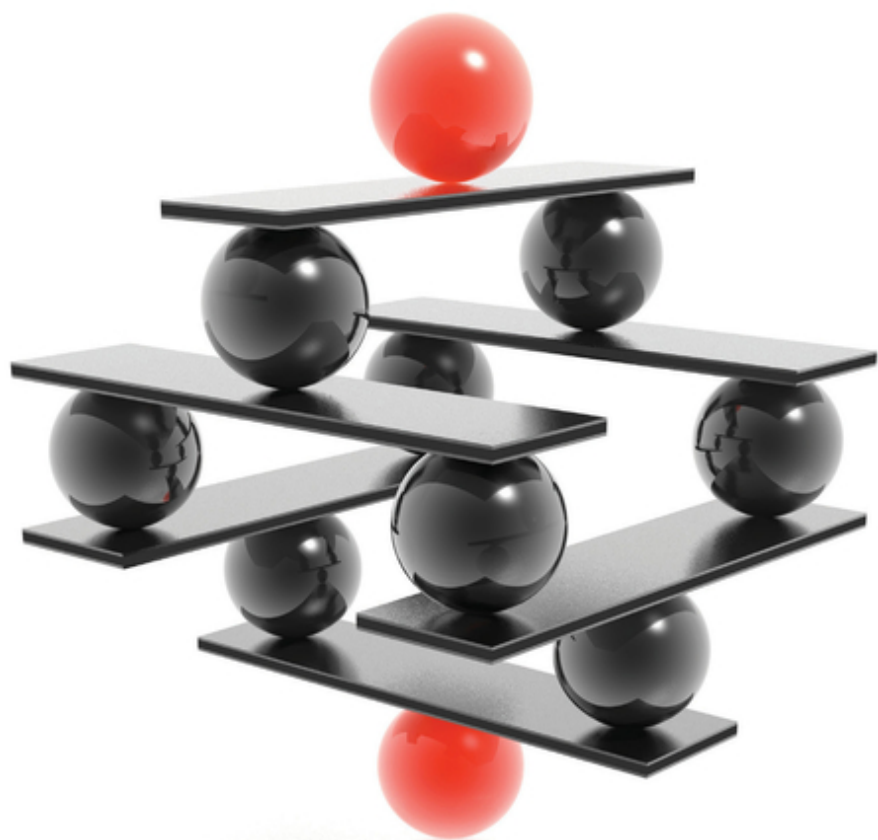


KEITH CUTHBERTSON | DIRK NITZSCHE | NIALL O'SULLIVAN

# DERIVATIVES

THEORY AND PRACTICE



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# Derivatives

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Theory and Practice

Keith Cuthbertson  
Dirk Nitzsche  
Niall O'Sullivan

WILEY

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*To Alfred Stanley*

—*Keith Cuthbertson*

*To Emily and Jacqueline*

—*Dirk Nietzsche*

*To my parents and Sara*

—*Niall O'Sullivan*



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