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*Minimize:  $C(\rho) = F^T U(\rho)$   
subject to:  $K(\rho)U(\rho) = F$*

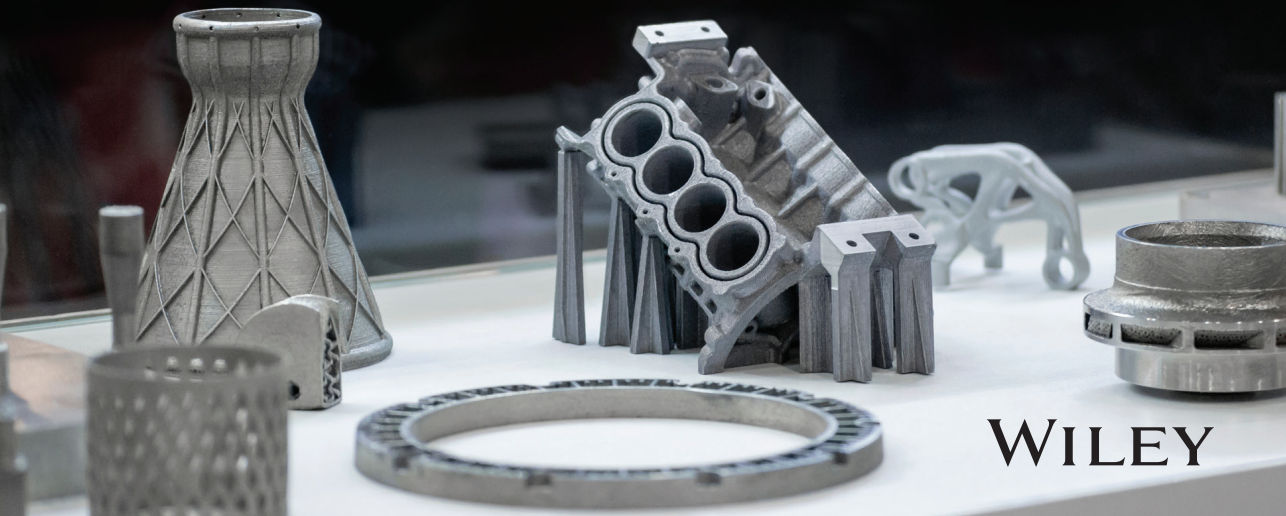
$$\frac{\partial C}{\partial \rho} = -\frac{\partial}{\partial \rho}$$

$$\frac{V(\rho)}{f_v V_0} \leq 1 \quad 0 \leq \rho \leq 1$$

$$y, z) = \frac{6\beta \cdot P}{\pi H(r_e^2 + r_e r_l + r_l^2)} \cdot e^{-2\frac{x^2 + y^2}{r_0^2}}$$

$$T - T_0 = \frac{\beta P}{2\pi R K} e^{-v(x+R)/(2\alpha)}$$

# METAL ADDITIVE MANUFACTURING



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**Ehsan Toyserkani, Dyuti Sarker, Osezua Obehi Ibhádode,  
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This edition first published 2022  
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*Library of Congress Cataloging-in-Publication Data*

Names: Toyserkani, Ehsan, author. | Sarker, Dyuti, 1983- author. | Ibhadoe, Osezua Obehi, 1989- author. | Liravi, Farzad, 1990- author. | Russo, Paola, 1986- author. | Taherkhani, Katayoon, 1989- author. | John Wiley & Sons, publisher.

Title: Metal additive manufacturing / Ehsan Toyserkani, Dyuti Sarker, Osezua Obehi Ibhadoe, Farzad Liravi, Paola Russo, Katayoon Taherkhani.

Description: Hoboken, NJ : Wiley, 2021.

Identifiers: LCCN 2021028894 (print) | LCCN 2021028895 (ebook) | ISBN 9781119210788 (cloth) | ISBN 9781119210849 (adobe pdf) | ISBN 9781119210832 (epub)

Subjects: LCSH: Additive manufacturing. | Metal powder products--Design and construction. | Powder metallurgy.

