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Jian Pei · Liang Zhao *Eds.*

Graph Neural Networks

Foundations,
Frontiers,
and Applications

 Springer

Graph Neural Networks: Foundations, Frontiers, and Applications

Lingfei Wu • Peng Cui • Jian Pei • Liang Zhao
Editors

Graph Neural Networks: Foundations, Frontiers, and Applications

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Foreword

“The first comprehensive book covering the full spectrum of a young, fast-growing research field, graph neural networks (GNNs), written by authoritative authors!”

Jiawei Han (Michael Aiken Chair Professor at University of Illinois at Urbana-Champaign, ACM Fellow and IEEE Fellow)

“This book presents a comprehensive and timely survey on graph representation learning. Edited and contributed by the best group of experts in this area, this book is a must-read for students, researchers and practitioners who want to learn anything about Graph Neural Networks.”

Heung-Yeung ”Harry” Shum (Former Executive Vice President for Technology and Research at Microsoft Research, ACM Fellow, IEEE Fellow, FREng)

“As the new frontier of deep learning, Graph Neural Networks offer great potential to combine probabilistic learning and symbolic reasoning, and bridge knowledge-driven and data-driven paradigms, nurturing the development of third-generation AI. This book provides a comprehensive and insightful introduction to GNN, ranging from foundations to frontiers, from algorithms to applications. It is a valuable resource for any scientist, engineer and student who wants to get into this exciting field.”

Bo Zhang (Member of Chinese Academy of Science, Professor at Tsinghua University)

“Graph Neural Networks are one of the hottest areas of machine learning and this book is a wonderful in-depth resource covering a broad range of topics and applications of graph representation learning.”

Jure Leskovec (Associate Professor at Stanford University, and investigator at Chan Zuckerberg Biohub).

“Graph Neural Networks are an emerging machine learning model that is already taking the scientific and industrial world by storm. The time is perfect to get in on the action – and this book is a great resource for newcomers and seasoned practitioners

alike! Its chapters are very carefully written by many of the thought leaders at the forefront of the area.”

Petar Veličković (Senior Research Scientist, DeepMind)

Preface

The field of graph neural networks (GNNs) has seen rapid and incredible strides over the recent years. Graph neural networks, also known as deep learning on graphs, graph representation learning, or geometric deep learning, have become one of the fastest-growing research topics in machine learning, especially deep learning. This wave of research at the intersection of graph theory and deep learning has also influenced other fields of science, including recommendation systems, computer vision, natural language processing, inductive logic programming, program synthesis, software mining, automated planning, cybersecurity, and intelligent transportation.

Although graph neural networks have achieved remarkable attention, it still faces many challenges when applying them into other domains, from the theoretical understanding of methods to the scalability and interpretability in a real system, and from the soundness of the methodology to the empirical performance in an application. However, as the field rapidly grows, it has been extremely challenging to gain a global perspective of the developments of GNNs. Therefore, we feel the urgency to bridge the above gap and have a comprehensive book on this fast-growing yet challenging topic, which can benefit a broad audience including advanced undergraduate and graduate students, postdoctoral researchers, lecturers, and industrial practitioners.

This book is intended to cover a broad range of topics in graph neural networks, from the foundations to the frontiers, and from the methodologies to the applications. Our book is dedicated to introducing the fundamental concepts and algorithms of GNNs, new research frontiers of GNNs, and broad and emerging applications with GNNs.

Book Website and Resources

The website and further resources of this book can be found at: <https://graph-neural-networks.github.io/>. The website provides online preprints and lecture slides of all the chapters. It also provides pointers to useful material and resources that are publicly available and relevant to graph neural networks.

To the Instructors

The book can be used for a one-semester graduate course for graduate students. Though it is mainly written for students with a background in computer science, students with a basic understanding of probability, statistics, graph theory, linear algebra, and machine learning techniques such as deep learning will find it easily accessible. Some chapters can be skipped or assigned as homework assignments for reviewing purposes if students have knowledge of a chapter. For example, if students have taken a deep learning course, they can skip Chapter 1. The instructors can also choose to combine Chapters 1, 2, and 3 together as a background introduction course at the very beginning.

