# Proceedings of COMPSTAT'2010

Yves Lechevallier · Gilbert Saporta Editors

# Proceedings of COMPSTAT'2010

19th International Conference on Computational Statistics Paris - France, August 22–27, 2010 Keynote, Invited and Contributed Papers



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#### **Preface**

The 19th Conference of IASC-ERS, COMPSTAT'2010, is held in Paris, France, from August 22nd to August 27th 2010, locally organised by the Conservatoire National des Arts et Métiers (CNAM) and the French National Institute for Research in Computer Science and Control (INRIA). COMPSTAT is an initiative of the European Regional Section of the International Association for Statistical Computing (IASC-ERS), a section of the International Statistical Institute (ISI). COMPSTAT conferences started in 1974 in Wien; previous editions of COMPSTAT were held in Berlin (2002), Prague (2004), Rome (2006) and Porto (2008). It is one of the most prestigious world conferences in Computational Statistics, regularly attracting hundreds of researchers and practitioners, and has gained a reputation as an ideal forum for presenting top quality theoretical and applied work, promoting interdisciplinary research and establishing contacts amongst researchers with common interests.

Keynote lectures are addressed by Luc Devroye (School of Computer Science, McGill University, Montreal), Lutz Edler (Division of Biostatistics, German Cancer Research Center, Heidelberg) and David Hand (Statistics section, Imperial College, London). The conference program includes three tutorials: "Statistical Approach for Complex data" by Lynne Billard (University of Georgia, United States), "Bayesian discrimination between embedded models" by Jean-Michel Marin (Université Montpellier II, France) and "Machine Learning and Association Rules" by Petr Berka and Jan Rauch (University of Economics, Prague, Czech Republic). Each COMPSTAT meeting is organised with a number of topics highlighted, which lead to Invited Sessions. The Conference program includes also contributed sessions and short communications (both oral communications and posters).

The Conference Scientific Program Committee chaired by Gilbert Saporta, CNAM, includes:

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Due to space limitations, the Book of Proceedings includes keynote speakers' papers, invited sessions speakers' papers and a selection of the best contributed papers, while the e-book includes all accepted papers.

The papers included in this volume present new developments in topics of major interest for statistical computing, constituting a fine collection of methodological and application-oriented papers that characterize the current research in novel, developing areas. Combining new methodological advances with a wide variety of real applications, this volume is certainly of great value for researchers and practitioners of computational statistics alike.

First of all, the organisers of the Conference and the editors would like to thank all authors, both of invited and contributed papers and tutorial texts, for their cooperation and enthusiasm. We are specially grateful to all colleagues who served as reviewers, and whose work was crucial to the scientific quality of these proceedings. A special thanks to Hervé Abdi who took in charge the session on Brain Imaging. We also thank all those who have contributed to the design and production of this Book of Proceedings, Springer Verlag, in particular Dr. Martina Bihn and Dr. Niels Peter Thomas, for their help concerning all aspects of publication.

The organisers would like to express their gratitude to all people from CNAM and INRIA who contributed to the success of COMPSTAT'2010, and worked actively for its organisation. We are very grateful to all our sponsors, for their generous support. Finally, we thank all authors and participants, without whom the conference would not have been possible.

The organisers of COMPSTAT'2010 wish the best success to Erricos Kontoghiorghes, Chairman of the 20th edition of COMPSTAT, which will be held in Cyprus in Summer 2012. See you there!

Paris, August 2010

Yves Lechevallier Gilbert Saporta

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Part I

Keynote

# Complexity Questions in Non-Uniform Random Variate Generation

Luc Devroye

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**Abstract.** In this short note, we recall the main developments in non-uniform random variate generation, and list some of the challenges ahead.

Keywords: random variate generation, Monte Carlo methods, simulation

#### 1 The pioneers

World War II was a terrible event. But it can not be denied that it pushed science forward with a force never seen before. It was responsible for the quick development of the atomic bomb and led to the cold war, during which the United States and Russia set up many research labs and attracted the best and the brightest to run them. It was at Los Alamos and RAND that physicists and other scientists were involved in large-scale simulations. John von Neumann, Stan Ulam and Nick Metropolis developed the Monte Carlo Method in 1946: they suggested that we could compute and predict in ways never before considered. For example, the Metropolis chain method developed a few years later (Metropolis, Rosenbluth, Rosenbluth, Teller and Teller, 1953) can be used to simulate almost any distribution by setting up a Markov chain that has that distribution as a limit. At least asymptotically, that is. But it was feasible, because the computers were getting to be useful, with the creation of software and the FORTRAN compiler.

To drive the Markov chains and other processes, one would need large collections of uniform random numbers. That was a bit of a sore point, because no one knew where to get them. Still today, the discussion rages as to how one should secure a good source of uniform random numbers. The scientists eventually settled on something that a computer could generate, a sequence that looked random.

The early winner was the linear congruential generator, driven by  $x_{n+1} = (ax_n + b) \mod m$ , which had several well-understood properties. Unfortunately, it is just a deterministic sequence, and many of its flaws have been exposed in the last three decades. The built-in linear-congruential generator in the early FORTRAN package for IBM computers was RANDU. Consecutive pairs

 $(x_n,x_{n+1})$  produced by RANDU fall on just a few parallel lines, prompting Marsaglia (1968) to write a paper with the ominous title "Random numbers fall mainly in the plane". But bad linear congruential or related generators have persisted until today—the generator in Wolfram's Mathematica had a similar problem: their built-in generator Random uses the Marsaglia-Zaman subtract-with-borrow generator (1991), which has the amazing property that all consecutive triples  $(x_n,x_{n+1},x_{n+2})$  fall in only two hyperplanes of  $[0,1]^3$ , a fact pointed out to me by Pierre Lecuyer. Many thousands of simulations with Mathematica are thus suspect—I was made aware of this due an inconsistency between simulation and theory brought to my attention by Jim Fill in 2010. The company has never apologized or offered a refund to its customers, but it has quietly started using other methods, including one based on a cellular automaton (the default). Hoewever, they are still offering linear congruential generators as an option. The story is far from over, and physical methods may well come back in force.

Information theorists and computer scientists have approached randomness from another angle. For them, random variables uniformly distributed on [0,1] do not and can not exist, because the binary expansions of such variables consist of infinitely many independent Bernoulli (1/2) random bits. Each random bit has binary entropy equal to one, which means that its value or cost is one. A bit can store one unit of information, and vice versa, a random bit costs one unit of resources to produce. Binary entropy for a more complex random object can be measured in terms of how many random bits one needs to describe it. The binary entropy of a random vector of n independent fair coin flips is n, because we can describe it by n individual fair coins.

For the generation of discrete or integer-valued random variables, which includes the vast area of the generation of random combinatorial structures, one can adhere to a clean model, the pure bit model, in which each bit operation takes one time unit, and storage can be reported in terms of bits. In this model, one assumes that an i.i.d. sequence of independent perfect bits is available. This permits the development of an elegant information-theoretic theory. For example, Knuth and Yao (1976) showed that to generate a random integer X described by the probability distribution

$$\mathbf{P}\{X=n\}=p_n, n\geq 1,$$

any method must use an expected number of bits greater than the binary entropy of the distribution,

$$\sum_{n} p_n \log_2(1/p_n).$$

They also showed how to construct tree-based generators that can be implemented as finite or infinite automata to come within three bits of this lower bound for any distribution. While this theory is elegant and theoretically