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# Uncertainty Quantification in Computational Fluid Dynamics and Aircraft Engines



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ISSN 2191-530X                      ISSN 2191-5318 (electronic)  
SpringerBriefs in Applied Sciences and Technology  
ISBN 978-3-319-14680-5              ISBN 978-3-319-14681-2 (eBook)  
DOI 10.1007/978-3-319-14681-2

Library of Congress Control Number: 2015930818

Springer Cham Heidelberg New York Dordrecht London

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*To Manola and Marcello*

# Preface

It is no wonder that Uncertainty Quantification has become more and more of an actuality in the last decade as the modelling capability jointly with computational power has increased a lot. In the past, the capability to predict flow field and performance in aero engines as well as in turbomachinery was of great support to the design. However, the range of errors in such results was so large as to suggest the use of CFD, mainly to understand the direction of trends and improvements more than the exact evaluation of thermo-fluid-dynamic parameters, which could affect performance, reliability and life of the engine components.

Recently, we have seen two different but relevant matters:

- the improvement of simulation and modelling capabilities, with increasing accuracy and reliability linked as well to the enhanced computing capability offered by massive Parallel Computing architectures;
- the marginal space left to increase the efficiency and reliability of turbomachinery components in aero engines that is approaching the theoretical limits; because of this fact the competition among producers is becoming continuously stronger and critical.

In this environment, the uncertainty on the real configuration of the components both in terms of geometry and real operational conditions becomes a key point and the capability to manage properly these elements both in the design phase and in the monitoring and diagnostic of the engines can be winner elements.

We can only imagine the tremendous impact that this is going to have in the coming years, helping engineers to develop more reliable configurations able to withstand random variations and unexpected failures. Yet, it is strangely difficult to find any book explaining the impact of manufacturing deviations in different components and how UQ should be used to address this problem. It was to supply this need that the present work was written. This monograph represents a valid contribution to the understanding of the methodology that even today can be carried out to control and manage this tough matter.

This book has been written with the support of various academic and industrial actors who provided elements from both real-life experience in the design/production and theoretical and conceptual contest.

This work will provide a wide review of the configuration affected by uncertainty in aero engines as well as of the more up-to-date tools that can be implemented. It is my hope that this book may do something to encourage and direct the reader in studying Uncertainty Quantification and to identify how this will help in the development of future engines.

Firenze, November 2014

Prof. Francesco Martelli



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