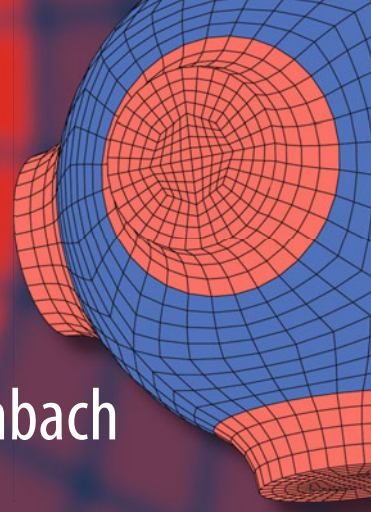


Advanced Structured Materials

Andreas Öchsner · Holm Altenbach  
*Editors*



# Engineering Design Applications

 Springer

# **Advanced Structured Materials**

Volume 92

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Editors

# Engineering Design Applications

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# Preface

Different engineering disciplines such as mechanical, materials, computer and process engineering provide the foundation for the design and development of improved structures, materials and processes. The modern design cycle is characterized by an interaction of different disciplines and a strong shift to computer-based approaches where only a few experiments are performed for verification purposes. A major driver for this development is the increased demand for cost reduction, which is also connected to environmental demands. In the transportation industry (e.g. automotive or aerospace), this is connected with the demand for higher fuel efficiency, which is related to the operational costs and the lower harm for the environment. One way to fulfil such requirements is lighter structures and/or improved processes for energy conversion. Another emerging area is the interaction of classical engineering with the health and medical sector. This volume gives an overview on recent developments in the mentioned areas of modern engineering design application.

We would like to express our sincere appreciation to the representatives of Springer, in particular to Dr. Christoph Baumann, Senior Editor Engineering, who made this volume possible.

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Magdeburg, Germany

Prof. Dr.-Ing. Andreas Öchsner, D.Sc.  
Prof. Dr.-Ing. habil. Dr. h. c. mult.  
Holm Altenbach

# Contents

<b>A Remedy for a Family of Dissipative, Unconditionally Stable Explicit Integration Methods</b> . . . . .	1
Shuenn-Yih Chang and Chiu-Li Huang	
<b>Development and Characterization of AA5083 Reinforced with SiC and Al<sub>2</sub>O<sub>3</sub> Particles by Friction Stir Processing</b> . . . . .	11
Eman M. Zayed, N. S. M. El-Tayeb, M. M. Z. Ahmed and Ragaie M. Rashad	
<b>Influence of the Change in Relative Dielectric Constant on Partial Discharge in Insulators</b> . . . . .	27
Ivica Kuzmanić and Igor Vujović	
<b>Dynamic and Noise Characteristics of Lead Screw in Vehicle Power Seat Adjuster</b> . . . . .	43
Sung-Yuk Kim and Key-Sun Kim	
<b>ICT-Based Integrated Operation Management System Design and Plant Growth Monitoring System Development for Plant Factories</b> . . . . .	55
Y. C. Kim and M. T. Cho	
<b>Cable Railway Simulation: A Two-Span Oscillator Model</b> . . . . .	65
Markus Wenin, Michael Irschara, Stephan Obexer, Maria Letizia Bertotti and Giovanni Modanese	
<b>Beams with Quadratic Function's Variation of Height</b> . . . . .	81
Matjaž Skrinar and Denis Imamović	

<b>Design and Manufacture of a Forearm Prosthesis by Plastic 3D Impression for a Patient with Transradial Amputation Applied for Strum of a Guitar</b> .....	97
Beatriz Romero-Ángeles, Daniel Hernández-Campos, Guillermo Urriolagoitia-Sosa, Christopher René Torres-San Miguel, Rafael Rodríguez-Martínez, Jacobo Martínez-Reyes, Rosa Alicia Hernández-Vázquez and Guillermo Urriolagoitia-Calderón	
<b>Numerical Analysis of the Knee Articulation Leg. The Angular Position Parameters and Forces Acting on the Joint Were Obtained and Applied into the Corresponding, During Different Stages of the Gait Process</b> .....	123
Guillermo Urriolagoitia-Sosa, Beatriz Romero-Ángeles, Daniel Méndez-Romero, Rafael Rodríguez-Martínez, Christopher René Torres-San Miguel, Jacobo Martínez-Reyes, Rosa Alicia Hernández-Vázquez and Guillermo Urriolagoitia-Calderón	
<b>Automatic Modeling of Surfaces with Identical Slopes</b> .....	143
Victorina A. Romanova, Marina Rynkovskaya and Vyacheslav Ivanov	
<b>Analytical Method to Analyze Right Helicoid Stress-Strain</b> .....	157
Marina Rynkovskaya and Vyacheslav Ivanov	
<b>Effect of Anisotropy of Masonry on the Behaviour of Unreinforced and Confined Masonry Walls Under Ground Motion</b> .....	173
Marija Smilovic, Jure Radnic, Nikola Grgic and Goran Baloevic	
<b>New Procedure to Construct an Anisotropic Elastic FE-Model Based on Swine Femoral Bones Using Numerical Modeling</b> .....	187
Rafael Rodríguez-Martínez, Christopher René Torres-San Miguel, Guillermo Urriolagoitia-Sosa, Beatriz Romero-Ángeles and Guillermo Urriolagoitia-Calderón	
<b>Fatigue Safety Design of Automotive Rear Sub-frame by Using CAE (Computer Aided Engineering) Static Analysis</b> .....	201
Kee Joo Kim and Jun-Hyub Park	
<b>Magnetic Field Distribution Around Magnetized Steel Ropes and Its Modulation by Rope Defects</b> .....	211
Jaromír Pištora, Michal Lesňák, Jan Valíček, Marta Harničárová and Vladimír Vrabko	
<b>Analysis of the Wear Damage on Offshore Gas Turbine Blades</b> .....	221
Luz Yazmin Villagrán-Villegas, Luis Héctor Hernández-Gómez, Miguel Patiño-Ortiz, Juan Alfonso Beltrán-Fernández, Julian Patiño-Ortiz, Juan Rodrigo Laguna-Camacho, Maricela Cuellar-Orozco and Miguel Toledo-Velazquez	

**Termomechanical Analysis of 3D Printing Specimens (Acrylonitrile Butadiene Styrene)** . . . . . 237  
 Juan Atonal-Sánchez, Juan Alfonso Beltrán-Fernández, Luis Héctor Hernández-Gómez, Luz Yazmin-Villagran, Juan Alejandro Flores-Campos, Adolfo López-Lievano and Pablo Moreno-Garibaldi

**2D Crack Problems in Functionally Graded Magneto-Electro-Elastic Materials** . . . . . 255  
 Yonko Stoynov

**Nonlinear Dynamic Behaviour of a Rectangular Thin Plate with a Bifurcation Diagram** . . . . . 267  
 Sohayb Abdul Karim

**Topological and Contact Force Analysis of a Knee Tumor Prosthesis** . . . . . 291  
 T. De la Mora Ramirez, M. A. Doñu Ruiz, I. Hilerio Cruz, N. López Perrusquia and E. D. García Bustos

