	principal solar semi-diurnal constituent (Section 5.5.3)
$S_2$	principal solar semi-diurnal constituent (Section 1.7)
$t$	time, for example, in the Kelvin equation (s) (Section 1.8)
$T$	tidal period, for example, in the Airy wave (s) (Section 2.8)
$T_S$	period of rotation of the shaft (s) (Section 3.6)
$T_{SR}$	tip speed ratio (Section 3.6)
$T_1$	sidereal period of planet 1 in Kepler's third law (m) (Section 1.3)
$T_2$	sidereal period of planet 2 in Kepler's third law (m) (Section 1.3)

$u$	velocity in, for example, the Bernoulli equation ( $\text{m s}^{-1}$ ) (Section 2.6)
$u_{100}$	tidal-current speed at 100 cm above the bed ( $\text{m s}^{-1}$ ) (Section 2.7)
$U$	horizontal downstream current in turbulent decomposition ( $\text{m s}^{-1}$ ) (Section 2.11)
$U(t)$	speed of tidal current at any time $t$ in the harmonic current equation (Section 1.9)
$U_A$	mean amplitude of any constituent $A$ in the harmonic current equation (Section 1.9)
$U_M$	horizontal downstream mean current in turbulent decomposition ( $\text{m s}^{-1}$ ) (Section 2.11)
$U_o$	mean current speed (usually $U_o = 0$ ) in the harmonic current equation (Section 1.9)
$U_R$	flow velocity at the rotor ( $\text{m s}^{-1}$ ) (Section 3.5)
$U'$	horizontal downstream turbulent current component ( $\text{m s}^{-1}$ ) (Section 2.11)
$U_*$	friction velocity ( $\text{m s}^{-1}$ ) (Section 2.4)
$U_0$	tidal velocity at the entrance to the device ( $\text{m s}^{-1}$ ) (Section 3.5)
$V$	horizontal cross-stream current in turbulent decomposition ( $\text{m s}^{-1}$ ) (Section 2.11)
$V_M$	horizontal cross-stream mean current in turbulent decomposition ( $\text{m s}^{-1}$ ) (Section 2.11)
$V_R$	tip speed of the rotor blades ( $\text{m s}^{-1}$ ) (Section 3.6)
$V'$	horizontal cross-stream turbulent current component ( $\text{m s}^{-1}$ ) (Section 2.11)
$W$	vertical current in turbulent decomposition ( $\text{m s}^{-1}$ ) (Section 2.11)
$W_M$	vertical mean current in turbulent decomposition ( $\text{m s}^{-1}$ ) (Section 2.11)
$W'$	vertical turbulent current component ( $\text{m s}^{-1}$ ) (Section 2.11)
$x$	Cartesian coordinate in Kepler's first law (m) (Section 1.3)
$y$	Cartesian coordinate in Kepler's first law (m) (Section 1.3)
$z$	elevation in, for example, the Bernoulli equation (m) (Section 2.6)
$\theta$	latitude used in Newton's analysis (m) (Section 1.4)
$\kappa$	von Karman's coefficient (Section 2.7)
$\kappa_V$	van Veen coefficient (Section 2.7)
$\lambda$	wavelength of the tide in, for example, the Airy wave (m) (Section 2.8)
$\mu$	dynamic viscosity of water in a Newtonian fluid ( $\text{kg m}^{-1} \text{s}^{-1}$ ) (Section 2.4)
$\nu$	kinematic viscosity, equal to the dynamic viscosity divided by the density in a Newtonian fluid (Section 2.4)
$\rho$	density of water = $1026 \text{ kg m}^{-3}$
$\rho_A$	phase difference when $t = 0$ in the harmonic current equation (h) (Section 1.9)
$\sigma$	Airy wave radian frequency = $2p/T$ ( $\text{rad s}^{-1}$ ) (Section 2.8)
$\tau$	shear stress in a Newtonian fluid ( $\text{N m}^{-2}$ ) (Section 2.4)
$T$	shaft torque (N m) (Section 3.6)
$\phi$	gravitational potential due to the Moon in Newton's equations (Section 1.4)



# Part I: Theory





# 1

## History of tidal and turbine science

1.1	Introduction	3
<b>Part 1</b>	<b>Tidal science</b>	4
1.2	Antiquity: Aristotle and Ptolemy	4
1.3	Middle Ages: Copernicus to Galileo	7
1.4	Isaac Newton and the equilibrium theory	12
1.5	Measurement after Moray	15
1.6	Eighteenth and nineteenth centuries: Laplace to Kelvin	17
1.7	Tide-predicting machines	20
1.8	Tidal currents	22
<b>Part 2</b>	<b>Turbine science</b>	24
1.9	Antiquity: the Romans and Chinese	24
1.10	Middle Ages: the Syrians and Agricola	25
1.11	Eighteenth and nineteenth centuries: Smeaton to Kaplan	26
1.12	Modern turbines	29
1.13	Summary	30
1.14	Bibliography	30

### 1.1 Introduction

Renewable energy in general and tidal power in particular are receiving a great deal of attention at present, driven by issues including the security of supply and the availability of hydrocarbon energy sources. Tidal power has traditionally implied the construction of turbines in a barrage for the generation of electricity (cf. Section 3.2 below). This book, however, moves the focus forward to analyse the physics and deployment of tidal stream power devices that are fixed to the seabed and generate electricity directly from the ebbing and flooding of the currents.

