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Advances in Ranking and Selection, Multiple Comparisons, and Reliability

Methodology and Applications

N. Balakrishnan

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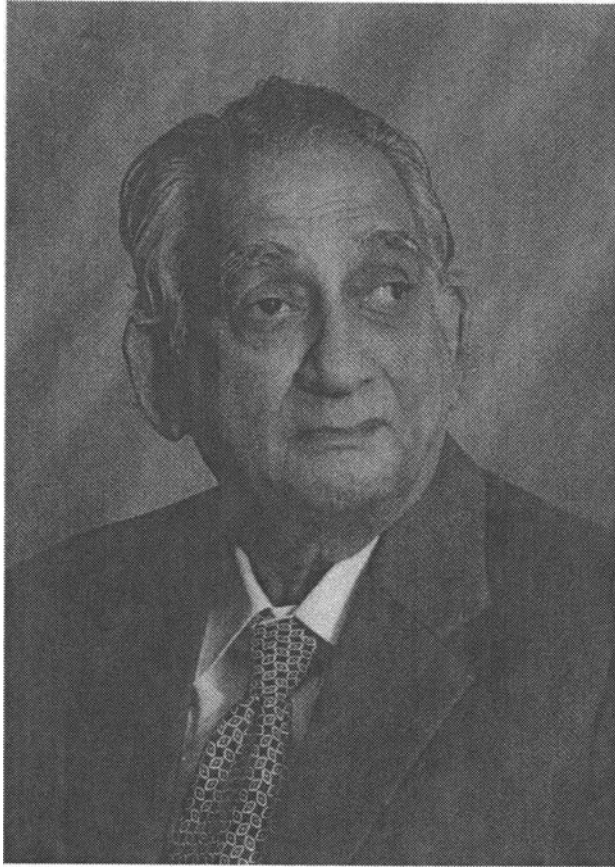
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In Honor of S. Panchapakesan



S. Panchapakesan

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Preface

Prof. S. Panchapakesan has made significant contributions to the area of ranking and selection. Besides ranking and selection, he has also published in many other areas of statistics including order statistics, reliability theory, stochastic inequalities, and inference.

In order to reflect his diverse interests and also to recognize his important contributions to different areas, we invited a number of authors to write articles for this volume. These authors form a representative group from coauthors, friends, colleagues and other close professional associates of S. Panchapakesan, in addition to being experts working in one or more of the above-mentioned areas. All the articles present here have been peer reviewed and carefully organized into 20 chapters. For the convenience of the readers, this volume has been divided into the following parts:

- INFERENCE
- RANKING AND SELECTION
- MULTIPLE COMPARISONS AND TESTS
- AGREEMENT ASSESSMENT ANALYSIS
- RELIABILITY
- BIostatISTICS

The above list has taken into account various types of inferential problems of interest. This volume is *not* a proceedings, although many of the authors were present at an International Conference held in honor of S. Panchapakesan during December 2002 in Chennai, Tamilnadu, India.

Our sincere thanks go to all the authors who have contributed to this volume. They all share our admiration and appreciation of S. Panchapakesan for all his contributions and sincere work during the past 35 years, and have given us their full cooperation and support in bringing this volume out. We are also indebted to the referees for helping us in the evaluation of the manuscripts and in improving the quality of this publication. In particular, we thank Professors Dipak Dey, Wen-Tao Huang and Nitis Mukhopadhyay for their assistance in the editorial process.

Special thanks are due to Mrs. Debbie Iscoe for the excellent typesetting of the entire volume. Finally, we thank Mr. Thomas Grasso (Editor, Birkhäuser, Boston) for the invitation and encouragement to undertake this project.

With great pleasure, we dedicate this volume to our beloved friend and colleague, S. Panchapakesan.

