

**Springer Theses**

Recognizing Outstanding Ph.D. Research

Endao Han

# Transient Dynamics of Concentrated Particulate Suspensions Under Shear



Springer

# **Springer Theses**

Recognizing Outstanding Ph.D. Research

## **Aims and Scope**

The series “Springer Theses” brings together a selection of the very best Ph.D. theses from around the world and across the physical sciences. Nominated and endorsed by two recognized specialists, each published volume has been selected for its scientific excellence and the high impact of its contents for the pertinent field of research. For greater accessibility to non-specialists, the published versions include an extended introduction, as well as a foreword by the student’s supervisor explaining the special relevance of the work for the field. As a whole, the series will provide a valuable resource both for newcomers to the research fields described, and for other scientists seeking detailed background information on special questions. Finally, it provides an accredited documentation of the valuable contributions made by today’s younger generation of scientists.

### **Theses are accepted into the series by invited nomination only and must fulfill all of the following criteria**

- They must be written in good English.
- The topic should fall within the confines of Chemistry, Physics, Earth Sciences, Engineering and related interdisciplinary fields such as Materials, Nanoscience, Chemical Engineering, Complex Systems and Biophysics.
- The work reported in the thesis must represent a significant scientific advance.
- If the thesis includes previously published material, permission to reproduce this must be gained from the respective copyright holder.
- They must have been examined and passed during the 12 months prior to nomination.
- Each thesis should include a foreword by the supervisor outlining the significance of its content.
- The theses should have a clearly defined structure including an introduction accessible to scientists not expert in that particular field.

More information about this series at <http://www.springer.com/series/8790>

Endao Han

# Transient Dynamics of Concentrated Particulate Suspensions Under Shear

Doctoral Thesis accepted by the University  
of Chicago, IL, USA

 Springer

Endao Han  
Joseph Henry Laboratories of Physics  
Princeton University  
Princeton, NJ, USA

ISSN 2190-5053

ISSN 2190-5061 (electronic)

Springer Theses

ISBN 978-3-030-38347-3

ISBN 978-3-030-38348-0 (eBook)

<https://doi.org/10.1007/978-3-030-38348-0>

© Springer Nature Switzerland AG 2020

This work is subject to copyright. All rights are reserved by the Publisher, whether the whole or part of the material is concerned, specifically the rights of translation, reprinting, reuse of illustrations, recitation, broadcasting, reproduction on microfilms or in any other physical way, and transmission or information storage and retrieval, electronic adaptation, computer software, or by similar or dissimilar methodology now known or hereafter developed.

The use of general descriptive names, registered names, trademarks, service marks, etc. in this publication does not imply, even in the absence of a specific statement, that such names are exempt from the relevant protective laws and regulations and therefore free for general use.

The publisher, the authors, and the editors are safe to assume that the advice and information in this book are believed to be true and accurate at the date of publication. Neither the publisher nor the authors or the editors give a warranty, expressed or implied, with respect to the material contained herein or for any errors or omissions that may have been made. The publisher remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

This Springer imprint is published by the registered company Springer Nature Switzerland AG.  
The registered company address is: Gewerbestrasse 11, 6330 Cham, Switzerland

*To my family*

*The greatest obstacle to discovery is not ignorance—it is the illusion of knowledge.*

—Daniel J. Boorstin

# Supervisor's Foreword

How does the flow of a simple liquid change when particles are added to it? This was calculated by Albert Einstein in his PhD thesis over 100 years ago for small volume fractions of particles and subsequently extended by others to increasingly larger fractions. The result is that the suspension's resistance to applied shear, i.e., its viscosity, rises rapidly as more and more particles are added, to the point where all flow becomes arrested and the suspension's viscosity diverges. Underlying this divergence is the mechanism of jamming: beyond some critical volume fraction there simply is no longer room for neighboring particles to move with respect to one another and the whole suspension turns rigid, exhibiting a solid-like yield stress. Exactly when the jamming transition will occur, i.e., what value the critical volume fraction for jamming will assume, depends on details of the particle–particle interactions, which in turn is controlled by aspects such as the particles' shape and their surface properties. This type of isotropic jamming transition, controlled only by the particle density, describes the response to applied shear when the suspension is at rest. There is, however, another possibility to induce jamming, namely by driving an initially fluid suspension into a rigid state. This type of dynamic jamming occurs without any overall change in the volume fraction of particles. Instead, it is a consequence of the fact that shear reorganizes particles into anisotropic configurations. These configurations can establish load-carrying force chains as long as the particle volume fraction is not too low and the particle–particle contacts are sufficiently frictional. This thesis demonstrates how suspensions provide a model system for investigating such jamming by shear and it describes some of the remarkable consequences of the associated dynamic transformation that converts a fluid into a solid in a fully reversible manner.