**Wettability, Interfacial Tension (IFT) and Viscosity Alteration of Nanofluids Under Electromagnetic (EM) Waves for Enhanced Oil Recovery (IFT) Applications** . . . . . 305  
 Kanchuan Lee, Muhammad Adil, Hasnah Mohd. Zaid, Beh Hoe Guan, Hassan Soleimani and Martin Weis

**Design and Characterization of a Mandibular Prosthesis Prototype by Hemimandibulectomy** . . . . . 313  
 Juan Alfonso Beltrán-Fernández, Iliana Picco-Díaz, Itzel Bantle-Chávez, Carolina Alvarado-Moreno, Luis Héctor Hernández-Gómez, Juan Luis Cuevas-Andrade, Mauricio González-Rebattú, Adolfo López-Lievano, Juan Alejandro Flores-Campos and Pablo Moreno-Garibaldi

**Development of a Sensitive System to Fixed Prosthesis in the Lumbar and Cervical Orthopedic Area** . . . . . 345  
 Rodrigo Vázquez-Machorro, Juan Alfonso Beltrán-Fernández, Alexander Reyes-Cruz, Luis Héctor Hernández-Gómez, Juan Atonal-Sánchez, Adolfo López-Lievano, Juan Alejandro Flores-Campos and Alejandro González Rebattu y González

**Solution Behavior Near an Envelope of Characteristics in Planar Flow of a Material Obeying the Double Slip and Rotation Model** . . . . . 363  
 Sergei Alexandrov and Alexander Pirumov

<b>Principal Stress Trajectories in Plane Strain and Plane Stress Plasticity</b> .....	373
Sergei Alexandrov and Alexander Pirumov	
<b>Design and Methodology to Produce Auxiliary Orthopedic Rehabilitation</b> .....	383
Alexander Reyes-Cruz, Juan Alfonso Beltrán-Fernández, Luis Héctor Hernández-Gómez, Irving Omar Cazares-Ramírez, Alejandro González-Rebattú y González, Juan Alejandro Flores-Campos and Adolfo López-Lievano	
<b>Design and Manufacturing of a Temporomandibular Joint (TMJ) Prosthesis for Mandibular Bone Necrosis Using the Finite Element Method</b> .....	393
Juan Alfonso Beltrán-Fernández, Luis Héctor Hernández-Gómez, Juan Luis Cuevas-Andrade, Jesús Eduardo Campa-Zuno, Alfredo de la Peña-Muñoz, José Manuel Guzmán-López, Pablo Moreno-Garibaldi and Adolfo López-Lievano	
<b>Evaluation of Hot Corrosion Behavior of APS and HVOF Sprayed Thermal Barrier Coatings (TBCs) Exposed to Molten Na<sub>2</sub>SO<sub>4</sub> + V<sub>2</sub>O<sub>5</sub> Salt at 1000 °C</b> .....	441
Mustafa Kaplan, Mesut Uyaner, Yasin Ozgurluk, Kadir Mert Doleker and Abdullah Cahit Karaoglanli	
<b>Wear Behavior of Severe Shot Peened and Thermally Oxidized Commercially Pure Titanium</b> .....	461
Okan Unal, Abdullah Cahit Karaoglanli, Yasin Ozgurluk, Kadir Mert Doleker, Erfan Maleki and Remzi Varol	
<b>Characterization of Scaffold Structures for the Development of Prostheses and Biocompatible Materials</b> .....	471
Luis Héctor Hernández-Gómez, Juan Alfonso Beltrán-Fernández, Marcelino Ramírez-Jarquín, Itzel Bantle-Chávez, Carolina Alvarado-Moreno, Alejandro González-Rebattú y González, Mauricio González-Rebattú y González, Juan Alejandro Flores-Campos, Pablo Moreno-Garibaldi, Nefi Pava-Chipol and Salatiel Pérez-Montejo	
<b>Evaluation of the Structural Integrity of a Boiling Water Reactor Skirt Under Stationary and Transient Loading Conditions</b> .....	495
Yunuén López Grijalba, Luis Héctor Hernández Gómez, Pablo Ruiz López, Guillermo Manuel Urriolagoitia Calderón, Gilberto Soto Mendoza, Alejandra Armenta Molina and Juan Alfonso Beltrán Fernández	
<b>Effective Thermal Conductivity of Fiber Reinforced Composites Under Orientation Clustering</b> .....	507
Zia Javanbakht, Wayne Hall and Andreas Öchsner	

# A Remedy for a Family of Dissipative, Unconditionally Stable Explicit Integration Methods



Shuenn-Yih Chang and Chiu-Li Huang

**Abstract** A family of dissipative structure-dependent integration methods has been developed for structural dynamics. In general, this family of methods can integrate favorable numerical properties together, such as the unconditional stability, explicit formulation, second-order accuracy and controllable numerical damping. Due to the unconditional stability and explicit formulation, it is very computationally efficient for solving general structural dynamics problems. However, an adverse high-frequency overshooting behavior in the steady-state response might be generally experienced if this family of methods is applied to carry out the time integration. The cause of this overshoot is explored. It seems that the incomplete formulation of the difference equation for the displacement increment is responsible for this overshoot. Consequently, this overshooting can be completely eliminated after adding an appropriate load-dependent term into the difference equation for the displacement increment.

**Keywords** High-frequency overshoot · Steady-state response · Unconditional stability · Explicit formulation · Time integration method · Dynamic analysis

## 1 Introduction

Structure-dependent integration methods are a new type of time integration methods. It is well known that the coefficients of the two difference equations are generally scalar constants for conventional integration methods while they will become functions of the initial structural properties and the step size for structure-dependent integration methods. The first structure-dependent integration method was developed by Chang in 2002 and it can simultaneously have the unconditional stability

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and explicit formulation together [1]. Some other structure-dependent integration methods were proposed to improve numerical properties later [2–8]. Recently, some dissipative structure-dependent integration methods were successfully developed by using an asymptotic equation of motion [9–13]. All of the family methods were enhanced with desirable high-frequency numerical damping. One of them is a free parameter controlled family method [9]. In fact, the parameter  $p$  is applied to govern the numerical properties. This family method is referred as Chang dissipative method and will be abbreviated as CDM for brevity herein.

In general, CDM is performed very well in the general dynamic analysis and it is computationally efficient in the step-by-step solution of a nonlinear structural dynamic problem, where the total response is dominated by the low frequency modes while the high frequency responses are of no interest. However, it might experience a new type of overshoot in the steady-state response of a high frequency mode rather than in the early transient response. Notice that an overshoot in the early transient response has been found by Goudreau and Taylor in 1972 [14]. Clearly, the overshoot in this study is different from that found by Goudreau and Taylor since it only occurs under dynamic loading. In this work, the root cause of this overshoot is thoroughly studied and a load-correction scheme is proposed to overcome the overshoot.