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October 2004

S. Panchapakesan

Career and Accomplishments

Subramanian Panchapakesan was born on August 27, 1933, to Subramanian and Visalakshi, in Mylapore, Madras (currently known as Chennai). In 1938, his whole family moved to Pudukkottai in Tamilnadu where he completed the first thirteen years of his studies – first to eleventh standards of his school in an institution run by the Church of Swedish Mission, and then two years of Intermediate in Arts and Sciences at the Rajah's College. He then moved to Madras for further studies at Vivekananda College, obtaining a B.A. (Honours) in Mathematics from the University of Madras in 1954. This B.A. (Honours) degree was equivalent to the M.A. degree, but he had to wait for a year to get the M.A. degree in Mathematics because of some technical reasons.

During 1955–1960, he served as a Lecturer in Mathematics at Islamiah College in Vaniyambadi, Tamilnadu. He left this position in 1960 to join the Indian Statistical Institute (ISI), Calcutta, where he obtained a M.Stat. degree in 1962. For the next two years, he held a Research Assistantship in the Research and Training School of the ISI. During this period, he also spent six months in Hyderabad, Andhra Pradesh, as Officer-in-Charge of Evening Centre run by the ISI and the rest of the period as an instructor at the International Statistical Education Centre (ISEC). This training centre was run by the ISI under a United Nations program. In February 1965, he joined the technical staff in the Data Processing Unit of the Research and Training School of the ISI. After six months, he resigned to go to Purdue University, West Lafayette, Indiana, to do his graduate study in statistics. He received his Ph.D. in Mathematical Statistics in 1969 for his thesis entitled *Some Contributions to Multiple Decision (Selection and Ranking) Procedures* written under the guidance of Professor Shanti Swarup Gupta. With this, he started his illustrious career and made pioneering contributions to the area of Ranking and Selection Methodology and many other areas of Statistics.

Subsequent to his Ph.D., he took a one-year visiting Assistant Professorship in the Department of Statistics at Purdue University. In 1970, he joined the Department of Mathematics at Southern Illinois University, Carbondale, Illinois,

as an Assistant Professor. He was promoted to the rank of Associate Professor in 1974 and then to Full Professor in 1980. After a 28-year service there, he retired on June 1, 1998, and currently holds the title of Professor Emeritus in that department.

He had visiting appointments in the Department of Statistics at Purdue University during the fall term of 1975, and the spring terms of 1984 and 1986. He also went as a Visiting Expert to the Institute of Mathematics at Academia Sinica, Taipei, Taiwan, during the spring term of 1980.

He has provided valuable service to many research journals in various capacities. Included in this list are: Member of the International Editorial Board of *Communications in Statistics* during 1985–1994. Associate Editor of *Journal of Statistical Planning and Inference* during 1984–2000. Member of the Editorial Board of *American Journal of Mathematical and Management Sciences* since 1993, and Associate Editor of *Communications in Statistics* since 2001.

S. Panchapakesan, through his pioneering research in the area of ranking and selection over the last 35 years, has made a significant impact in this area. He has not only inspired and encouraged, but also mentored and helped numerous young researchers.

Now that he is retired and is free from teaching and administrative duties, we are confident that he will continue to make fine contributions to the field with renewed interest, enthusiasm and energy. In addition, he will also have more time to enjoy the Indian classical music, his lifelong interest.

Publications

Books

1. *Multiple Decision Procedures: Methodology of Selecting and Ranking Populations* (co-authored with S. S. Gupta), New York: John Wiley & Sons, 1979. Republished as: *Classics in Applied Mathematics*, 44, SIAM, Philadelphia, 2002.
2. *Advances in Statistical Decision Theory and Applications* (co-edited with N. Balakrishnan), Birkhäuser, Boston, 1997.

Articles in Journals/Books and Technical Reports

1967

1. Order statistics arising from independent binomial populations (with S. S. Gupta), *Mimeograph Series No. 120*, Department of Statistics, Purdue University, West Lafayette, Indiana.