Classification: LCC TS183.25 .T69 2021 (print) | LCC TS183.25 (ebook) | DDC 621.9/88--dc23

LC record available at <https://lccn.loc.gov/2021028894>

LC ebook record available at <https://lccn.loc.gov/2021028895>

Cover Design: Wiley

Cover Image: Courtesy of Ehsan Toyserkani (top); © MarinaGrigorivna/Shutterstock

Set in 10/12pt Times LT Std by Straive, Pondicherry, India

10 9 8 7 6 5 4 3 2 1

*In memory of*

*Professor Pearl Sullivan (1961–2020)*

*Former Dean of Faculty of Engineering, University of Waterloo, Canada*

*A true leader, an exemplary advocate for engineering education, and a great friend*





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# Preface

Additive manufacturing (AM) promises to change the entire manufacturing enterprise over the next two decades. No longer limited to prototyping and low-volume manufacturing, AM is being adopted for *economies of scale* without compromising *economies of scope*. The need for the digitization of manufacturing, on-demand personalized manufacturing, distributed production, and rapid production in the event of crises have all elevated the position of AM in the medical and engineering sectors. AM is now a major research target for industrialized countries as they seek to regain leadership in advanced manufacturing through innovation. The global economy is on the verge of the next industrial revolution and sector after sector is pulling away from traditional, conventional production methods to engage in and utilize AM. However, this promise does come with many challenges, particularly for metal AM. Research and development activities are progressing at full steam to address multiple technical challenges, such as speed and productivity, quality assurance, standards, and end-to-end workflow.

A major skill sets gap currently hinders efforts to tackle these challenges. For companies seeking to embrace AM, this gap translates into a limited availability of expertise to draw an entry strategy to the AM industry. The wider adoption of AM will require overcoming the limited foundational understanding of AM that currently exists within the workforce. A thorough understanding of AM capabilities is necessary for technical experts to accurately communicate the pros and cons of AM to decision-makers, while preventing misconceptions and misinformation about AM capabilities. Currently, the knowledge gap is significantly impacting progress in the sector, as companies have difficulties in recruiting AM experts to help them develop effective designs for AM as well as meaningful business cases for metal AM.

This book is designed to help academia and industry move toward filling this gap. Enhancing AM skills will require the development of foundational knowledge of AM starting at the undergraduate level. To our knowledge, there is currently no textbook available that links the basics of fundamental undergraduate Engineering courses with metal AM processes. There is a clear need to customize undergraduate concepts in technical courses related to design, heat transfer, fluid mechanics, solid mechanics, and control, with respect to AM applications. Additionally, business- and management-oriented courses should include AM to facilitate the consideration

of AM in conjunction with life cycle assessment and business model developments among students.

The development of this book was motivated by our desire to provide foundational material for a core undergraduate course in Mechanical and Manufacturing Engineering, and we envision its use in graduate courses as well. Universities globally are revising their curriculum to incorporate AM-related courses. This textbook may provide an introductory platform to be adopted in such courses to promote an appreciation for and grasp of AM among both undergraduate and graduate students. This book may also fill a gap for engineers working outside academia who want to appreciate AM processes by identifying links between traditional core physics and engineering concepts courses and AM. The book provides a step-by-step understanding of metal AM and a solid foundation of the topic for readers, who will subsequently be well equipped to explore AM research in greater depth.

For a broad range of readers, this book sheds light on various key metal AM technologies, focusing on basic physics and modeling. This textbook is not a literature survey, nor is it intended for readers with no engineering background. In contrast, it is an introduction to basic physical concepts and phenomena of metal AM processes and their applications. Relevant foundational concepts, such as energy deposition, powder bed fusion, and binder jetting processes, are explained in-depth and illustrated by case studies throughout the book. Additionally, two emerging processes for metal AM: material extrusion and material jetting, are described. Basic design for AM (DfAM) and quality assurance principles are also covered.

We would like to express our sincere gratitude to several people who helped in the preparation of this book. Special thanks to Francis Dibia, Ali Keshavarzkermani, Zhidong Zhang, Yuze Huang, Mazyar Ansari, Andrew Barlow, Misha Karpinska, Donovan Kwong, and Eniife Elebute, who helped us with some materials and produced some of the figures, as attributed in the book. In addition, we acknowledge all organizations, publishers, authors, and companies that permitted use of their figures, plots, and texts; they have been cited accordingly throughout the book. Last but not least, thanks to our families, who make it all worthwhile.

Like any first edition, this textbook may contain errors and typos. We openly welcome the reader's suggestions to be considered in the second edition of this textbook in which multiple problem sets for each chapter will be introduced.