This chapter introduces tides and tidal phenomena through consideration of the original work of some of the great innovators. The first sections deal with the early recognition of tidal processes and the rapid progress following the adoption of the heliocentric model for the solar system. Biographical summaries are used to introduce the fundamental work of Isaac Newton and the other luminaries. Attention then turns to the development of turbine science, and progress is reviewed from the earliest water wheels through the turbines of the late eighteenth century to modern turbines and to their application in low-head tidal streams.

The essence of the problem is to be able to understand and to predict the electrical power output from, and the economics of, a tidal stream device throughout periods from a tidal cycle to a year or more. The result is a complex flow that may accelerate from rest to speeds in excess of  $3 \text{ m s}^{-1}$  before peaking, reversing, and accelerating and decelerating in the opposite direction. Within this general, daily, or twice-daily pattern will be the effects of turbulence, which generates peak flows and outputs that are significantly larger than the mean. There are also variations from the seabed to the surface. The flow will peak just below the surface and will decelerate as the seabed is approached. The rate of deceleration depends both upon the overall flow velocity and upon the nature of the seabed. Further complications include the fact that the magnitude of the flows increases and decreases over the lunar cycle, peaking a few days after the new and the full Moons and increasing still further around the equinoxes in March and September. Consideration must then be given to the type of device, to its efficiency in converting flow energy into rotary motion and then into electrical power, and, overall, to the cost of the construction and operational maintenance of the device. This is a fascinating story written alongside 3000 years of cultural, religious, and scientific history.

A very good bibliography of tidal power developments is given by Charlier (2003). This chapter is based, in part, on the books by Defant (1961), Cartwright (1999) and Andrews and Jelley (2007). Cartwright offers a scholarly historical treatise on tidal science, but it is difficult to identify the significant developments within a plethora of players. Here, by sacrificing many of the named contributors (Cartwright lists more than 200, while only 10 are identified here), it is hoped that a clearer derivation of the important principles emerges. These principles are then taken forward in the later chapters. The development of tidal turbines is based upon the first chapter in Round (2004) and the references contained therein. The principles of flow-driven power machines are shown to emerge from the work of Archimedes, Vitruvius, and Poncelet and lead to the modern turbines of Francis, Kaplan, Pelton, and others. Again, these principles are taken forward in later chapters.

## Part 1 Tidal science

### 1.2 Antiquity: Aristotle and Ptolemy

Antiquity forms the earliest period in the traditional division of European history into three 'ages': the classical civilization of Antiquity, the Middle Ages between about AD 500 and AD 1500, and then Modern Times. The early history of tidal

science is described by Pugh (1996) who reports that the first evidence of man's interaction with the rise and fall of the tide, implying some understanding of the processes, is the discovery by Indian archaeologists of a tidal dock near Ahmedabad, dating from 2000 BC (Pannikar & Srinivasan, 1971). The earliest known reference to the connection between the tides and the Moon is found in the Samaveda of the Indian Vedic period (2000–1400 BC).

### 1.2.1 Aristotle and cosmology

The development of tidal science began in Antiquity with the cosmology of Aristotle (Figure 1.1) who observed that 'ebbings and risings of the sea always come around with the Moon and upon certain fixed times'. Aristotle, working in the third century BC, used his books *On the Heavens* and *Physics* to put forward his notion of an ordered universe divided into two distinct parts, the earthly region and the heavens. The earthly region was made up of the four elements: earth, water, air, and fire. Earth was the heaviest, and its natural place was the centre of the cosmos, and for that reason, Aristotle maintained, the Earth was situated at the centre of the cosmos. The heavens, on the other hand, were made up of an entirely different substance, called the aether, and the heavenly bodies were part of spherical shells of aether from the Moon out to Mercury, Venus, the Sun, Mars, Jupiter, Saturn, and the fixed stars. Aristotle argued that the orbits of the heavenly bodies were circular and that they travelled at a constant speed.

Ingenious as this cosmology was, it turned out to be wholly unsatisfactory for astronomy. Heavenly bodies did not move with perfect circular motions: they accelerated, decelerated, and in the cases of the planets even stopped and reversed their motions. Although Aristotle and his contemporaries tried to account for these variations by splitting individual planetary spheres into components, these constructions were very complex and, ultimately, doomed to failure. Furthermore, no matter how complex a system of spheres for an individual planet became, these spheres were still



Figure 1.1 Aristotle (384–322 BC).

centred on the Earth. The distance of a planet from the Earth could therefore not be varied in this system, but planets varied in brightness. Since variations in intrinsic brightness were ruled out, and since spheres did not allow for a variation in planetary distances from the Earth, variations in brightness could not be accounted for in this system.