## 2 Chang Dissipative Integration Method

The general formulation of CDM for a single degree of freedom system can be written as:

$$\begin{aligned}
 ma_{i+1} + c_0 v_{i+1} + \frac{2p}{p+1} k_{i+1} d_{i+1} - \frac{p-1}{p+1} k_i d_i &= \frac{2p}{p+1} f_{i+1} - \frac{p-1}{p+1} f_i \\
 d_{i+1} &= \beta_0 d_{i-1} + \beta_1 d_i + \beta_2 (\Delta t) v_i + \beta_3 (\Delta t)^2 a_i \\
 v_{i+1} &= v_i + \frac{3p-1}{2(p+1)} (\Delta t) a_i - \frac{p-3}{2(p+1)} (\Delta t) a_{i+1}
 \end{aligned} \tag{1}$$

where the coefficients  $\beta_0$  to  $\beta_3$  are found to be:

$$\begin{aligned}
 \beta_0 &= -\frac{1}{D} \left[ \frac{p-1}{8} \left( \frac{2}{p+1} \right)^3 \Omega_0^2 \right] \\
 \beta_1 &= 1 + \frac{1}{D} \left[ \frac{p-1}{8} \left( \frac{2}{p+1} \right)^3 \Omega_0^2 \right] \\
 \beta_2 &= \frac{1}{D} \left( 1 - \frac{p-3}{p+1} \xi \Omega_0 \right) \\
 \beta_3 &= \frac{1}{D} \left\{ \frac{1}{2} - \frac{1}{2} \left[ \left( \frac{2}{p+1} \right)^2 + \frac{p-3}{p+1} \right] \xi \Omega_0 \right\}
 \end{aligned} \tag{2}$$

where  $\xi$  is a viscous damping ratio;  $\Omega_0 = \omega_0 (\Delta t)$  and  $\omega_0 = \sqrt{k_0/m}$  is the natural frequency of the system determined from the initial stiffness  $k_0$ .

### 3 Overshoot Behavior

To illustrate that an unusual overshoot may occur in the steady-state response of a high frequency mode for CDM, the following equation of motion is solved.

$$\ddot{u} + \omega_0^2 u = \varepsilon \omega_0^2 \sin(\bar{\omega} t) \quad (3)$$

where  $\bar{\omega}$  is a driving frequency; and  $\varepsilon$  is a constant for adjusting the response amplitude. The exact solution of this equation for the initial conditions of  $u(0) = u_0$  and  $\dot{u}(0) = \dot{u}_0$  can be obtained from the fundamental theory of structural dynamics and is found to be:

$$u(t) = u_0 \cos(\omega_0 t) + \left( \frac{\dot{u}_0}{\omega_0} - \frac{\varepsilon \theta}{1 - \theta^2} \right) \sin(\omega_0 t) + \frac{\varepsilon}{1 - \theta^2} \sin(\bar{\omega} t) \quad (4)$$

where  $\theta = \bar{\omega}/\omega_0$  is a frequency ratio;  $u_0$  and  $\dot{u}_0$  are the initial displacement and velocity, respectively. There will be no transient response in the total response if the initial conditions are chosen to be  $u_0 = 0$  and  $\dot{u}_0 = \omega_0 \varepsilon \theta / (1 - \theta^2)$ .

Three systems are simulated by taking  $\omega_0 = 1, 100$  and  $1000$  rad/s corresponding to S1, S2 and S3. In addition, the driving frequency  $\bar{\omega} = 1.5$  rad/s is assumed for each analysis. This leads to  $\theta = 1.5, 1.5 \times 10^{-2}$  and  $1.5 \times 10^{-3}$  in correspondence to S1, S2 and S3. To demonstrate the unusual overshoot that might be experienced for CDM, two members of CDM are adopted to calculate the responses. The member of  $p = 1$  is referred as CDM1 while that of  $p = 0.75$  is referred as CDM2. Notice that CDM1 has no numerical damping while CDM2 can have a desired numerical damping. A time step of  $\Delta t = 0.1$  s is adopted for time integration. The calculated results are plotted in Fig. 1. This time step is small enough to accurately integrate the steady-state response since the value of  $\Delta t/\bar{T}_0$  is as small as  $3/40\pi$ , where  $\bar{T}_0 = 2\pi/\bar{\omega}_0 = 4\pi/3$ . It has been shown by Chang that a harmonic loading can be very accurately represented if  $\Delta t/\bar{T}_0$  is chosen to be less than  $1/12$  [15]. In Fig. 1 it is shown that either CDM1 or CDM2 can provide accurate solutions for S1 while an overshoot is found in the results of S2 and S3. In Fig. 1a–c it can be seen that the overshoot becomes more significant as the natural frequency increases; and there is almost no overshoot for a low frequency mode. Similar phenomena are also seen in Fig. 1d–f except for the amount of overshoot. This is because that CDM2 can have a desired numerical damping to suppress or even remove the high frequency mode and thus the results obtained from CDM2 show less significant overshoot for S2 and S3 when compared to CDM1. It is evident that CDM experiences an overshoot in the steady-state response of a high frequency mode.

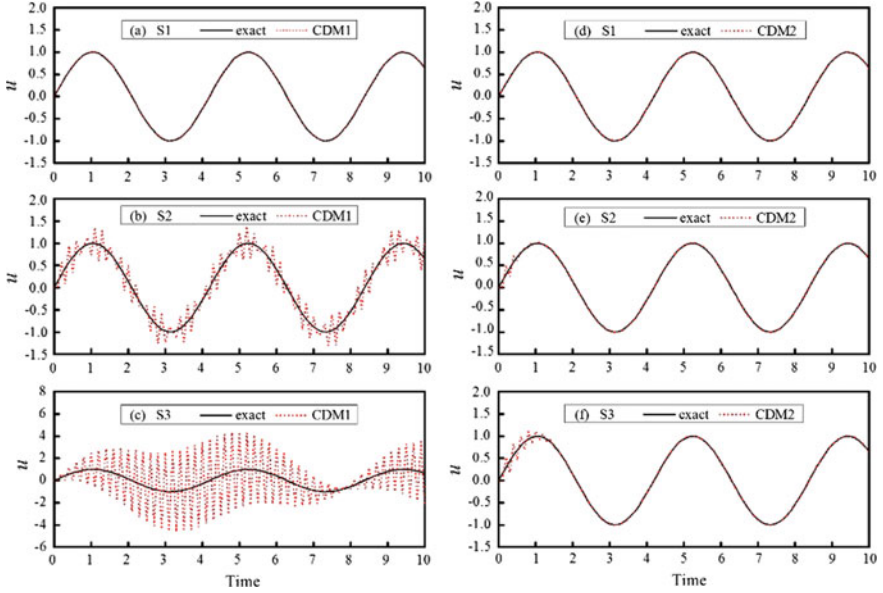


Fig. 1 Forced vibration responses to sine loading for using CDM1 and CDM2

## 4 Cause of Overshoot

In order to investigate the cause of the overshoot in the steady-state response of a high frequency mode, a local truncation error is constructed from a forced vibration response rather than a free vibration response since the dynamic loading is closely related to the overshoot. A local truncation error is defined as the error committed in each time step by using the differential equation to replace the difference equation. The derivations of the local truncation error for an integration method can be found in the references [1–5] and will not be elaborated herein.