January 2021      Ehsan Toyserkani, Dyuti Sarker, Osezua Obehi Ibhado, Farzad Liravi,  
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# Abbreviations

<b>2D</b>	Two-Dimensional
<b>3D</b>	Three-Dimensional
<b>3DQCN</b>	Three-Dimensional Quasi-Continuous Network
<b>AI</b>	Artificial Intelligence
<b>AE</b>	Auto-Encoder
<b>Al</b>	Aluminum
<b>AL</b>	Absolute Limits
<b>ALE</b>	Arbitrary Lagrangian–Eulerian
<b>AM</b>	Additive Manufacturing
<b>AMCs</b>	Aluminum Matrix Composites
<b>AMF</b>	Additive Manufacturing File Format
<b>AMGTA</b>	Additive Manufacturer Green Trade Association
<b>ANFIS</b>	Adaptive Neuro-Fuzzy Inference System
<b>ANN</b>	Artificial Neural Network
<b>ANOVA</b>	Analysis of Variance
<b>ANSI</b>	American National Standards Institute
<b>APG</b>	Absorptivity Profile Group
<b>ASCI</b>	American Standard Code For Information Interchange
<b>ASTM</b>	American Society for Testing and Materials
<b>BD</b>	Big Data
<b>BESO</b>	Bidirectional Evolutionary Structural Optimization
<b>BJ</b>	Binder Jetting
<b>BJP</b>	Binder Jet Printing
<b>BP</b>	Backpropagation
<b>BSE</b>	Backscattered Electrons
<b>CAD</b>	Computer-Aided Design
<b>CAE</b>	Computer-Aided Engineering
<b>CAGR</b>	Compound Annual Growth Rate
<b>CAM</b>	Computer-Aided Manufacturing

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<b>CCD</b>	Charged-coupled device
<b>CCT</b>	Continuous Cooling Transformation
<b>CDA</b>	Constant Drawing Area
<b>CET</b>	Columnar-to-Equiaxed Transition
<b>CFD</b>	Computational Fluid Dynamics
<b>CL</b>	Cathodoluminescence
<b>CMOS</b>	Complementary Metal-Oxide Semiconductor
<b>CNC</b>	Computer Numerical Control
<b>CNN</b>	Convolutional Neural Network
<b>COLIN</b>	Convex Linearization
<b>CS</b>	Crack Susceptibility
<b>CT</b>	Computed Tomography
<b>μCT</b>	micro Computed Tomography
<b>CVD</b>	Chemical Vapor Deposition
<b>CW</b>	Continuous Wave
<b>DAE</b>	Differential-Algebraic Equation
<b>DBN</b>	Deep Belief Network
<b>DC</b>	Direct Current
<b>DDA</b>	Decreasing Drawing Area
<b>DED</b>	Directed Energy Deposition
<b>DEM</b>	Discrete/Dynamic Element Model
<b>DfAM</b>	Design for AM
<b>DfM</b>	Design for Manufacturing
<b>DHA</b>	Dust Hazard Analysis
<b>DL</b>	Deep Learning
<b>DMLS</b>	Direct Metal Laser Sintering
<b>DoD</b>	Drop-on-Demand
<b>DoG</b>	Difference of Gaussian
<b>DXF</b>	Drawing Exchange Format
<b>EA</b>	Electrical Arc
<b>EAM</b>	Embedded-Atom Method
<b>EB</b>	Electron Beam
<b>EBAM</b>	Electron Beam Additive Manufacturing
<b>EB-DED</b>	Electron Beam Directed Energy Deposition
<b>EBF3</b>	Electron Beam Freeform Fabrication
<b>EBF<sup>3</sup></b>	Electron Beam Fusion
<b>EBM</b>	Electron Beam Melting
<b>EB-PBF</b>	Electron Beam Powder Bed Fusion
<b>EDM</b>	Electrical Discharge Machining
<b>EIGA</b>	Electrode Induction Melting Inert Gas Atomization
<b>EKF</b>	Extended Kalman Filter
<b>ELT</b>	Effective Layer Thickness
<b>EMFs</b>	Electric and Magnetic Fields
<b>ESO</b>	Evolutionary Structural Optimization
<b>FBG</b>	Fiber Bragg Gratings
<b>FCC</b>	Face Centered Cubic
<b>FCM</b>	Finite Cell Method
<b>FDM</b>	Fused Deposition Modeling
<b>FE</b>	Finite Element
<b>FEA</b>	Finite Element Analysis