1969

2. Some selection and ranking procedures for multivariate normal populations (with S. S. Gupta), In *Multivariate Analysis II: Proceedings of the Second International Symposium on Multivariate Analysis* (Ed., P. R. Krishnaiah), pp. 475-505, Academic Press, New York.
3. On the distribution of the maximum and minimum of ratios of order statistics (with R. E. Barlow and S. S. Gupta), *Annals of Mathematical Statistics*, 40, 918-934.
4. Selection and ranking procedures (with S. S. Gupta), In *The Design of Computer Simulation Experiments* (Ed., T. H. Naylor), pp. 132-160, Duke University Press, North Carolina.
5. Some contributions to multiple decision (selection and ranking) procedures, *Mimeograph Series No. 192*, Department of Statistics, Purdue University, West Lafayette, Indiana.

1971

6. On a subset selection procedure for the most probable event in a multinomial distribution, In *Statistical Decision Theory and Related Topics* (Eds., S. S. Gupta and J. Yackel), pp. 275–298, Academic Press, New York.
7. Contributions to multiple decision (subset selection) rules, multivariate distribution theory and order statistics (with S. S. Gupta), *Technical Report ARL 71-0218*, Aerospace Research Laboratories, Dayton, Ohio.

1972

8. On a class of subset selection procedures (with S. S. Gupta), *Annals of Mathematical Statistics*, **43**, 814–822.
9. On multiple decision (subset selection) procedures (with S. S. Gupta), *Journal of Physical and Mathematical Sciences*, **6**, 1–72.

1973

10. On order statistics and some applications of combinatorial methods in statistics (with S. S. Gupta), In *A Survey of Combinatorial Theory* (Ed., J. N. Srivastava), pp. 217–250, North-Holland Publishing Company, Amsterdam.
11. On order statistics from equally correlated normal random variables (with S. S. Gupta and K. Nagel), *Biometrika*, **60**, 403–413.
12. Inference for restricted families: (A) multiple decision procedures; (B) order statistics inequalities (with S. S. Gupta), In *Reliability and Biometry: Statistical Analysis of Life Length* (Eds., F. Proschan and R. J. Serfling), pp. 503–596, SIAM, Philadelphia.

1974

13. On moments of order statistics from independent binomial populations (with S. S. Gupta), *Annals of the Institute of Statistical Mathematics Supplement*, **8**, 95–113.

1975

14. On a quantile selection procedure and associated distribution of ratios of order statistics from a restricted family of probability distributions (with S. S. Gupta), In *Reliability and Fault Tree Analysis* (Eds., R. E. Barlow, J. B. Fussell and N. D. Singpurwalla), pp. 557–576, SIAM, Philadelphia.

1976

15. A modified subset selection formulation with special reference to one-way and two-way layout experiments (with D.-Y. Huang), *Communications in Statistics—Theory and Methods*, **5**, 621–633.

1977

16. Subset selection procedures for Δ_p -superior populations (with T. J. Santner), *Communications in Statistics—Theory and Methods*, **6**, 1081–1090.

1978

17. A subset selection formulation of the complete ranking problem (with D.-Y. Huang), *Journal of the Chinese Statistical Association*, **16**, 5801–5810.
18. On a monotonicity property relating to gamma distributions, *Journal of the Chinese Statistical Association*, **16**, 6003–6005.

1980

19. Some statistical techniques in climatological data (with S. S. Gupta), In *Statistical Climatology: Developments in Atmospheric Science*, **13** (Eds., S. Ikeda et al.), pp. 35–48, Elsevier Scientific Publishing Company, Amsterdam.

1981

20. ASA and statistical education (with S. S. Gupta), In *Proceedings of the American Statistical Association - Section on Statistical Education*, pp. 27–29, Alexandria, Virginia.

1982

21. On eliminating inferior regression models (with D.-Y. Huang), *Communications in Statistics—Theory and Methods*, **11**, 751–759.
22. Some locally optimal subset selection rules based on ranks (with D.-Y. Huang), In *Statistical Decision Theory and Related Topics-III* (Eds., S. S. Gupta and J. O. Berger), Vol. 2, pp. 1–14, Academic Press, New York.

1984

23. Some locally optimal subset selection rules for comparison with a control (with D.-Y. Huang), *Journal of Statistical Planning and Inference*, **9**, 63–72.