After very complex algebraic manipulations, the local truncation error for CDM for zero viscous damping is found to be:

$$E = \frac{1}{D} \left\{ \left[ \frac{p(p-2)}{(p+1)^2} + \frac{1}{12} \right] (\Delta t)^2 \ddot{u} + \frac{1}{(p+1)^2} \frac{1}{m} (\Delta t)^2 \ddot{f}_i \right\} \quad (5)$$

where

$$D = 1 - \frac{p-3}{p+1} \xi \Omega_0 + \frac{p}{4} \left( \frac{2}{p+1} \right)^3 \Omega_0^2 \quad (6)$$

Clearly, a second-order accuracy can be generally achieved for CDM. It seems that the last error term in Eq. 5 plays the key issue to cause an overshooting phenomenon

in the steady-state response of a high frequency mode for CDM since it can be replaced by the other three terms of the second derivative of the equation of motion:

$$\frac{1}{m} (\Delta t)^2 \ddot{f}_i = \Omega_0^2 \ddot{u}_i + 2\xi \Omega_0 (\Delta t) \ddot{u}_i + (\Delta t)^2 \ddot{\ddot{u}}_i \quad (7)$$

After substituting this equation into Eq. 5, it will become:

$$E = \frac{1}{D} \left\{ \left[ \frac{(p-1)^2}{(p+1)^2} + \frac{1}{12} \right] (\Delta t)^2 \ddot{\ddot{u}}_i + \frac{1}{(p+1)^2} \Omega_0^2 \ddot{u}_i \right\} \quad (8)$$

In this equation, it is found that the second term is quadratically proportional to  $\Omega_0$ . Thus, the steady-state response might be almost unaffected by low frequency modes or a small value of  $\Omega_0$  while it might be drastically affected by high frequency modes or a large value of  $\Omega_0$ . Consequently, this local truncation error seems to explain why an overshoot behavior might occur in the steady-state response of a high frequency mode while there is no such overshoot for a low frequency mode.

## 5 A Proposed Remedy

Since the overshoot in the steady-state response is an adverse behavior for CDM, it is better to eliminate it to obtain an accurate solution. For this purpose, we want to propose a remedy to remove the adverse overshoot behavior in the steady-state response of a high frequency mode. It seems that a slight modification of the formulation of the CDM can be applied to remove the adverse overshoot behavior. Since this modification should not affect the original numerical properties of CDM, a load-dependent term is simply introduced into the difference equation for displacement increments. This is because any load-dependent term will not affect the eigen-analysis of the amplification matrix and thus numerical properties. As a result, the modified form of CDM can be expressed as:

$$\begin{aligned} ma_{i+1} + c_0 v_{i+1} + \frac{2p}{p+1} k_{i+1} d_{i+1} - \frac{p-1}{p+1} k_i d_i &= \frac{2p}{p+1} f_{i+1} - \frac{p-1}{p+1} f_i \\ d_{i+1} &= \beta_0 d_{i-1} + \beta_1 d_i + \beta_2 (\Delta t) v_i + \beta_3 (\Delta t)^2 a_i + q_{i+1} \\ v_{i+1} &= v_i + \frac{3p-1}{2(p+1)} (\Delta t) a_i - \frac{p-3}{2(p+1)} (\Delta t) a_{i+1} \end{aligned} \quad (9)$$

where  $q_{i+1}$  is a load-dependent term. This modified form of the CDM can be referred to as the MCDM herein for brevity. Based on this formulation, the local truncation error for MCDM can be also obtained by using the same procedure to derive that for CDM and it is found to be:

$$E = \frac{1}{D} \left\{ \left[ \frac{(p-1)^2}{(p+1)^2} + \frac{1}{12} \right] (\Delta t)^2 \ddot{u}_i + \frac{1}{(p+1)^2} \Omega_0^2 \ddot{u}_i \right\} - q_{i+2} + q_{i+1} \quad (10)$$

Apparently, this equation is very similar to Eq. 8, except that the last two error terms are closely related to the load-dependent term, which is intentionally introduced into the difference equation for displacement increments.

In Eq. 10, the load-dependent term  $q_{i+1}$  must be properly determined so that the quadratic error term  $\Omega_0^2 \ddot{u}_i / D (p+1)^2$  in Eq. 8 can be completely removed. After a series of algebraic manipulations, a possible choice of  $q_{i+1}$  is found to be:

$$q_{i+1} = \frac{1}{D} \frac{1}{(p+1)^2} \frac{1}{m} (\Delta t)^2 (f_{i+1} - f_i) + \frac{1}{D} \frac{p-1}{(p+1)^3} \frac{1}{m} (\Delta t)^2 (f_{i+1} - 2f_i + f_{i-1}) \quad (11)$$

Notice that the extra loading term is also structure dependent and the denominator is the same as that for  $\beta_0$  to  $\beta_3$ . After determining the extra loading term, the local truncation error for CDM is found to be:

$$E = \frac{1}{D} \left[ \frac{(p-1)^2}{(p+1)^2} + \frac{1}{12} \right] (\Delta t)^2 \ddot{u}_i \quad (12)$$

It is apparent that the adverse error term as shown in Eq. 8 is no longer in this local truncation error. This strongly indicates that the overshoot in the steady-state response of a high frequency mode is eliminated by the load-dependent term.

## 6 Numerical Confirmations

In order to verify the effectiveness of the proposed scheme, two numerical examples are examined by using MCDM. Notice that MCDM1 and MCDM2 are in correspondence to CDM1 and CDM2. Apparently, the only difference between CDM and MCDM in the formulation is that the latter has a load-dependent term.

### 6.1 Example 1

The illustrated example for a forced vibration response of a single degree of freedom system is solved again by using MCDM and the calculated results are plotted in Fig. 2. It is noteworthy that the calculated results obtained from MCDM1 and MCDM2 for a time step of  $\Delta t = 0.1$  s are overlapped together with the exact solutions in each plot

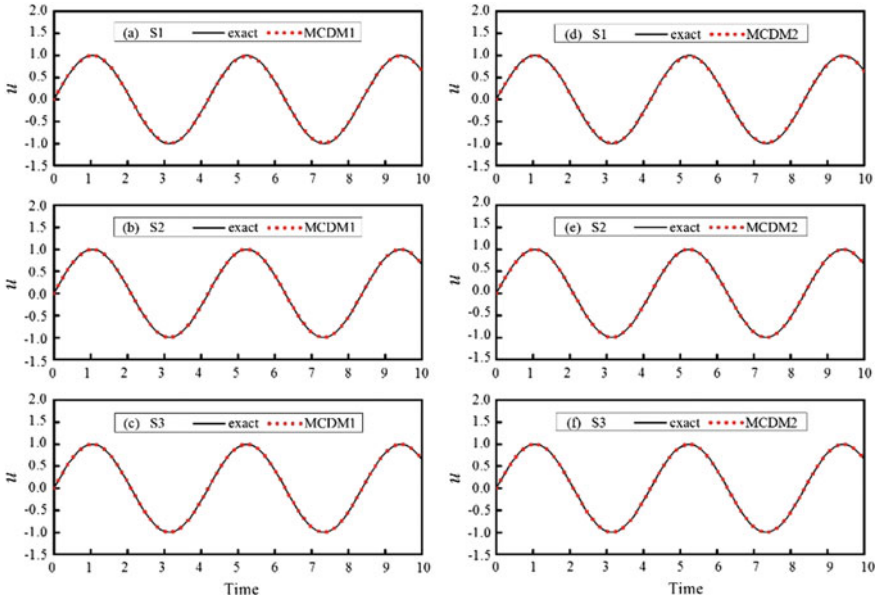


Fig. 2 Forced vibration responses to sine loading for using MCDM1 and MCDM2

of this figure. Thus, it is verified that the proposed scheme can effectively eliminate the adverse overshooting behavior in the steady-state response of a high frequency mode.