When the course focuses more on the foundation and theories of graph neural networks, the instructor can choose to focus more on Chapters 4-8 while using Chapters 19-27 to showcase the applications, motivations, and limitations. Please refer to the Editors' Notes at the end of each chapter on how Chapters 4-8 and Chapters 19-27 are correlated. When the course focuses more on the research frontiers, Chapters 9-18 can be the pivot to organize the course. For example, an instructor can make it an advanced graduate course where the students are asked to search and present the most recent research papers in each different research frontier. They can also be asked to establish their course projects based on the applications described in Chapters 19-27 as well as the materials provided on our website.

To the Readers

This book was designed to cover a wide range of topics in the field of graph neural network field, including background, theoretical foundations, methodologies, research frontiers, and applications. Therefore, it can be treated as a comprehensive handbook for a wide variety of readers such as students, researchers, and professionals. You should have some knowledge of the concepts and terminology associated with statistics, machine learning, and graph theory. Some backgrounds of the basics have been provided and referenced in the first eight chapters. You should better also have knowledge of deep learning and some programming experience for easily accessing the most of chapters of this book. In particular, you should be able to read pseudocode and understand graph structures.

The book is well modularized and each chapter can be learned in a standalone manner based on the individual interests and needs. For those readers who want to have a solid understanding of various techniques and theories of graph neural networks, you can start from Chapters 4-9. For those who further want to perform in-depth research and advance related fields, please read those chapters of interest among Chapters 9-18, which provide comprehensive knowledge in the most recent research issues, open problems, and research frontiers. For those who want to apply graph neural networks to benefit specific domains, or aim at finding interesting applications to validate specific graph neural networks techniques, please refer to Chapters 19-27.

Acknowledgements

Graph machine learning has attracted many gifted researchers to make their seminal contributions over the last few years. We are very fortunate to discuss the challenges and opportunities, and often work with many of them on a rich variety of research topics in this exciting field. We are deeply indebted to these collaborators and colleagues from JD.COM, IBM Research, Tsinghua University, Simon Fraser University, Emory University, and elsewhere, who encouraged us to create such a book comprehensively covering various topics of Graph Neural Networks in order to educate the interested beginners and foster the advancement of the field for both academic researchers and industrial practitioners.

This book would not have been possible without the contributions of many people. We would like to give many thanks to the people who offered feedback on checking the consistency of the math notations of the entire book as well as reference editing of this book. They are people from Emory University: Ling Chen, Xiaojie Guo, and Shiyu Wang, as well as people from Tsinghua University: Yue He, Ziwei Zhang, and Haoxin Liu. We would like to give our special thanks to Dr. Xiaojie Guo, who generously offered her help in providing numerous valuable feedback on many chapters.

We also want to thank those who allowed us to reproduce images, figures, or data from their publications.

Finally, we would like to thank our families for their love, patience and support during this very unusual time when we are writing and editing this book.

Editor Biography



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Dr. Jian Pei is a Professor in the School of Computing Science at Simon Fraser University. He is a well-known leading researcher in the general areas of data science, big data, data mining, and database systems. His expertise is on developing effective and efficient data analysis techniques for novel data intensive applications, and transferring his research results to products and business practice. He is recognized as a Fellow of the Royal Society of Canada (Canada's national academy), the Canadian Academy of Engineering, the Association of Computing Machinery (ACM) and the Institute of Electrical and Electronics Engineers (IEEE). He is one of the most cited authors in data mining, database systems, and information retrieval. Since 2000, he has published one textbook, two monographs and over 300 research papers in refereed journals and conferences, which have been cited extensively by others. His research has generated remarkable impact substantially beyond academia. For example, his algorithms have been adopted by industry in production and popular open-source software suites. Jian Pei also demonstrated outstanding professional leadership in many academic organizations and activities. He was the editor-in-chief of the IEEE Transactions of Knowledge and Data Engineering (TKDE) in 2013-16, the chair of the Special Interest Group on Knowledge Discovery in Data (SIGKDD) of the Association for Computing Machinery (ACM) in 2017-2021, and a general co-chair or program committee co-chair of many premier conferences. He maintains a wide spectrum of industry relations with both global and local industry partners. He is an active consultant and coach for industry on enterprise data strategies, healthcare informatics, network security intelligence, computational finance, and smart retail. He received many prestigious awards, including the 2017 ACM SIGKDD Innovation Award, the 2015 ACM SIGKDD Service Award, the 2014 IEEE ICDM Research Contributions Award, the British Columbia Innovation Council 2005 Young Innovator Award, an NSERC 2008 Discovery Accelerator Supplements Award (100 awards cross the whole country), an IBM Faculty Award (2006), a KDD Best Application Paper Award (2008), an ICDE Influential Paper Award (2018), a PAKDD Best Paper Award (2014), a PAKDD Most Influential Paper Award (2009), and an IEEE Outstanding Paper Award (2007).