24. On some inequalities and monotonicity results in selection and ranking theory (with S. S. Gupta and D.-Y. Huang), In *Inequalities in Statistics and Probability* (Ed., Y. L. Tong), IMS Lecture Notes - Monograph Series, Vol. 5, pp. 211–227, Institute of Mathematical Statistics, Hayward, California.
25. An estimation problem relating to subset selection from normal populations (with S. Jeyaratnam), In *Design of Experiments: Ranking and Selection* (Eds., T. J. Santner and A. C. Tamhane), pp. 287–302, Marcel Dekker, New York.
26. Edgeworth expansions in statistics: some recent developments (with S. S. Gupta), In *Colloquia Mathematica Societatis János Bolyai: 34. Limit Theorems in Probability and Statistics, Vol. I* (Ed., P. Révész), pp. 519–565, North-Holland Publishing Company, Amsterdam.

1985

27. On the distribution of the studentized maximum of equally correlated normal random variables (with S. S. Gupta and J. K. Sohn), *Communications in Statistics—Simulation and Computation*, **14**, 103–135.
28. Subset selection procedures: review and assessment (with S. S. Gupta), *American Journal of Mathematical and Management Sciences*, **5**, 235–311.
29. Shanti S. Gupta: an appreciation (with T. J. Santner), *American Journal of Mathematical and Management Sciences*, **5**, 347–369.
30. Estimation after subset selection from exponential populations (with S. Jeyaratnam), *Communications in Statistics—Theory and Methods*, **15**, 3459–3473.

1986

31. Estimation of $\Pr(X > Y)$ for gamma distributions (with R. Ismail and S. Jeyaratnam), *Journal of Statistical Computation and Simulation*, **26**, 253–267.

1987

32. Statistical selection procedures in multivariate models (with S. S. Gupta), In *Advances in Multivariate Statistical Analysis* (Ed., A. K. Gupta), pp. 141–160, D. Reidel Publishing Company, Dordrecht, Holland.

1988

33. Inference about the change-point in a sequence of random variables: a selection approach (with T. Liang), In *Statistical Decision Theory and Related Topics-IV* (Eds., S. S. Gupta and J.O. Berger), Vol. 2, pp. 79–87, Springer-Verlag, New York.
34. Selection and ranking procedures in reliability models (with S. S. Gupta), In *Handbook of Statistics 7: Quality Control and Reliability* (Eds., P. R. Krishnaiah and C. R. Rao), pp. 131–156, North-Holland Publishing Company, Amsterdam.
35. Prediction intervals for balanced one-factor random models (with S. Jeyaratnam), In *Probability and Statistics: Essays in Honor of F. A. Graybill* (Ed., J. N. Srivastava), pp. 161–170, North-Holland Publishing Company, Amsterdam.
36. Selection from uniform populations based on sample midranges and an associated estimation after selection (with S. Jeyaratnam), *Communications in Statistics—Theory and Methods*, **17**, 2303–2314.
37. Prediction intervals for the random intercept linear model (with S. Jeyaratnam), *Communications in Statistics—Theory and Methods*, **17**, 3067–3073.

1989

38. Entropy based subset selection from Bernoulli populations (with S. Jeyaratnam), In *Computing and Information* (Eds., R. Janicki and W. W. Koczkodaj), Vol. II, pp. 202–204, Canadian Scholars' Press Inc., Toronto.

1990

39. Preliminary test based sometimes-pool estimator of the Bernoulli entropy function (with S. Jeyaratnam), In *Advances in Computing and Information* (Eds., S. G. Akl, F. Fiala and W. W. Koczkodaj), pp. 16–18, Canadian Scholars' Press Inc., Toronto.

1991

40. On sequential ranking and selection procedures (with S. S. Gupta), In *Handbook of Sequential Analysis* (Eds., B. K. Ghosh and P. K. Sen), pp. 363–380, Marcel Dekker, New York.