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<b>FEG</b>	Field-Emission Gun
<b>FEM</b>	Finite Element Method
<b>FFT</b>	Fast Fourier Transformation
<b>FGM</b>	Functionally Graded Material
<b>FGSs</b>	Functionally Graded Structures
<b>FIS</b>	Fuzzy Inference System
<b>FMC</b>	Ford Motor Company
<b>FN</b>	False Negative
<b>FP</b>	False Positive
<b>FS</b>	Free Surface
<b>GD</b>	Gradient Descent
<b>GM</b>	General Motors
<b>GMG</b>	Geometrically Modified Group
<b>GP</b>	Gaussian Process
<b>HA</b>	Hydroxyapatite
<b>HAZ</b>	Heat-Affected Zone
<b>HDR</b>	Heating Depth Ratio
<b>HF</b>	Highly Filled
<b>HIP</b>	Hot Isostatic Pressing
<b>HPM</b>	Heaviside Projection Method
<b>ICI</b>	Inline Coherent Imaging
<b>IDAM</b>	Industrialization and Digitization of Additive Manufacturing
<b>IDT</b>	Interdigitated Transducers
<b>IN</b>	Inconel
<b>IoT</b>	Internet of Things
<b>ISO</b>	International Standards Organization
<b>ISO</b>	International Standards Organization
<b>KF</b>	Kafman Filter
<b>KNN</b>	K-nearest neighbors
<b>LaB<sub>6</sub></b>	Lanthanum Hexaboride
<b>LBM</b>	Lattice–Boltzmann Method
<b>LCA</b>	Life Cycle Assessment
<b>LCF</b>	Low Cycle Fatigue
<b>LDED</b>	Laser Directed Energy Deposition
<b>LENS</b>	Laser Engineered Net Shaping
<b>LGA</b>	Lattice Gas Automata
<b>LM</b>	Levenberg–Marquardt
<b>LN</b>	Large Negative
<b>LoF</b>	Lack of Fusion
<b>LP</b>	Large Positive
<b>LPBF</b>	Laser Powder Bed Fusion
<b>LPM</b>	Laser Power Monitoring
<b>LSF</b>	Level Set Functions
<b>LSM</b>	Level Set Method
<b>LWIR</b>	Long Wave Infrared
<b>MAPE</b>	Mean Absolute Prediction Error
<b>MC</b>	Metal Carbide
<b>MD</b>	Molecular Dynamics
<b>ME</b>	Material Extrusion
<b>MG</b>	Metallic Glass

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<b>MJ</b>	Material Jetting
<b>MMA</b>	Method of Moving Asymptotes
<b>MMCs</b>	Metal Matrix Composites
<b>MME</b>	Metal Material Extrusion
<b>MMP</b>	Micro-Machining Process
<b>MMV</b>	Moving Morphable Voids
<b>MOV</b>	Main Oxidizer Valve
<b>MPC</b>	Metal–Polymer Composite
<b>MPE</b>	Maximum Permissible Exposure
<b>MPM</b>	Melt Pool Monitoring
<b>MS</b>	Multi-Speed
<b>MSDS</b>	Material Safety Data Sheet
<b>MSE</b>	Mean Squared Error
<b>MTPS</b>	Multifunctional Thermal Protection System
<b>Nd</b>	Neodymium
<b>NDT</b>	Non-Destructive Testing
<b>NFPA</b>	National Fire Protection Association
<b>nHA</b>	Nano-Hydroxyapatite
<b>NHZ</b>	Nominal Hazard Zone
<b>Ni</b>	Nickle
<b>NIR</b>	Near-Infrared
<b>NIST</b>	National Institute of Standards and Technology
<b>NN</b>	Neural Network
<b>NS</b>	Navier–Stokes
<b>OCM</b>	Optimality Criterial Method
<b>OCT</b>	Optical Coherence Tomography
<b>OEM</b>	Original Equipment Manufacturers
<b>OPD</b>	Optical Penetration Depth
<b>OTLs</b>	Orthogonal Translational Lattices
<b>PBF</b>	Powder Bed Fusion
<b>PCA</b>	Principal Component Analysis
<b>PDF</b>	Point Distribution Function
<b>PF</b>	Powder-Fed
<b>PI</b>	Proportional–Integral
<b>PID</b>	Proportional–Integral–Derivative
<b>PMC</b>	Polymer Matrix Composite
<b>PMZ</b>	Partially Melted Zone
<b>PPE</b>	Personal Protective Equipment
<b>PPHT</b>	Post-Processing Heat Treatment
<b>PREP</b>	Plasma Rotate Electrode Process
<b>PSD</b>	Particle Size Distribution
<b>PTA-DED</b>	Plasma Transferred Arc Directed Energy Deposition
<b>PVD</b>	Physical Vapor Deposition
<b>PW</b>	Pulsed Wave
<b>PZT</b>	Piezoelectric
<b>R&amp;D</b>	Research and development
<b>RAMP</b>	Rational Approximation of Material Properties
<b>RDM</b>	Relative Density Mapping
<b>REP</b>	Rotating Electrode Process
<b>RF</b>	Radio Frequency