Other developments in tidal science at this time included those by Pytheas who travelled through the Strait of Gibraltar to the British Isles and reported the half-monthly variations in the range of the Atlantic Ocean tides, and that the greatest ranges (Spring tides) occurred near the new and the full Moons.

Many other aspects of the relationship between tides and the Moon are noted in Pliny the Elder's (AD 23–79) *Natural History*. Pliny described how the maximum tidal ranges occur a few days after the new or full Moon, and how the tides at the equinoxes in March and September have a larger range than those at the summer solstice in June and winter solstice in December.

### 1.2.2 Ptolemy's geometrical solar system

Mathematicians who wished to create geometrical models of the solar system in order to account for the actual motions of heavenly bodies began using different constructions within a century of Aristotle's death. Although these violated Aristotle's physical and cosmological principles somewhat, they were ultimately successful in accounting for the motions of heavenly bodies. We see the culmination of these efforts in the work of Claudius Ptolemy (Figure 1.2). In his great astronomical work *Almagest*, Ptolemy presented a complete system of mathematical constructions that accounted successfully for the observed motion of each heavenly body. Ptolemy used three basic constructions, the eccentric, the epicycle, and the equant, to describe the movements of the planets, the Sun, and the Moon. With such combinations of constructions, Ptolemy was able to account for the motions of heavenly bodies within the standards of observational accuracy of his day.



Figure 1.2 Claudius Ptolemy (AD 90–168).

Early explanations for the tides were curious; Aristotle is credited with the law that no animal dies except when the water is ebbing. This idea survived into popular culture. For example, as recently as 1595 in the North of England, the phase of the tide was recorded at the time of each person's death. Eastern cultures held the belief that the water was the blood of the Earth and that the tides were caused by the Earth breathing.

### 1.3 Middle Ages: Copernicus to Galileo

The Middle Ages was a period of great cultural, political, and economic change in Europe and is typically dated from around AD 500 to approximately AD 1500. During the early Middle Ages, for example, the Venerable Bede (673–735) was familiar with the tides along the coast of Northumbria in England, and was able to calculate the tides using the 19 year lunar cycle. By the early ninth century, tide tables and diagrams showing how Neap and Spring tides alternate were appearing in several manuscripts.

#### 1.3.1 Copernicus's heliocentric solar system

Although Aristotelian cosmology and Ptolemaic astronomy were still dominant, it was the fundamental change brought about by Copernicus's heliocentric view that removed the barriers to progress and opened the way for the advancement of tidal science by Newton's deterministic analysis in the seventeenth century.

The Polish astronomer Copernicus (Figure 1.3) proposed that the planets have the Sun as the fixed point to which their motions are to be referred and that the Earth is a planet that, besides orbiting the Sun annually, also turns once daily on its own axis. He also recognized that the very slow long-term changes in the direction of this axis account for the precession of the equinoxes. This of the heavens is



Figure 1.3 Nicolaus Copernicus (1473–1543).

usually called the heliocentric, or ‘Sun-centred’, system – derived from the Greek *helios*, meaning ‘Sun’. Copernicus wrote about these ideas in a manuscript called the *Commentariolus* (‘Little Commentary’) during the period 1508–1514. However, the work that contains the final version of his theory, *De revolutionibus orbium coelestium libri vi* (‘Six Books Concerning the Revolutions of the Heavenly Orbs’), did not appear in print until 1543, the year of his death.

### 1.3.2 Tycho Brahe’s observations

Tyge (latinized as Tycho) Brahe (Figure 1.4) was born in Skane, Sweden (The Galileo Project, 2007). He attended the Universities of Copenhagen and Leipzig, and then travelled through Germany, studying at Wittenberg, Rostock, and Basel. His interest in astronomy was aroused during this period, and he bought several astronomical instruments. Tycho Brahe lost part of his nose in a duel with another student, in Wittenberg in 1566, and for the rest of his life he wore a metal insert to cover the scar. He returned to Denmark in 1570.

Brahe accepted an offer from King Frederick II in the 1570s to fund an observatory. He was given the little island of Hven in the Sont near Copenhagen, and there he built Uraniburg, which became the finest observatory in Europe. Brahe designed and built new instruments, calibrated them, and instituted nightly observations. He also ran his own printing press. His observations were not published during his lifetime, but he employed Johannes Kepler as an assistant to calculate planetary orbits from the data. Brahe did not entirely abandon the Copernican, Earth-centred approach because, he argued, if the Earth were not at the centre of the universe, physics, as it was then known, was utterly undermined. Instead, he developed a system that combined the best of both worlds. He kept the Earth in the centre of the universe, so that he could retain Aristotelian physics. The Moon and Sun revolved



Figure 1.4 Tycho Brahe (1546–1601).