41. An empirical Bayes procedure for selecting the most homogeneous multinomial population according to the Gini-Simpson index (with T. Liang), In *The Proceedings of the 1990 Taipei Symposium in Statistics* (Eds., M. T. Chao and P. E. Cheng), pp. 447–460, Institute of Statistical Science, Academia Sinica, Taipei, Taiwan.

1992

42. Ranking and selection procedures, In *Handbook of the Logistic Distribution* (Ed., N. Balakrishnan), pp. 145–167, Marcel Dekker, New York.
43. On a monotone empirical Bayes test procedure in geometric model (with T. Liang), *Annals of the Institute of Statistical Mathematics*, **44**, 133–140.
44. Isotonic selection with respect to a control: A Bayesian approach (with T. Liang). In *The Frontiers of Modern Statistical Inference Procedures, II* (Eds., E. Bofinger et al.), pp. 273–285. American Sciences Press, Syracuse, New York.

1993

45. A two-stage procedure for selecting δ^* -optimal guaranteed lifetimes in the two-parameter exponential model (with T. Liang), In *Multiple Comparisons, Selection, and Applications in Biometry: A Festschrift in Honor of Charles W. Dunnett* (Ed., F. M. Hoppe), Chapter 20, pp. 353–365, Marcel Dekker, New York.
46. Selection and screening procedures in multivariate analysis (with S. S. Gupta), In *Multivariate Analysis: Future Directions* (Ed., C. R. Rao), North-Holland Series in Statistics and Probability, Vol. 5, Chapter 12, pp. 223–262. Elsevier Science Publishers, Amsterdam.
47. Robustness of selection procedures: an overview, In *Selection Procedures I: Proceedings of the 3rd Schwerin Conference on Mathematical Statistics* (Eds., G. Herrendorfer and K. J. Miescke), pp. 134–146, Agricultural University, Dummerstorf-Rostock, Germany.
48. Multistage subset selection procedures for normal populations and associated second-order asymptotics (with N. Mukhopadhyay), *Metron*, **21**, 25–42.

1994

49. An integrated formulation for selecting the best normal population and eliminating bad ones (with P. Chen). In *Compstat 1994* (Eds., R. Dutter and W. Grossman), pp. 18–19, University of Technology and University of Vienna, Vienna, Austria.

50. Selecting among the multinomial losers (with P. Chen and M. Sobel), *Sequential Analysis*, **13**, 177–200.

1995

51. Estimation of the location and scale parameters of the extreme value distribution based on multiply type-II censored samples (with N. Balakrishnan and S. S. Gupta), *Communications in Statistics—Theory and Methods*, **24**, 2105–2125.
52. Estimation of the mean and standard deviation of the logistic distribution based on multiply type-II censored samples (with N. Balakrishnan and S. S. Gupta), *Statistics*, **27**, 127–142.
53. Selection of the normal population with the largest absolute mean, In *Bulletin of the International Statistical Institute, Contributed Papers of the 50th Session*, Book 2, pp. 955–956.
54. Selection and ranking procedures, In *The Exponential Distribution: Theory, Methods and Applications* (Eds., N. Balakrishnan and A. P. Basu). Chapter 16, pp. 259–278, Gordon and Breach Science Publishers, Newark, New Jersey.
55. Exponential classification and applications (with N. Balakrishnan and Q. Zhang), In *The Exponential Distribution: Theory, Methods and Applications* (Eds., N. Balakrishnan and A. P. Basu), Chapter 32, pp. 525–546, Gordon and Breach Science Publishers, Newark, New Jersey.
56. Multiple decision procedures in analysis of variance and regression analysis (with S. S. Gupta and D.-Y. Huang), *Technical Report No. 95-44c*, Department of Statistics, Purdue University, West Lafayette, Indiana.