A key aspect of jamming by shear in suspensions is that the process proceeds along rapidly moving fronts. Ahead of a front the suspension is still in its initial, fluid state, while behind the front the suspension has been transformed into a solid-like state. The thesis breaks new ground in establishing a constitutive framework that relates the properties of shear-jamming fronts, such as their propagation speed, to the applied shear stress and strain. In treating the dynamic, effectively transient conversion of fluid into solid, this significantly extends prior work on jamming



phase transitions, which only considered steady-state conditions. As the thesis shows, the local shear stress in the front region is set by the external stress applied at the boundary of the suspension. This enables a completely new way of performing stress-controlled experiments: by using the jamming fronts to generate conditions of controllable local stress, a method is introduced that overcomes a critical limitation of standard steady-state rheology, which cannot establish spatially uniform stress conditions in the interior of a concentrated suspension as jamming is approached. Finally, the thesis introduces high-speed ultrasound imaging as a powerful experimental technique to image propagating shear jamming fronts and extract the associated flow field.

As a whole, the work described here has significantly advanced our understanding of how jamming by shear can reversibly solidify a dense suspension and how this transformation depends on both the suspension properties and the kind of forcing that is applied. In concert with the powerful experimental techniques that are introduced, this opens up exciting new avenues for further research.

Chicago, IL, USA  
January 29, 2020

Heinrich Jaeger

# Acknowledgments

I want to express my most sincere gratitude to my advisor, Heinrich Jaeger, for all the support he consistently provided over the years. Nothing that I have been working on at Chicago could have been achieved without his insights, advice, encouragement, and patience. From Heinrich, I learned not only how to be a good scientist, but also how to be a better person. His influence on me is on a wide range of scales.

At the James Franck Institute, I am incredibly fortunate to have had the chance to be around faculty who are interested, open-minded, and treat every scientific problem seriously. I want to thank Sidney Nagel and Thomas Witten for many inspiring discussions and useful advice. Every moment with them was a memorable learning experience for me. Bozhi Tian always had great ideas during a discussion, and no matter when I sent him an email, he replied within a few minutes. I would also like to thank my thesis committee members, Arvind Murugan and Stephan Meyer, for their valuable inputs on my research and thesis.

I am very grateful to my collaborators at Chicago and other institutions. Matthieu Wyart showed me how an outstanding theorist thinks. Working with him was both challenging and exciting. Patrick La Riviere provided much help when we set up the ultrasound system, and his lectures kick-started my research with ultrasound. Yin Fang, Yuanwen Jiang, Xianghui Xiao, and Jin Wang opened doors for me that led to brand new research opportunities. I am delighted to have been part of this wonderful collaboration between people with such diverse backgrounds. I enjoyed working with Rui Zhang, Tonia Hsieh, Swapnil Pravin, and Kenneth Bader on various projects. I also appreciate the expertise of Qiti Guo, Justin Jureller, Helmut Krebs, Luigi Mazzenga, and John Phillips. They were always there when I was in trouble.

I am particularly thankful for my labmates. Ivo Peters is a good mentor, collaborator, and friend. I can never thank him enough for all the help he offered. I can hardly think of a better person than Nicole James to share an office with for five years. When I needed to work with any chemical that was not tap water, I asked Nicole first. Scott Waitukaitis and Qin Xu provided great help when I was an innocent rookie and had no idea what to do. I would also like to thank Victor

Lee, Yifan Wang, Mengfei He, Sayantan Majumdar, Marc Miskin, Kieran Murphy, Leah Roth, Adam Wang, Melody Lim, Nigel Van Ha, Liang Zhao, Michael van der Naald, Daniel Hexner, Irmgard Bischofberger, Kimberly Weirich, Andrzej Latka, Noah Mitchell, Sofia Magkiriadou, Edward Barry, Tom Caswell, Carlos Orellana, Justin Burton, Michelle Driscoll, Nidhi Pashine, and everyone else in the Jaeger and Nagel labs. Thank you for all the help during this unforgettable journey.

My special appreciation to Tom Mullin, who showed me the beauty of fluids and grains before I came to Chicago.

Last but not least, I thank my parents, Peiji Han and Xiuqin Xue, for everything they gave me. Special thanks to my lovely wife Junchi Li, for her companionship and support through good and bad times. She is my sunshine every day.