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Terminologies

This chapter describes a list of definitions of terminologies related to graph neural networks used throughout this book.

1 Basic concepts of Graphs

- **Graph:** A graph is composed of a node set and an edge set, where nodes represent entities and edges represent the relationship between entities. The nodes and edges form the topology structure of the graph. Besides the graph structure, nodes, edges, and/or the whole graph can be associated with rich information represented as node/edge/graph features (also known as attributes or contents).
- **Subgraph:** A subgraph is a graph whose set of nodes and set of edges are all subsets of the original graph.
- **Centrality:** A centrality is a measurement of the importance of nodes in the graph. The basic assumption of centrality is that a node is thought to be important if many other important nodes also connect to it. Common centrality measurements include the degree centrality, the eigenvector centrality, the betweenness centrality, and the closeness centrality.
- **Neighborhood:** The neighborhood of a node generally refers to other nodes that are close to it. For example, the k -order neighborhood of a node, also called the k -step neighborhood, denotes a set of other nodes in which the shortest path distance between these nodes and the central node is no larger than k .
- **Community Structure:** A community refers to a group of nodes that are densely connected internally and less densely connected externally.
- **Graph Sampling:** Graph sampling is a technique to pick a subset of nodes and/or edges from the original graph. Graph sampling can be applied to train machine learning models on large-scale graphs while preventing severe scalability issues.

- **Heterogeneous Graphs:** Graphs are called heterogeneous if the nodes and/or edges of the graph are from different types. A typical example of heteronomous graphs is knowledge graphs where the edges are composed of different types.
- **Hypergraphs:** Hypergraphs are generalizations of graphs in which an edge can join any number of nodes.
- **Random Graph:** Random graph generally aims to model the probability distributions over graphs that the observed graphs are generated from. The most basic and well-studied random graph model, known as the Erdos–Renyi model, assumes that the node set is fixed and each edge is identically and independently generated.
- **Dynamic Graph:** Dynamic graph refers to when at least one component of the graph data changes over time, e.g., adding or deleting nodes, adding or deleting edges, changing edges weights or changing node attributes, etc. If graphs are not dynamic, we refer to them as static graphs.

2 Machine Learning on Graphs

- **Spectral Graph Theory:** Spectral graph theory analyzes matrices associated with the graph such as its adjacency matrix or Laplacian matrix using tools of linear algebra such as studying the eigenvalues and eigenvectors of the matrix.
- **Graph Signal Processing:** Graph Signal Processing (GSP) aims to develop tools for processing signals defined on graphs. A graph signal refers to a finite collection of data samples with one sample at each node in the graph.
- **Node-level Tasks:** Node-level tasks refer to machine learning tasks associated with individual nodes in the graph. Typical examples of node-level tasks include node classification and node regression.
- **Edge-level Tasks:** Edge-level tasks refer to machine learning tasks associated with a pair of nodes in the graph. A typical example of an edge-level task in link prediction.
- **Graph-level Tasks:** Graph-level tasks refer to machine learning tasks associated with the whole graph. Typical examples of graph-level tasks include graph classification and graph property prediction.
- **Transductive and Inductive Learning:** Transductive learning refers to that the targeted instances such as nodes or edges are observed at the training time (though the labels of the targeted instances remain unknown) and inductive learning aims to learn the model which is generalizable to unobserved instances.

3 Graph Neural Networks

- **Network embedding:** The goal of network embedding is to represent each node in the graph as a low-dimensional vector so that useful information such as the