1996

57. A review of robustness of selection procedures, *Journal of Statistical Planning and Inference*, **54**, 279–290.
58. Design of experiments with selection and ranking goals (with S. S. Gupta), In *Handbook of Statistics 13: Design and Analysis of Experiments* (Eds., S. Ghosh and C. R. Rao), Chapter 17, pp. 555–585, Elsevier Science Publishers, Amsterdam.
59. δ -exceedance records (with N. Balakrishnan and K. Balasubramanian), *Journal of Applied Statistical Sciences*, **4**, 123–132.

1997

60. An integrated formulation for selecting the best from several normal populations in terms of the absolute values of their means: common known variance case (with S. Jeyaratnam), In *Advances in Statistical Decision Theory and Applications* (Eds., S. Panchapakesan and N. Balakrishnan), Chapter 19, pp. 277–289, Birkhäuser, Boston.

1998

61. Inverse sampling procedures to test for homogeneity in a multinomial distribution (with A. Childs, B. H. Humphrey and N. Balakrishnan), In *Handbook of Statistics 17: Order Statistics and Their Applications* (Eds., N. Balakrishnan and C.R. Rao), Chapter 14, pp. 259–265, Elsevier Science Publishers, Amsterdam.
62. A two-stage procedure for selecting from normal populations the one with the largest absolute mean: common unknown variance case (with S. Jeyaratnam). In *Proceedings of the 3rd St. Petersburg Workshop on Simulation* (Eds., S. M. Ermakov, Y. N. Kashtanov and V. B. Melas), pp. 259–265. Saint Petersburg University Press, St. Petersburg, Russia.

2000

63. Selecting from normal populations the one with the largest absolute mean: common unknown variance case (with S. Jeyaratnam), In *Advances in Stochastic Simulation Methods* (Eds., N. Balakrishnan, S. M. Ermakov and V. B. Melas), Chapter 16, pp. 283–292, Birkhäuser, Boston.

2001

64. Simultaneous selection of extreme populations from a set of two-parameter exponential populations (with K. Hussein), In *Handbook of Statistics 20: Advances in Reliability* (Eds., N. Balakrishnan and C. R. Rao), Chapter 33, pp. 813–830, Elsevier Science Publishers, Amsterdam.

2002

65. On selection from normal populations in terms of the absolute values of their means (with K. Hussein), In *Advances on Theoretical and Methodological Aspects of Probability and Statistics* (Ed. N. Balakrishnan), Chapter 25, pp. 371–390, Taylor and Francis Publishers, New York.
66. Selecting the normal population with the largest mean: a restricted subset selection rule (with L. Hsu), In *Statistical Methods and Practice: Recent Advances* (Eds., N. Balakrishnan, N. Kannan and M.R. Srinivasan), pp. 145–161, Narosa Publishing House, New Delhi, India.

67. Estimation of the mean and standard deviation of the normal distribution based on multiply type-II censored samples (with N. Balakrishnan and S. S. Gupta), *Journal of Statistical Studies, Special Volume in honor of Mir Masoom Ali* (Ed., M. F. Hossain), pp. 307–320.
68. Professor Shanti Swarup Gupta (with T. J. Santner), *American Journal of Mathematical and Management Sciences*, **22**, 173–198.

2003

69. Sequential procedures for selecting the most probable multinomial cell when a nuisance cell is present (with M. Aoshima and P. Chen), *Communications in Statistics—Theory and Methods*, **32**, 893–906.

2004

70. Detecting signals simultaneously at k sites (with P. Chen), *Communications in Statistics—Theory and Methods*, **33**, 1667–1688.
71. Selection procedures for type I extreme value populations in terms of location parameters and a related homogeneity test (with S. Jeyaratnam), In *Extreme Value Distributions: Theory, Methods and Applications* (Ed., N. Balakrishnan), Taylor and Francis Publishers, New York (to appear).
72. Gupta, Shanti Swarup, In *Encyclopedia of Statistical Sciences, Second Edition* (Eds., N. Balakrishnan, C. B. Read and B. Vidakovic), John Wiley & Sons, New York (to appear).
73. Signal Processing, Selection approaches in (with P. Chen), In *Encyclopedia of Statistical Sciences, Second Edition* (Eds., N. Balakrishnan, C. B. Read and B. Vidakovic), John Wiley & Sons, New York (to appear).
74. Ranking and Selection procedures, In *Encyclopedia of Statistical Sciences, Second Edition* (Eds., N. Balakrishnan, C. B. Read and B. Vidakovic), John Wiley & Sons, New York (to appear).
75. On some variable selection procedures based on data for regression models (with D.-Y. Huang and R.-F. Lee), *Journal of Statistical Planning and Inference* (to appear).
76. A monotonicity property for gamma distributions (with G.C. McDonald), *Journal of Statistical Planning and Inference* (to appear).
77. A nonparametric procedure based on early failures for selecting the best population using a test for equality (with H. K.T. Ng and N. Balakrishnan), *Journal of Statistical Planning and Inference* (to appear).