### 6.2 Example 2

In order to show that the adverse overshoot might experience in general dynamic analysis, a 10-story shear-beam type building is used to illustrate that an overshoot in the steady-state response of a high frequency mode may occur in practical applications. The building and its structural properties are shown in Fig. 3, where only a dynamic loading of  $10k_1 \sin(3t)$  is intentionally imposed upon the bottom story of the building. The lowest natural frequency of the building is found to be 16.52 rad/s, whereas the highest natural frequency is found to be  $10^4$  rad/s. Both CDM1 and CDM2 as well as MCDM1 and MCDM2 with a time step of  $\Delta t = 0.02$  s are applied to calculate the numerical results. The results obtained from CDM1 and MCDM1 are plotted in Fig. 4. For comparison, the solution obtained from the use of the constant average acceleration method (AAM) with  $\Delta t = 0.01$  s is considered as a reference solution.

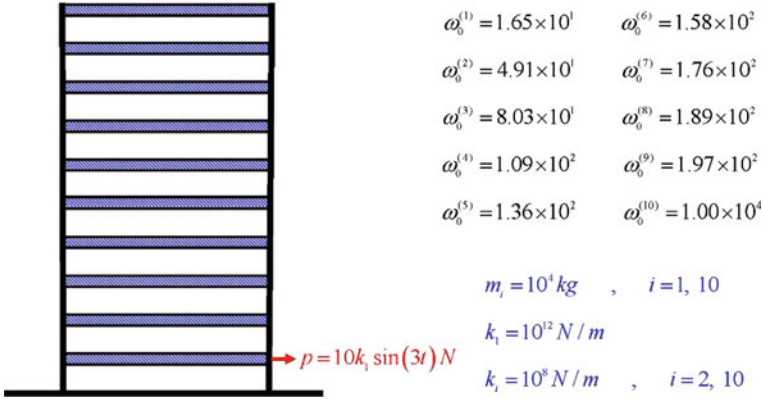


Fig. 3 A 10-story shear-beam type building and its structural properties

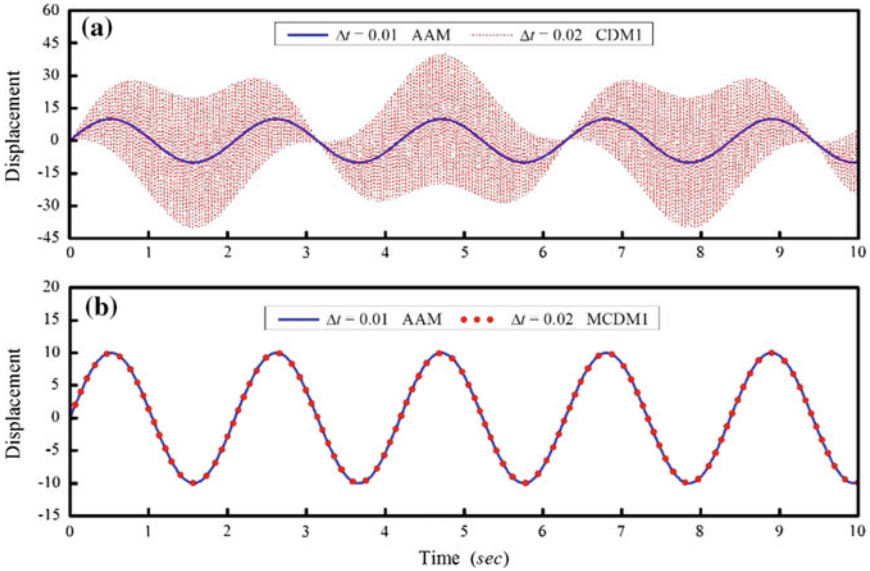


Fig. 4 Forced vibration response to 10-story building at bottom story

As shown in Fig. 4a, the response obtained from CDM1 for the bottom story of the 10-story building exhibits a very significant overshoot behavior. Contrary to this, there is almost no overshoot in Fig. 4b for the responses obtained from MCDM1 since the calculated results are coincided with the reference solutions. Notice that the displacement response at the bottom story is dominated by the steady-state response

since the period of this displacement response is exactly equal to  $2\pi/3$  s, which is the period of the sine loading. It is evident from this example that the proposed remedy can effectively remove the adverse overshoot in the steady-state response of a high frequency mode.

## 7 Conclusions

The one-parameter controlled Chang dissipative structure-dependent family method is very computationally efficient since it can simultaneously integrate the unconditional stability and explicit formulation together. In addition, it also has a second-order accuracy and desired numerical damping. However, it might experience an unusual overshoot in the steady-state response of a high frequency mode. This adverse overshooting can be revealed by the local truncation error constructed from a forced vibration response rather than a free vibration response. In addition, it can be used to derive a remedy to eliminate the adverse overshoot in the steady-state response of a high frequency mode. The remedy is to adjust the difference equation for displacement increment by adding an extra load-dependent term. The effectiveness of this remedy is confirmed by numerical examples in addition to the analytical study. As a result, the additional load-dependent term must be included in the general formulation of the one-parameter controlled Chang dissipative family method so that the adverse overshoot can be automatically eliminated.

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# Development and Characterization of AA5083 Reinforced with SiC and Al<sub>2</sub>O<sub>3</sub> Particles by Friction Stir Processing



Eman M. Zayed, N. S. M. El-Tayeb, M. M. Z. Ahmed and Ragaie M. Rashad

**Abstract** In this work, friction stir process (FSP) was performed to enhance the surface properties of the aluminum alloy 5083 by incorporating SiC of 6  $\mu\text{m}$  average size, Al<sub>2</sub>O<sub>3</sub> of 3  $\mu\text{m}$  average size and mixture of SiC/Al<sub>2</sub>O<sub>3</sub> particles in the alloy. Tensile tests, Vickers micro hardness measurements, wear tests, and optical and scanning electron microscopies (SEM) examination were conducted on the surface of Aluminum alloy 5083 to analyze the processed zones of composite samples. Results of tensile tests revealed that ultimate tensile strength of 120 MPa was obtained at 600 rpm. The average hardness increased by 30% with increasing the content of ceramic particles and the maximum hardness values obtained for the hybrid surface composite (50% Al<sub>2</sub>O<sub>3</sub> and 50% SiC) developed by 2 passes FSP and processing parameters of 600 rpm. The addition of ceramic powder (SiC) as a reinforcement into AA5083 improved the wear resistance of the received AA5083 by 40%. Hybrid composite of 50% SiC and 50% Al<sub>2</sub>O<sub>3</sub> exhibited a superior wear resistance compared to the 100% SiC or 100% Al<sub>2</sub>O<sub>3</sub> at a normal load of 20 N.

**Keywords** Aluminum alloy AA5083 · FSP · Surface modification  
Metal matrix composites · Hybrid surface composite

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## 1 Introduction

Aluminum and its alloys have versatile properties; they are lightweight in addition, their high strength to weight ratio and excellent resistance to corrosion make them suitable for use in structural applications like military, aerospace and transportation industries. However, in some applications, the surface needs to have better mechanical properties such as improved strength and better hardness [1]. Therefore, the reinforcement of surface layer of the component by hard ceramic particles is highly desirable to achieve the required properties while the substrate still maintains the original structure with good ductility and thermal conductivity [2].