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<b>RGB</b>	Red-Green-Blue
<b>RLS</b>	Recursive Least Square
<b>RMSE</b>	Root Mean Square Error
<b>RNN</b>	Recurrent Neural Networks
<b>ROS</b>	Reactive Oxygen Species
<b>RTE</b>	Radiation Transfer Equation
<b>SAW</b>	Surface Acoustic Wave
<b>SD</b>	Signal Dynamics
<b>SDAS</b>	Secondary Dendritic Arm Spacing
<b>SE</b>	Secondary Electrons
<b>SIMP</b>	Solid Isotropic Material with Penalization
<b>SINH</b>	Sine Hyperbolic Function
<b>SL</b>	Sheet Lamination
<b>SLD</b>	Super-Luminescent Diode
<b>SLD-OCT</b>	Super-Luminescent Diode—Optical Coherence Tomography
<b>SLM</b>	Selective Laser Melting
<b>SLP</b>	Sequential Linear Programming
<b>SLR</b>	Single-Lens Reflex
<b>SLS</b>	Selective Laser Sintering
<b>SN</b>	Small Negative
<b>SOM</b>	Self-Organizing Map
<b>SP</b>	Small Positive
<b>SQP</b>	Sequential Quadratic Programming
<b>SRAS</b>	Spatially Resolved Acoustic Spectroscopy
<b>STF</b>	Short-Term Fluctuations
<b>STL</b>	Standard Tessellation Language or StereoLithography
<b>STP</b>	Standard for the Product Data
<b>ST-PCA</b>	Spatially Weighted Principal Component Analysis
<b>SVD</b>	Singular Value Decomposition
<b>SVM</b>	Support Vector Machine
<b>TCP</b>	Topological Close-Packed
<b>TEM</b>	Transverse Electromagnetic Modes
<b>TGM</b>	Temperature Gradient Mechanism
<b>Ti</b>	Titanium
<b>TiC</b>	Titanium Carbide
<b>Ti-HA</b>	Titanium-Hydroxyapatite
<b>TMCs</b>	Titanium-Matrix Composites
<b>TN</b>	True Negative
<b>TP</b>	True Positive
<b>TPMS</b>	Triply Periodic Minimal Surface
<b>TRL</b>	Technology Readiness Level
<b>TTT</b>	Transformation Time Temperature
<b>VC</b>	Vanadium Carbides
<b>VED</b>	Volumetric Energy Density
<b>VoF</b>	Volume-of-Fluid
<b>VTM</b>	Virtual Temperature Method
<b>WF</b>	Wire-Fed
<b>WF-EDED</b>	Wire-Fed Electron Beam Directed Energy Deposition
<b>XRD</b>	X-Ray Diffraction
<b>XRF</b>	X-Ray Fluorescence

<b>YAG</b>	Yttrium Aluminum Garnet
<b>YLF</b>	Yttrium Lithium Fluoride
<b>YVO4</b>	Yttrium Orthovanadate