78. A restricted subset selection procedure for selecting in terms of means at least one of the t best from k normal populations with common known variance (with L. Hsu), *In this volume*.
79. Restricted subset selection procedures for normal means: A brief review with a fresh look at the classical formulation of Bechhofer and Gupta, *Communications in Statistics—Theory and Methods* (to appear).
80. A restricted subset selection procedure for selecting in terms of means at least one of the t best from k normal populations with common known variance, II (with L. Hsu), *Under preparation*.

Book Reviews

1. *Selecting and Ordering Populations: A New Statistical Methodology*, by J. D. Gibbons, I. Olkin and M. Sobel (John Wiley & Sons), *Journal of Quality Technology*, **12** (1980), 239–240.
2. *The Complete Categorized Guide to Statistical Selection and Ranking Procedures*, by E. J. Dudewicz and J. O. Koo (American Sciences Press), *Mathematical Reviews*, **84g** (1984).
3. *Selected Tables in Mathematical Statistics, Volume 11*, Eds., R. F. Odeh, J. M. Davenport and N. S. Pearson (American Mathematical Society), *Mathematical Computation*, **51** (1989), 252–253.
4. *Modern Mathematical Statistics*, by E. J. Dudewicz and S. N. Mishra (John Wiley & Sons), *Mathematical Reviews*, **89g:62002** (1989).
5. *Fundamentals of Mathematical Statistics, Vol. I: Probability for Statistics, Vol. II: Statistical Inference*, by H.T. Nguyen and C. S. Rogers (Springer-Verlag), *Mathematical Reviews*, **90i:62003a,b** (1990).
6. *A Statistical Model: Frederic Mosteller's Contributions to Statistics, Science, and Public Policy*, Eds., S. E. Fienberg, D. C. Hoaglin, W. H. Kruskal and J. M. Tanur (Springer-Verlag), *Mathematical Reviews*, **92a:01079** (1992).
7. *A First Course in Order Statistics*, by B. C. Arnold, N. Balakrishnan and H. N. Nagaraja (John Wiley & Sons), *Mathematical Reviews*, **94a:62076** (1994).
8. *Multistage Selection and Ranking Procedures*, by N. Mukhopadhyay and T. K. S. Solanky (Marcel Dekker), *Mathematical Reviews*, **95h:62032** (1995).

9. *Measurement, Regression, and Calibration*, by P.J. Brown (Oxford University Press). *SIAM Review*, **37** (1995), 635–636.
10. *Design and Analysis of Experiments for Statistical Selection, Screening, and Multiple Comparisons*, by R. E. Bechhofer, T. J. Santner and D. M. Goldsman (John Wiley & Sons), *Mathematical Reviews*, **96k:62001** (1996).
11. *Theory of Statistics*, by M. J. Schervish (Springer-Verlag), *Mathematical Reviews*, **96m:62001** (1996).
12. *Tables for the Use of Order Statistics in Estimation*, by H. L. Harter and N. Balakrishnan (CRC Press), *Mathematical Reviews*, **97d:62097** (1997).
13. *Robust Diagnostic Regression Analysis*, by A. Atkinson and M. Riani (Springer-Verlag), *Mathematical Reviews*, **2003a:62001** (2003).

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