In the past, attempts to fabricate metal matrix composites by adding particulate material to the molten alloy followed by casting have not been successful [3]. It has been postulated that the major difficulty in this approach is that the interfacial reaction between reinforcement and metal-matrix cannot be avoided in addition to the formation of some detrimental phases. Therefore, if processing of surface composite is carried out at temperatures below melting point of the substrate, the problems mentioned above can be avoided [4].

Friction stir processing has been evolved as a successful solid state processing technique based on the principle of friction stir welding developed by Mishra [5, 6]. FSP leads to a localized severe plastic deformation of the material and thus can be used for homogenization of microstructure and for grain refinement, thereby resulting in improved material properties. Little or no macroscopic shape change may occur despite the local severity of the plastic deformation [7].

In the view of the above it can be concluded that FSP can be employed to enhance the surface properties (viz. micro-hardness, wear resistance, among others) of metals and their alloys. However, the work pertaining to enhancement of surface properties of aluminum/aluminum alloys through friction stir processing (FSP) is rather scant. In this regard the aim of this study is to investigate the effect of incorporating the surface of AA5083 with micro-sized SiC and Al<sub>2</sub>O<sub>3</sub> particles and mixture of them through friction stir processing on its mechanical properties and to study the influence of FSP parameters on the microstructure of the developed metal matrix composite (MMC). In addition to the effect of varying the composition of reinforcement material on mechanical properties (i.e. hardness and tensile) and tribological properties (i.e. wear) were studied with respect to the process parameters.

## 2 Experimental Procedure

### 2.1 Material Used

In this study, a cold rolled aluminium alloy (AA5083) plate of 10 mm thickness, 200 mm length, and 50 mm width has been used for the purpose of carrying out FSP. A groove was machined at the center of the substrates with a width of 3 mm and a

**Table 1** Nominal chemical composition of 5083 Al alloy (wt%) [8]

	Si	Fe	Cu	Mn	Cr	Mg	Ti	Zn	Al
wt%	0.40 max	0.40 max	0.10 max	0.40/1.0	0.0/0.25	4.0/4.90	0.15 max	0.25 max	Balance

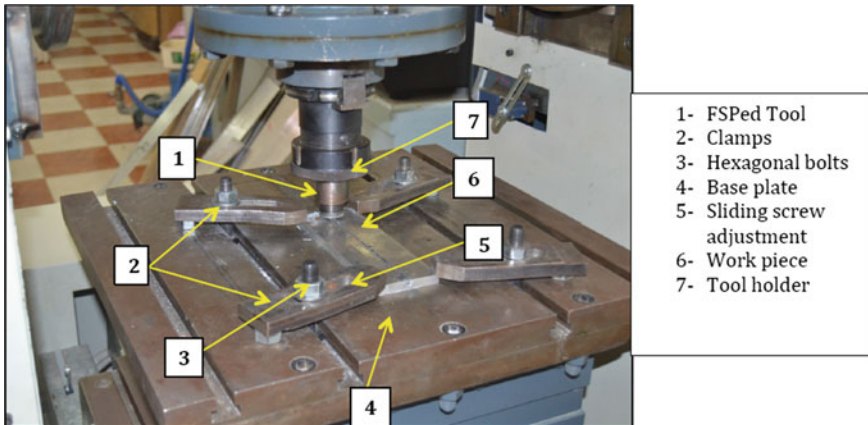
depth of 6 mm. The nominal chemical composition of the alloy 5083 is summarized in Table 1.

The surface of AA5083 is incorporated through FSP with micro-sized SiC and Al<sub>2</sub>O<sub>3</sub> powder to produce the (MMC).

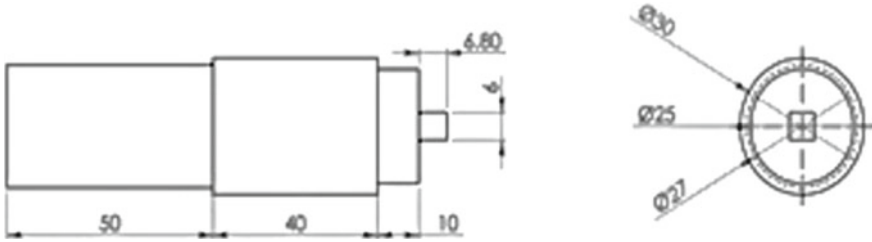
## 2.2 Friction Stir Processing (Equipment)

Figure 1 shows the FSP setup used for carrying the development of MMCs.

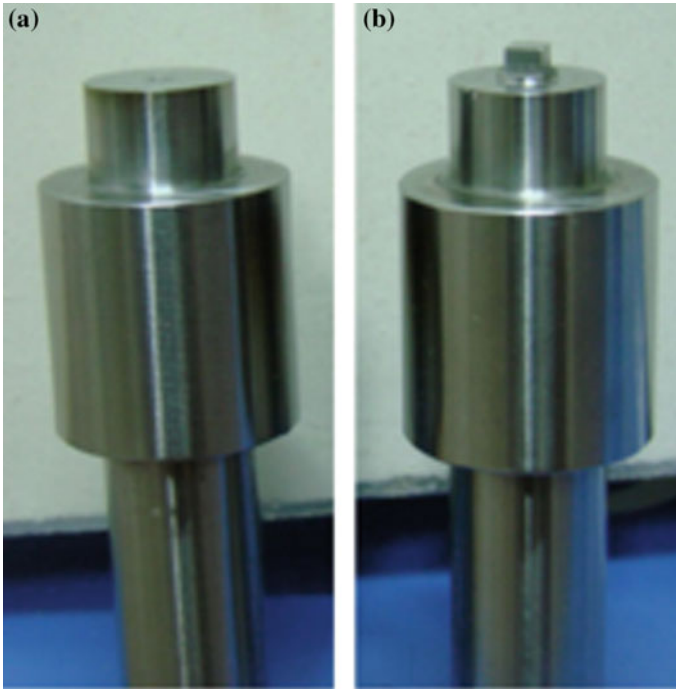
A FSP tool of H13 tool steel with shoulder of 25 mm diameter and square probe of 6 mm width and 6 mm length was used to perform the FSP with a schematic shown in Fig. 2, before the start of the actual FSP. The top surface of the grooves was closed using penless tool as shown in Fig. 3a of 25 mm diameter shoulder to prevent the escape of the packed particles during the process and then the FSP was then performed at rotation rate of 400, 600, 800 rpm, constant traverse speed of 60 mm/min, depth of 6 mm, and tool tilt angle was set at 3° with the conventional tool as manifested in Fig. 3b.



**Fig. 1** Clamping arrangement during friction stir processing



**Fig. 2** Schematic illustration of the used FSP tool dimension



**Fig. 3** Friction stir processing tool **a** pinless tool **b** conventional FSP tool

### 2.3 *Metallographic Preparation*

Representative sections from the FSPed samples were cut and then were grounded progressively using silicon carbide (SiC) paper, from p60 to p1200 grades, in which each stage progressively removes and replaces the larger surface scratches with smaller ones.

