



Darko Dujmović / Boris Androić / Ivan Lukačević

# Composite Structures according to Eurocode 4

## Worked Examples

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**Dujmović / Androić / Lukačević**

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Worked Examples

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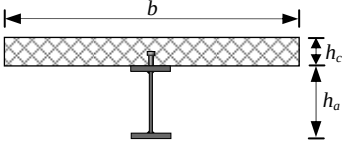
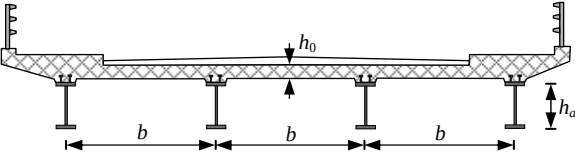
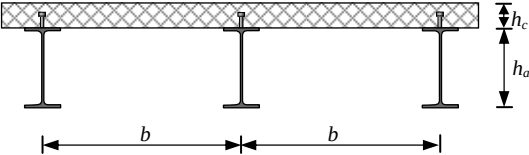
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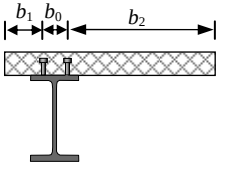
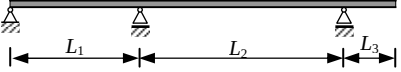
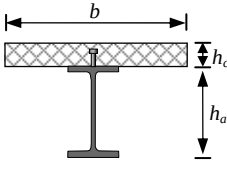
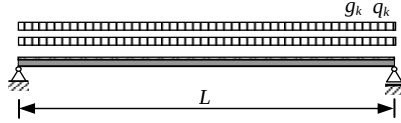
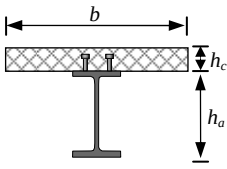
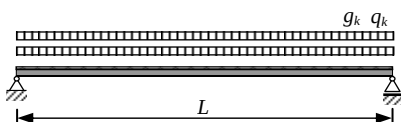
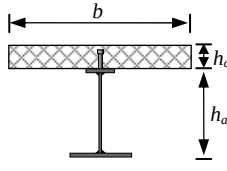
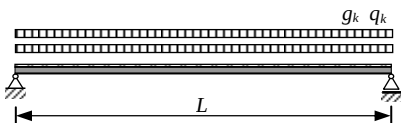
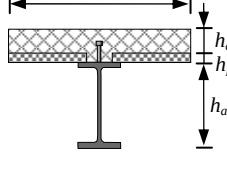
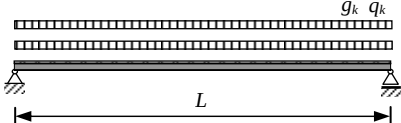
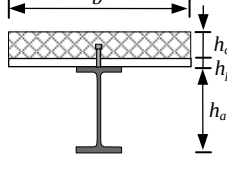
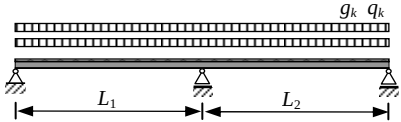
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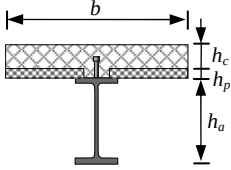
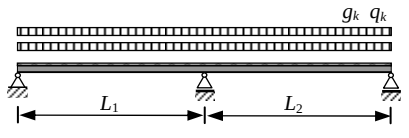
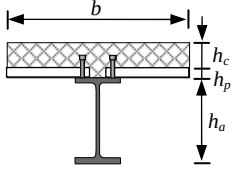
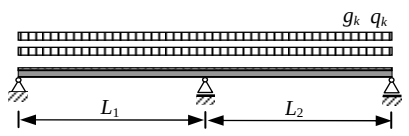


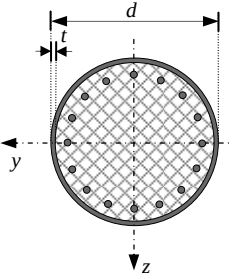
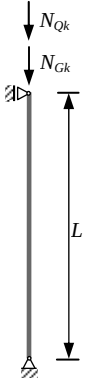
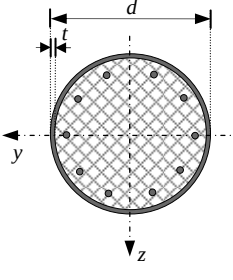

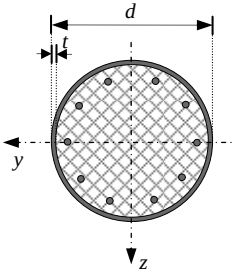
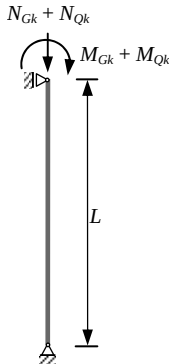


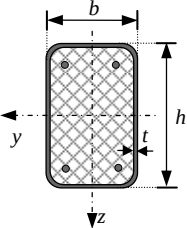
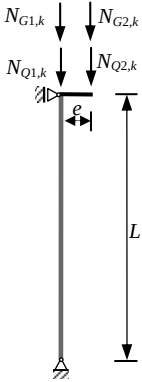
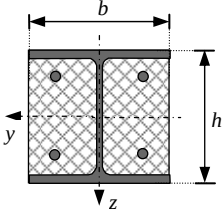
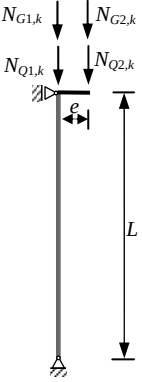
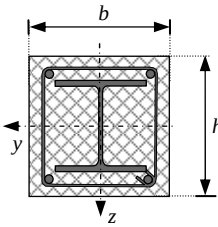
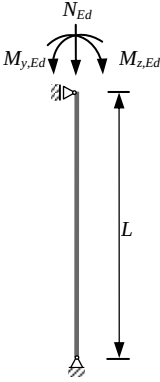
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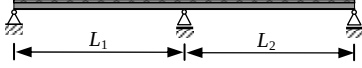

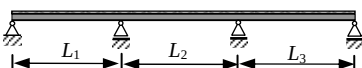

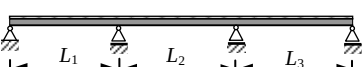

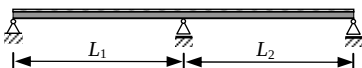
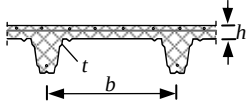
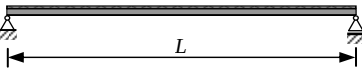
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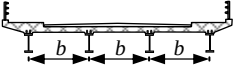
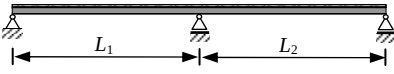
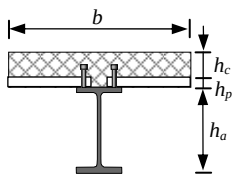
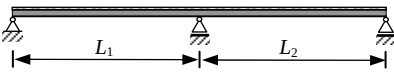
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