## Nomenclature

Unless otherwise stated in the text, these symbols have the following meanings

$a$	Characteristic length
$a$	Energy bilinear function for internal energy (Chapter 10)
$A$	Spot area – heat source interaction area
$A$	Filament or nozzle cross-section area (Chapter 7)
$A_{at}$	Attenuated area
$A_c$	Cross-section area
$A_{jet}^{liq}$	Intersection of melt pool area on substrate and powder stream
$A_{jet}$	Cross-section of powder stream on substrate
$A_G$	Property of filament material
$A_{ij}, B_{ij}$	Einstein coefficients
$A_S$	Surface area
$b$	Melt pool depth
$b$	Bias (Chapter 11)
$B$	Size of gap (Chapter 7)
$B$	Magnetic field
$\mathbf{B}$	Differential shape function matrix (Chapter 10)
$c$	Speed of light
$c_p$	Heat capacity
$cyl$	Function based on Bessel functions
$c_s$	Speed of sound in the fluid
$C$	Duty cycle
$C$	Compliance (Chapter 10)
$Ca$	Capillary number
$C_s$	Solid composition
$C_L$	Liquid composition
$C_0$	Nominal alloy composition or solute concentration
$d$	Spot size
$d$	Euclidean distance (Chapter 11)
$d_0$	Droplet diameter
$d_{3,2}$	Surface mean particle diameter
$d_{con}$	Semispherical droplet
$D$	Laser beam diameter
$\mathbf{D}$	Material matrix
$D_f$	Diffusion constant
$D_{ijmn}$	Tensor of elastic coefficients
$D_L$	Solute diffusion coefficient



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$D_\emptyset$	Diffusion coefficient
$e$	When subscript or superscript, signifies a variable in its elemental form
$e_i$	Vector pointing
$E$	Laser beam energy
$E$	Electric field (Chapter 5)
$\mathbf{E}$	Young's modulus matrix (Chapter 10)
$E_a$	Energy of activation
$E_b$	E-beam energy
$E_i$	Input laser energy
$E_{kin}$	Kinetic energy
$E_r$	Reflected energy
$E_t$	Transmitted energy
$E_i$	Energy levels (Chapter 3)
$E_{specific}$	The energy enters the substrate from the surface in DED
$f$	Frequency
$f$	Volume fraction (Chapter 10)
$f_s$	Fraction of solid
$f_L$	Fraction of liquid
$f(R)$	Function of surface roughness
$f_i(x, t)$	Density of particles moving in the $e_i$ direction
$f_i^{eq}(x, t)$	Equilibrium distribution
$F$	Force
$F_0$	Fourier number
$\mathcal{F}_0$	Zero-order Bessel function of its first kind
$\mathcal{F}_1$	The first-order Bessel function of the first kind
$F^{Cap}$	Capillary force
$F_{st}$	Surface tension force
$F_{th}$	Thermal stress load
$F^{Wet}$	Wetting force
$g$	Gravity
$g_i$	Effect of external forces
$G$	Temperature gradient
$G_S$	Gibbs free energy for solid
$G_L$	Gibbs free energy for liquid
$G_z$	Graetz number
$\Delta G$	Total Gibbs free energy change
$\Delta G^*$	Critical free energy change
$\Delta G_V$	Free energy change per unit volume
$h$	Plank's constant (Chapter 3)
$h$	Height of a hexahedral element (Chapter 10)
$h_c$	Heat convection coefficient
$h_i$	Convective heat loss (cooling) coefficients
$h_a$	Average heat transfer coefficient of convection
$h_w$	Distance between the nozzle and surface
$h_r$	Radiative heat transfer coefficient

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$h_{min}$	Minimum radius of the liquid column
$H$	Barrel length or height of track
$H^*$	Height of the melt polymer
$\Delta H$	Enthalpy difference
$HDR$	Heating depth ratio
$I$	Intensity: energy per area
$I$	Current in electron beam (Chapter 5)
$I(x)$	Indicator function (Chapter 11)
$I_0$	Intensity scale factor or initial intensity
$I_b$	Beam current in the electron-beam process
$J$	Free electron current
$k$	Propagation factor
$k$	Equilibrium distribution coefficient (Chapter 8)
$k$	Solute partition coefficient (Chapter 9)
$K$	Thermal conductivity
$\mathbf{K}$	Global stiffness matrix (Chapter 10)
$\mathbf{K}_c$	Conductivity matrix (Chapter 10)
$\mathbf{K}_h$	Connective matrix (Chapter 10)
$K^*$	Modified thermal conductivity
$K_0$	Bessel function of the second kind and zero order
$l$	Layer thickness
$l$	Load linear function for external work (Chapter 10)
$\mathbf{L}$	Transformation matrix
$L$	Link intensity
$L_c$	Characteristic length based on domain size
$L_f$	Latent heat of fusion
$L_l^p$	Laguerre polynomial of order p and index l
$m$	Atomic mass
$m_b$	Mass of the ball (Chapter 9)
$m_b$	Deposited binder (Chapter 6)
$m_p$	Particle mass
$m_p$	Mass of the bound powder (Chapter 6)
$m_f$	Fluid mass
$\dot{m}$	Mass flow rate
$M^2$	Beam quality factor
$Ma$	Marangoni number
$n$	Reflection's index
$N$	Matrix of shape function for mesh element
$N_i$	Number of atoms or electrons per unit volume in the energy levels
$N_L$	Amount of atoms per unit volume of liquid
$N_{lx}$	Neumann function
$N_S$	Amount of atoms per unit volume of solid
$Nu$	Nusselt number
$N_{th}$	Shape vector for thermal expansion
$Oh$	Ohnesorge number