The samples were then polished on 6 and 3  $\mu\text{m}$  diamond cloths for 3–5 min, and finally with an alumina suspension for 5–10 min. Note that after each grinding and polishing step, the samples were washed thoroughly using methanol and air-dried.

## 2.4 Microstructural Characterization

### *Optical Microscopy (OM)*

The microstructure of the prepared specimens was examined using an optical microscope linked to a high-resolution digital camera. The microstructures were revealed after etching using Keller's reagent.

### *Scanning Electron Microscope (SEM)*

Quanta 250 Field Emission Gun—Scanning Electron Microscope (FEI model: Quanta FEG-250-SEM) was used to examine the reinforcement ceramic particles (SiC and Al<sub>2</sub>O<sub>3</sub>) and worn surface of the friction stir processed specimens and then they were further analyzed using Energy Dispersive X-Ray Spectroscopy (EDX) within the SEM instrument.

## 2.5 Mechanical Properties Characterization

To verify the feasibility of using FSP to enhance the mechanical properties of AA 5083, tensile strength and micro-hardness testing at ambient temperature was conducted for FSPed specimens and compared to the As-received AA5083.

### *Micro-hardness Test*

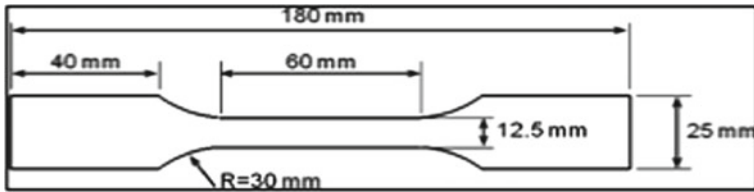
Hardness measurements were carried out on the polished samples. The micro hardness was measured using Vickers hardness tester, the test was carried out at load of 10 HV. The reported results are the average of 10 readings.

### *Tensile Test*

In order to determine the mechanical properties of the materials after FSP, tensile specimens were cut out from the processed zone (PZ) and machined to the specified dimensions according to *ASTM E8* as shown in Fig. 4 of 10 mm and gauge length 50 mm parallel to the processing direction, and tested at room temperature under uni-axial tensile conditions using a universal tensile testing machine. All results were based on the average of three samples from three different processed plates.

## 2.6 Tribological Characterization

Dry wear behavior of the base metal and surface composite layer (SCL) was studied using a pin on ring tribo-tester. The wear tests were conducted for base material at normal force of 20 N, sliding distance of 800 m and constant track diameter 370 mm. The wear rate is calculated depending on the weights before and after the wear test. The wear behavior of surface composite layer processed after the second pass with



**Fig. 4** Schematic diagram showing the dimensions of the tensile specimens used in the uni axial tensile experiment



**Fig. 5** Surface appearance of friction stir processed surface at 400 rpm and 100% SiC

additives SiC and  $Al_2O_3$  particles at different FSP conditions were compared with the wear behavior of base material.

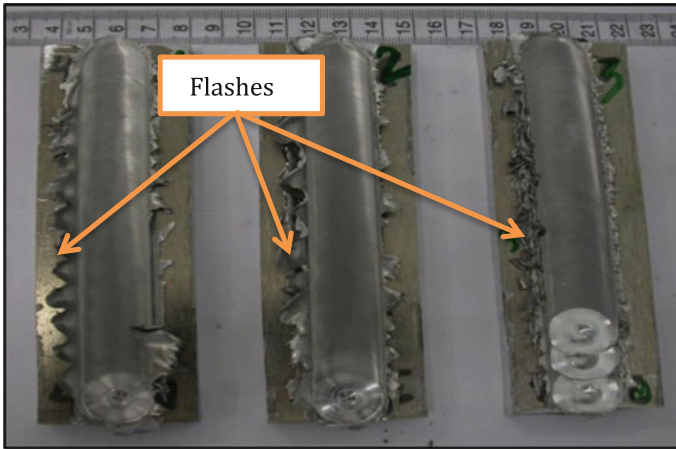
### 3 Results and Discussion

Figures 5 and 6 show the surface appearance of some of the processed surfaces produced at different composition of ceramic particles and rotational speeds. The processed surface showed a considerable amount of flash. A good appearance with a little flash was observed at the lower rotational speed of 400 rpm. The higher flash associated with the higher rotational speed may be attributed to the higher plunging forces applied.

#### 3.1 Microstructural Evolutions

##### 3.1.1 Optical Microstructure

From the micrograph images shown in Fig. 7, it was observed that the agglomeration size of ceramic particles is reduced by increasing number of FSP passes which resulted in improvement of reinforcement particles distribution. Furthermore, pro-



**Fig. 6** Surface appearance of friction stir processed surface at 800 rpm and 100% SiC

cessing ceramic particles dispersed more homogenously in the base metal at low rpm, microstructures show that good dispersion areas than with high rpm, since there are voids formed due to low action of homogeneity that resulted from high rotation. This result is in a good agreement with Kwon et al. [9] who studied the FS processed Al 1050 alloy and found the hardness and tensile strength of the FS processed 1050 aluminum alloy were observed to increase significantly with decreased tool rotation speed.

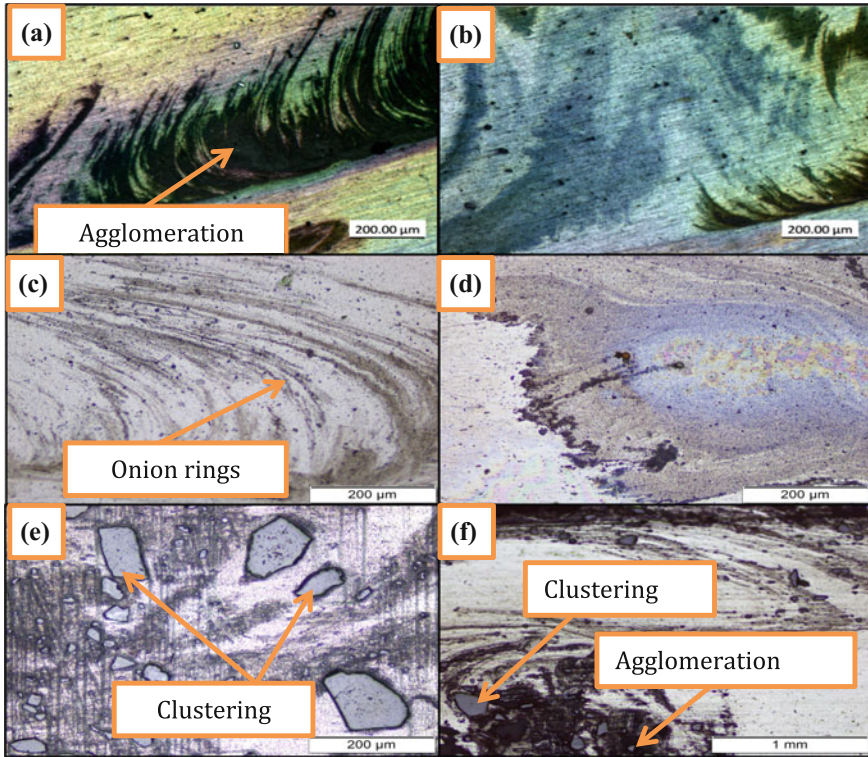
Formation of onion rings is one of the characteristics of FSP, which is found in Fig. 7c.