$p$	Constant characteristic of the material (Chapter 4)
$p$	Pressure
$p$	Penalty value (Chapter 10)
$p_c$	Capillary force
$P_f$	Packing fraction
$P$	Power
$P_{at}$	Attenuated laser power by particles
$P_{el}$	Power of electrical motor in FDM system
$P_l$	Net/average laser power
$P_{peak}$	Peak power per pulse
$P_{on}$	On the state of the laser power
$P_{off}$	Off state of the laser power
$P_{tot}$	Total delivered beam power
$P_e$	Peclet number
$Pr$	Prandtl number
$PR$	Packing density of the powder
$PW$	Pulsed wave laser
$P(\infty)$	Value of the extrudate property after an infinite healing time
$q$	Heat flux
$Q$	Power generated per unit volume (in all chapters except Chapter 3)
$Q$	Beam propagation factor (Chapter 3)
$Q_c$	Total energy absorbed by the substrate
$Q_{ext}$	Extinct coefficient
$Q_l$	Laser energy
$Q_{rs}$	Reflected energy from the substrate
$Q_L$	Latent energy of fusion
$Q_v$	Volumetric flow rate
$r$	Radius of nucleus (Chapter 8)
$r^*$	Critical nucleus radius
$r_b$	Ball mill radius
$r_f$	Filament radius
$r_{ol}$	Beam radius of the waist
$r_{jet}$	Radius of powder spray jet
$r_l$	Beam spot radius on the substrate
$r_s$	Powder stream diameter
$r_p$	Powder particle radius
$R$	Reflectivity
$R$	Solidification rate where it is referred to
$R_c$	Clad surface curvature
$R_{cur}$	Radius of curvature
$Re$	Reynolds number
$Re^*$	Property-based Reynolds number
$R_h$	Heat load by convection
$R_h(t)$	Intrinsic healing function
$R_L$	Local growth rate

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$R_N$	Nominal growth rate
$R_r$	Radius of the actuating motor
$R_{pore}$	Effective pore diameter in the bed
$R_q$	Heat load by surface conduction
$R_Q$	Heat load by volume conduction
$s$	Hatch spacing
$s_0$	Specific surface area
$S$	Binder saturation
$S_{ij}$	Lateral distance between neuron $i$ and $j$ (Chapter 11)
$S_{max}$	Spreading ratio
$S_{meas}$	Amount of signal (Chapter 11)
$S_{\emptyset}$	Source term corresponding to $\emptyset$
$S(\phi)$	Shape factor
$SS$	Scan speed
$S$	Strain rate deformation tensor
$\Delta S$	Expansion of surface area
$t$	Time and/or laser interaction time
$t^*$	Dimensionless time
$t_c = t_\mu$	Viscous time
$t_{CDA}$	Corresponding penetration time
$t_f$	Solidification time
$t_I$	Inertial-capillary time
$t_V$	Viscous-capillary time
$T$	Temperature
$T_\alpha$	Reference temperature
$T_{ave}$	Average temperature
$T_{in}$	Filament temperature
$T_g$	Glass transition temperature
$T_{out}$	Outlet temperature
$T_{\dot{m}}$	Temperature of the liquefier wall
$T_d$	Drying time
$T_e$	Equilibrium temperature
$T_l$	Liquidus temperature
$T_0$	Ambient temperature
$T_m$	Materials melting point
$T_p$	Maximum temperature
$\Delta T$	Undercooling temperature
$\Delta T_{tot}$	Total undercooling temperature
$\Delta T_C$	Undercooling temperature: solute diffusion
$\Delta T_T$	Undercooling temperature: thermal diffusion
$\Delta T_K$	Undercooling temperature: attachment kinetics
$\Delta T_R$	Undercooling temperature: solid–liquid boundary curvature
$TEM_{pl}$	Gaussian–Laguerre transverse electromagnetic modes
$U$	Beam velocity
$\mathbf{U}$	Travel velocity vector

$U$	Global displacement vector (Chapter 10)
$U_p$	Particle velocity vector
$U_s$	Rate of solidification
$v$	Scanning speed
$v_c$	Collision velocity
$v_j$	Jet velocity
$v_p$	Velocity of the particle
$v_{print}$	Velocity of the print head
$V$	Volume of melt pool
$V$	Design volume (Chapter 10)
$V_a$	Acceleration voltage
$V_S$	Volume of nucleus
$VED$	The energy enters the substrate from the surface in LPBF
$w$	Track or melt pool width
$w$	Neuron weight (Chapter 11)
$w_i$	Weight factor
$W$	Laser pulse width
$We$	Weber number
$X_{s+c}$	Weight percent of element $X$ in the total surface of the clad region
$X_c$	Weight percent of element $X$ in the powder alloy
$X_s$	Weight percent of element $X$ in the substrate
$y$	Dendrite arm spacing (Chapter 8)
$z$	Distance from the surface
$z_0$	Waist location with respect to an arbitrary coordinate along the propagation axis
$Z$	Printability of a liquid
$Z_h$	Heat penetration depth

## Greek Symbols

$\alpha$	Thermal diffusivity
$\alpha_t$	Coefficient of thermal expansion
$\beta$	Absorption factor
$\beta$	Absorption factor
$\beta_p$	Powder particles' absorbed coefficient
$\beta_w$	Substrate laser power absorptivity
$\gamma$	Surface tension
$\gamma$	Net electron beam energy (Chapter 5)
$\gamma_E$	Specific surface energy
$\gamma_{SL}$	Solid–liquid interfacial free energy
$\gamma_{SV}$	Solid–vapor interfacial energy
$\gamma_{LV}$	Liquid–vapor interfacial energy
$\dot{\gamma}$	Shear rate
$\Gamma$	Torque of electrical motors in FDM
$\Gamma$	Surface function (Chapter 10)
$\delta$	Solid/liquid interface thickness
$\delta$	Dirac delta function (Chapter 6)

$\epsilon$	Total strain
$\epsilon_c$	Cooling rate
$\epsilon_t$	Emissivity
$\epsilon^M$	Mechanical strains
$\epsilon^T$	Thermal strains
$\epsilon_p$	Equivalent plastic stress
$\epsilon_0$	Vacuum permittivity
$\epsilon_m$	Mechanical strain
$\epsilon_{th}$	Thermal strain
$\Sigma$	Covariance matrix
$\eta$	Dynamic viscosity
$\eta$	Powder catchment efficiency (wherever it refers to throughout chapters)
$\eta$	Numerical damping coefficient for OCM (Chapter 10)
$\eta$	Learning rate (Chapter 11)
$\eta_e$	Absorption efficiency for electron beam
$\eta_d$	Dynamic viscosity
$\eta_p$	Powder catchment efficiency
$\theta$	Representing different angles based on figures
$\theta$	Wetting angle (Chapter 2)
$\theta$	Far-field divergence angle (Chapter 3)
$\theta$	Dimensionless temperature in numerical models (Chapter 7)
$\theta_{jet}$	Angle between powder jet and substrate
$\theta_d$	Dynamic wetting angle
$\theta_{eq}$	Steady-state angle
$\Theta$	Dimensionless temp in analytical models
$\lambda$	Wavelength
$\lambda$	Lagrange multiplier (Chapter 10)
$\lambda_n$	Roots of zero-order Bessel function of its first kind
$\mu$	Viscosity
$\mu$	Membership function (Chapter 11)
$\nu$	Frequency (Chapter 3)
$\nu$	Kinematic viscosity
$\rho$	Density
$\rho_b$	Density of binder
$\rho_{pb}$	Powder bed density
$\rho_c$	Density of melted powder alloy
$\rho_s$	Density of substrate material
$\rho_s$	Packing density of the pores (Chapter 6)
$\sigma$	Stefan–Boltzmann constant
$\sigma$	Covariance (Chapter 11)
$\sigma_c$	Charge density
$\sigma_{ij}$	Elastic stress
$\tau$	Thermal time constant
$\tau_c$	Dimensionless capillary time
$\phi$	Different label for angles as indicated in the associated figures