Figure 7f represents the micro-structure of the hybrid composition of SiC and  $Al_2O_3$  particles at rotational speeds 400 rpm. As shown, clustering of reinforcement particles was observed in Fig. 7f due to the large size of SiC powders, Increasing the number of FSP passes can eliminate this feature.

### 3.1.2 SEM Microstructure

Figures 8a–f illustrate the SEM micrographs of the nugget cross-sections for processing parameters 400, 600 and 800 rpm for additive composition SiC,  $Al_2O_3$  and mixture of them. Figure 8c shows a uniform distribution of  $Al_2O_3$  powders in the stir zone, Clustering occurs at 800 rpm as shown in Fig. 8f.

Another important note should be mentioned is the alteration of the shape of the nugget with variation of processing parameters. Mishra and Ma [5] represented two types of stirring zone (nugget), basin-shaped nugget and elliptical nugget. For 400 rpm, elliptical-shaped nugget, was observed in Fig. 8e.



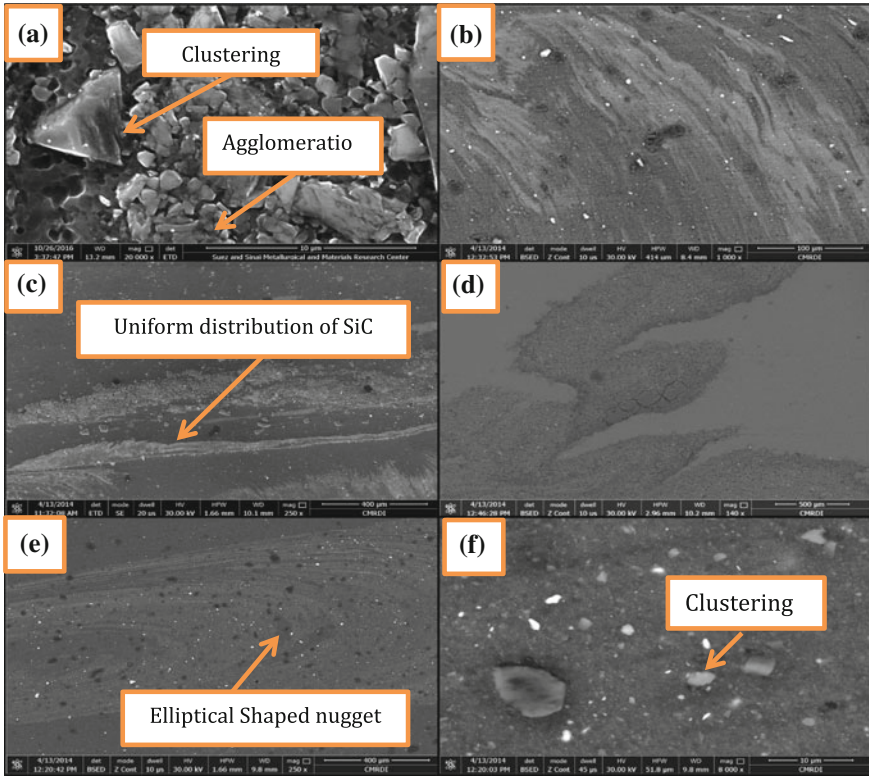
**Fig. 7** Optical microscopy images for processed specimens with SiC and Al<sub>2</sub>O<sub>3</sub> at different rotational speeds

## 3.2 Hardness

### 3.2.1 Effect of Reinforcement Particles Type on Hardness

Micro hardness of friction stir processed specimens was taken using Vickers hardness machine under load of 10 HV. The average hardness values are shown in Table 2 and Fig. 10. It is observed that Vickers hardness values depend on the rotational speeds and this can be interpreted by the frictional heat generated as a result of rubbing of the tool with the matrix. The quantity of frictional heating generated is dependent upon the tool rotation speed. As the tool rotation increases, the amount of frictional heating causing softening and sliding of material during FSP will also increase. Also coarsening of grains due to high heat generated was the main reason for the lowest hardness of those FSPed samples which have been produced at the higher rotation rate compared to the other with lower rotation rate.

It is observed from Fig. 9 that the hybrid surface composites having equal composition (50% SiC and 50% Al<sub>2</sub>O<sub>3</sub>) exhibit more hardness than the surface composite



**Fig. 8** SEM images for processed specimens with SiC and Al<sub>2</sub>O<sub>3</sub> at different rotational speeds

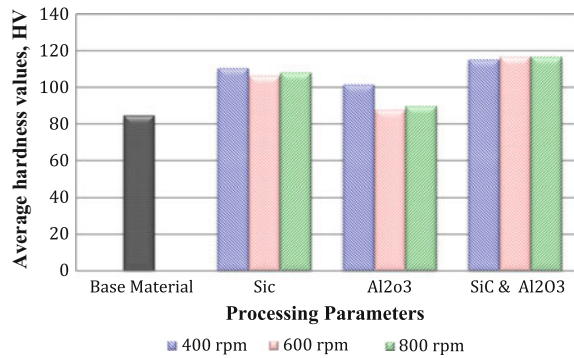
**Table 2** Hardness average values

Composition	Rotational speed (rpm)	Hardness avg. (HV)
SiC	400	110.8
	600	106.6
	800	108.4
Al <sub>2</sub> O <sub>3</sub>	400	101.8
	600	62.34
	800	84.4
SiC and Al <sub>2</sub> O <sub>3</sub>	400	115.5
	600	117
	800	117

fabricated using other composition of ceramic particles and this result is in a good agreement with Keerthivel et al. [10].

Figures 10 a–c show the micro hardness profile measured across top surface of the FSPed specimens. It is observed that the hardness of processed zone is signifi-

**Fig. 9** Effect of the content of ceramic powders and rotational speeds in rpm on the average hardness, HV



cantly higher than that observed for the as-received AA5083 base alloy which has an average hardness of 85 HV. The highest value is observed to be 230 HV for the specimen that underwent 2 passes of FSP at 50% SiC and 50% Al<sub>2</sub>O<sub>3</sub>. The Vickers hardness value has been characterized as rotational speed dependent [11]. As previously mentioned, the change in rotational and traverse speeds would alter the temperature profile, as well as the exposure time, in the stir zone; this will affect the microstructural characteristics. It can be observed that either increasing the rotational speed and/or changing the type and composition of ceramic powder affect the mechanical properties.

### 3.3 Evaluation of Tensile Strength

A tensile test of FSPed specimens was carried out. Figure 11 a–c show results of the tensile tests for FSPed specimens with different additive compositions at different rotational speeds. Table 3 shows the ultimate tensile strength (UTS) as well as the 0.2% offset yield values for each FSPed specimen. Two processed specimens were tested for each processing condition and the failure loads were averaged.

The effect of the rotational speed on the ultimate tensile strength of the processed zones is shown in Fig. 12. When the processing is carried out at 600 rpm and with an additive composition of 50% SiC and 50% Al<sub>2</sub>O<sub>3</sub>, ultimate tensile strength reached to the maximum value of 120 MPa. Conversely by further increasing the rotational speed to 800 rpm, tensile strength slightly decreased again. The reason behind decreasing the UTS values is the incorporation of ceramic particles, which increase the brittleness of the FSPed specimens. However the ductility of the material was greatly improved.